

# Summary-data-based Mendelian randomisation and prediction of gene targets

Zhihong Zhu, Ph.D

Senior Researcher, NCRR, Aarhus University  
Visitor, PCTG, University of Queensland  
[z.zhu@econ.au.dk](mailto:z.zhu@econ.au.dk) | [z.zhu1@uq.edu.au](mailto:z.zhu1@uq.edu.au)



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AARHUS UNIVERSITY

22 JUNE 2022

ZHIHONG ZHU  
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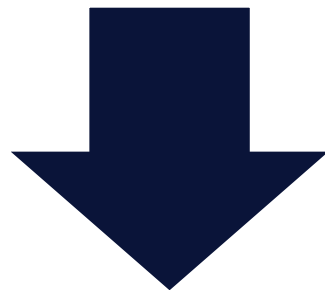
# Outlines

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## Summary-data-based Mendelian randomisation (SMR)

- Purposes of SMR
- Concept of SMR method
- A real example of SMR test
- SMR software
- Practical

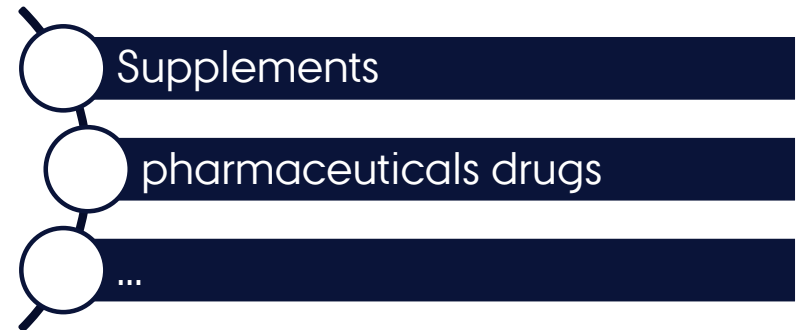
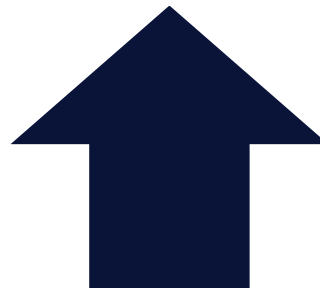
# Causal inference



Increasing risks  
of disorders



Therapy and  
side effects



# Risk gene – *CACNA2D4*

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The *CACNA2D4* gene, one of voltage-dependent calcium-channel genes, is an important gene target of anti-hypertensive drugs. It is a risk gene for both bipolar disorder and schizophrenia.

*CACNA2D4* | hypertensive disorder -> schizophrenia / bipolar disorder | hypertensive disorder

Given the independence of hypertensive disorder and schizophrenia / bipolar disorder  
*CACNA2D4* -> schizophrenia / bipolar disorder

# Observational study

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In observational study, regression model is used to test association,

$$y_j = x_j\beta + e_j$$

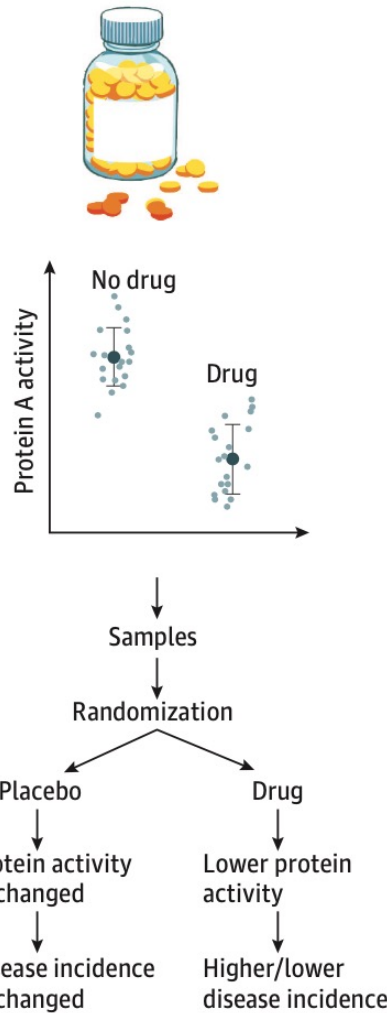
The ordinary least square estimate,

$$\hat{\beta}_{OLS} = (x^T x)^{-1} x^T y = (x^T x)^{-1} x^T (x\beta + e) = \beta + (x^T x)^{-1} x^T e$$

If there is confounding factor, then  $\hat{\beta}_{OLS}$  is biased.

# Randomised controlled trial

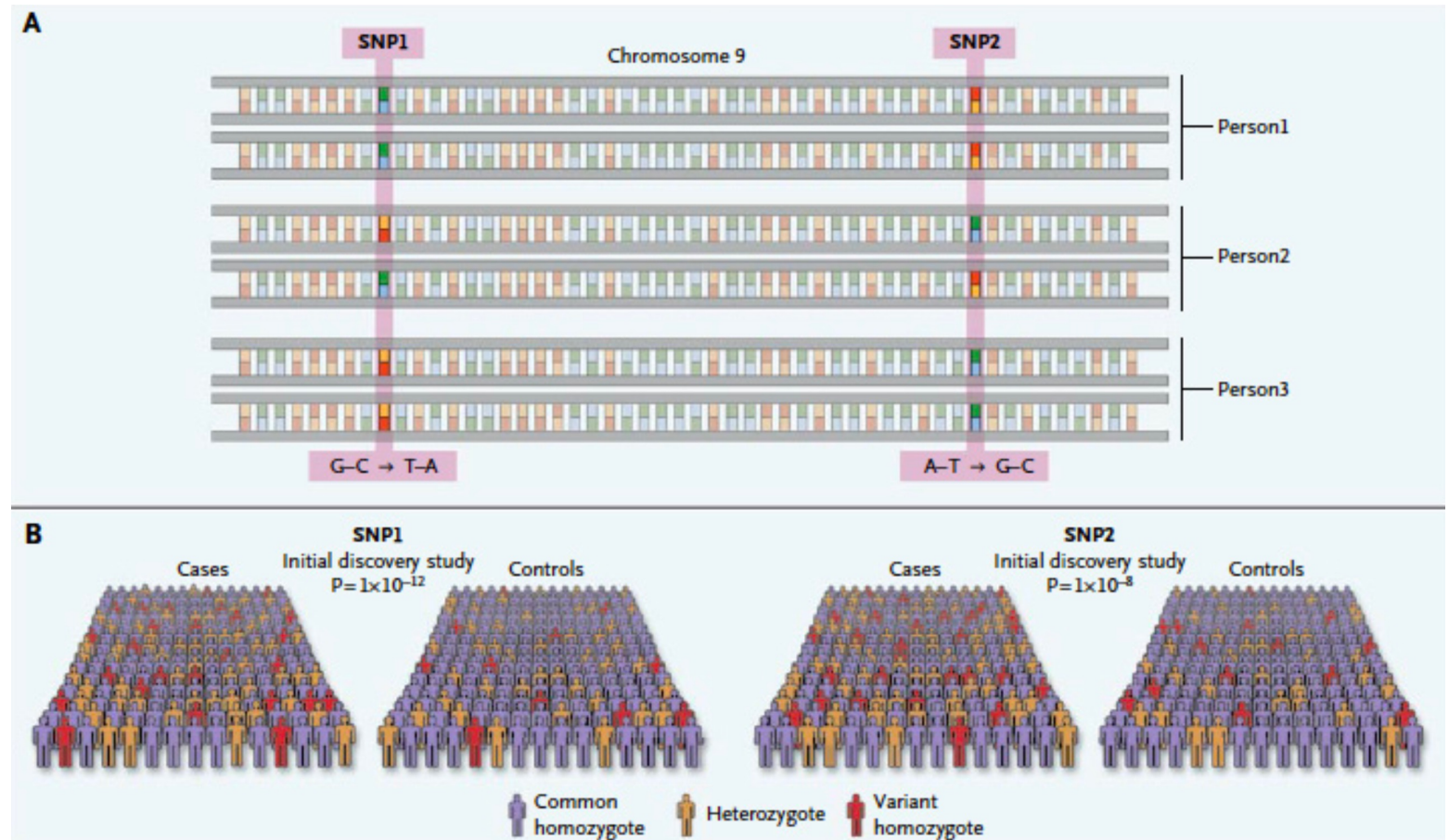
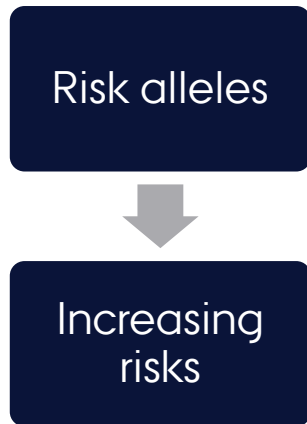
Randomized clinical trial



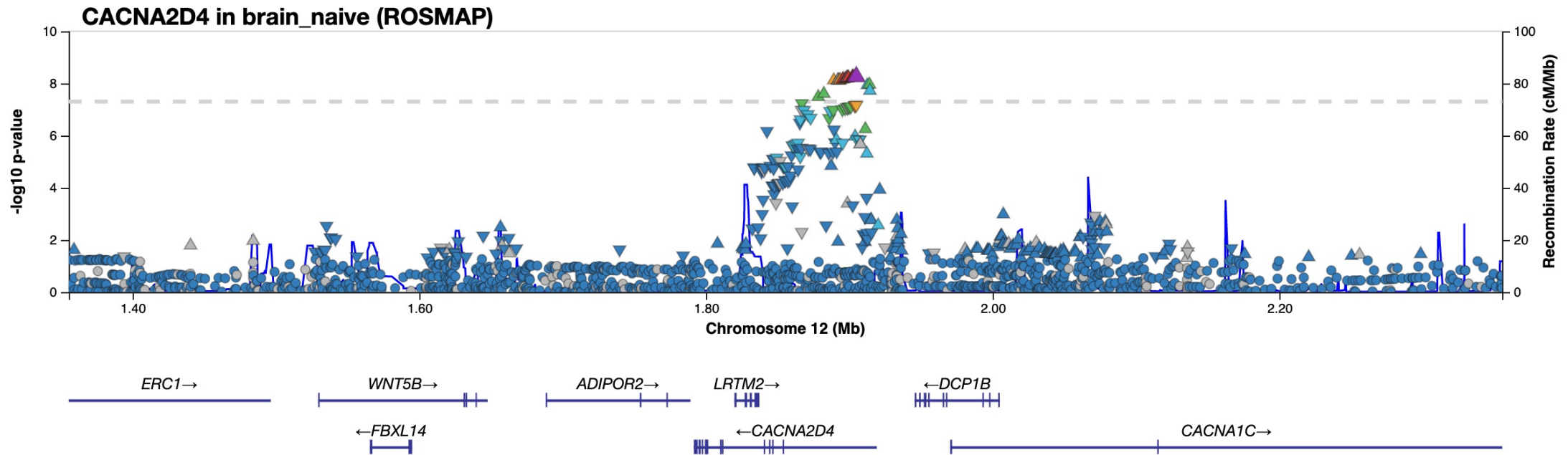
| Assumptions         | RCT   |
|---------------------|---|
| Two designed Groups | a) Treatment group<br>b) Control group                                    |
| Assignment          | Randomly assigning subjects to treatment conditions                       |
| Confounder          | Prior exposure and instrumentation do not threaten the internal validity. |
| Test                | The difference must be driven by intervention.                            |

Chauquet et al 2021 JAMA Psychiatry

# SNP (DNA variant)



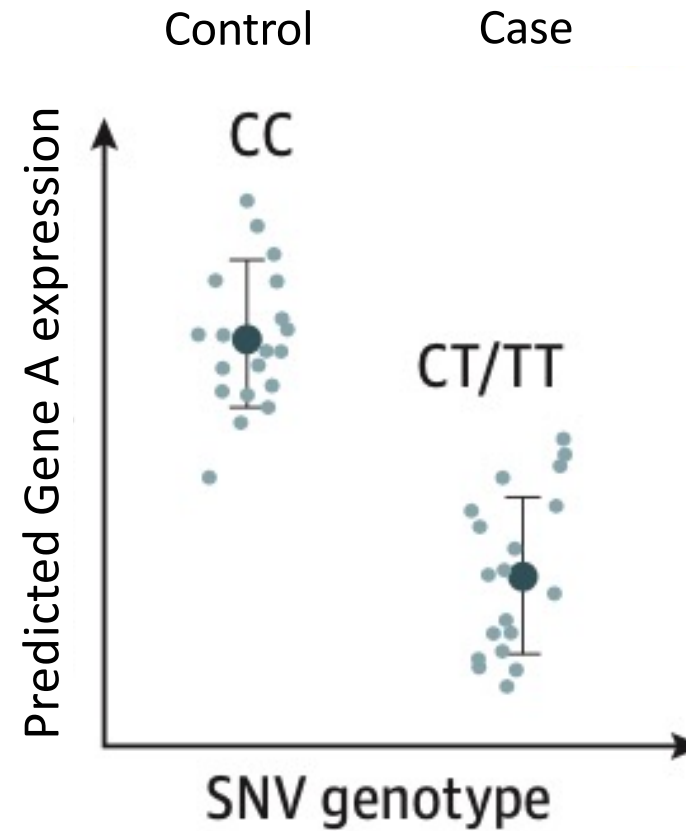
# eQTL study



allele -> lower gene expression

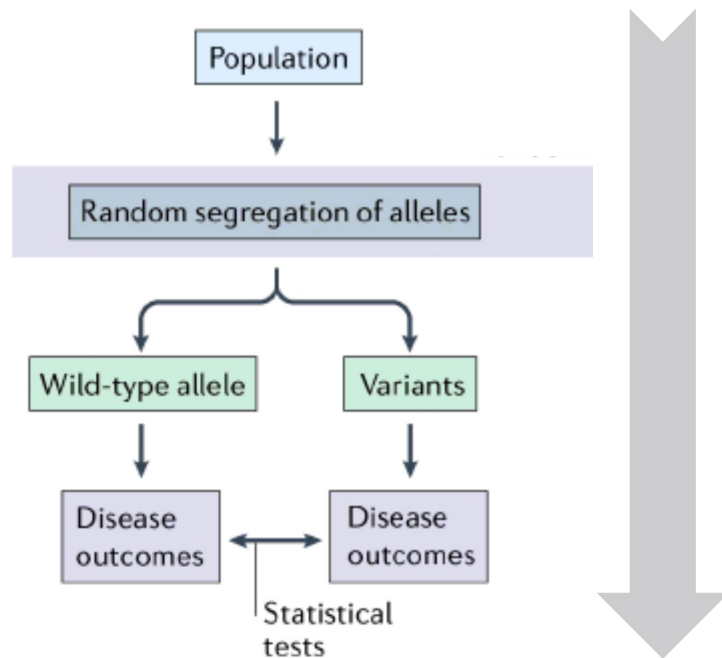


# Predicting heritable traits



# Mendelian randomisation

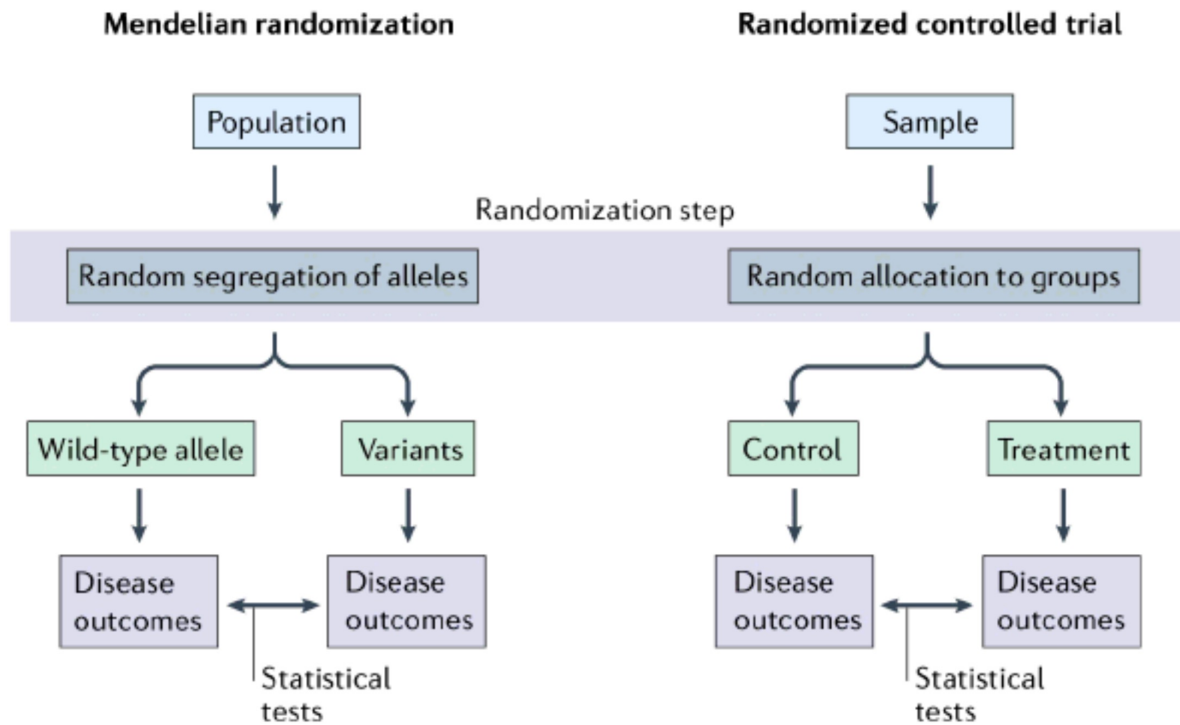
## Mendelian randomization



- DNA variant
- Risk factor
- Outcome

|             |                 |             |
|-------------|-----------------|-------------|
|             | Non-risk allele | Risk allele |
| DNA variant |                 |             |
| Risk factor | Normal          | Deficiency  |
| Outcome     | Low risk        | High risk   |

# Similar concept

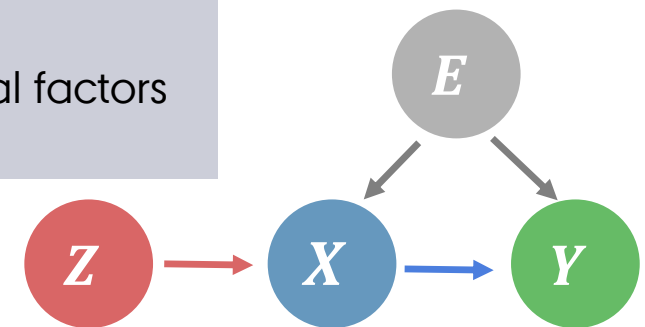


Wald ratio estimator

$$\beta = \frac{E(\text{Disorder}|A = 1) - E(\text{Disorder}|A = 0)}{E(\text{Risk factor}|A = 1) - E(\text{Risk factor}|A = 0)}$$

# Strength of MR

|            | RCT  | MR   |
|------------|--|--|
| Ethics     | Ethical issues, e.g . confidentiality, informed consent, etc.            | Using SNPs (DNA variants) as instruments               |
| Expense    | Time-consuming and expensive   | Many available genotyped populations and GWAS datasets |
| Confounder | Prior exposure and instrumentation do not threaten the internal validity | Free of environmental factors                          |

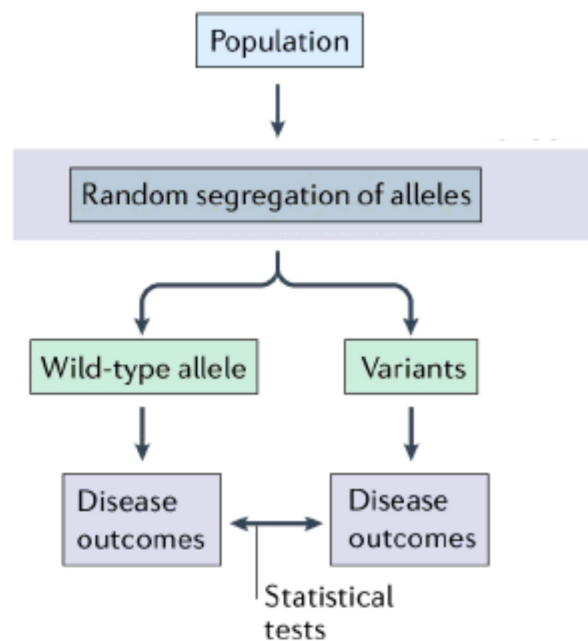


# Two-stage least square estimate

$$\text{Disorder} = \text{Risk factor} + e$$

Instruments (Z) ←

## Mendelian randomization



Risk factor (X)

- Regression of risk factor on instrument
- $$X = Z\delta + \text{error}$$

Disorder (Y)

- Regression of disorder on predicted risk factor
- $$Y = \hat{X}\beta + \text{error}$$

# Two-stage least square estimate



$$E(\hat{\beta}_{2LSL}) = (\hat{x}^T \hat{x})^{-1} \hat{x}^T y = \frac{x^T P_Z y}{x^T P_Z x} = \beta + \frac{x^T P_Z e}{x^T P_Z x} \quad \text{where } P_Z = Z(Z^T Z)^{-1} Z^T$$

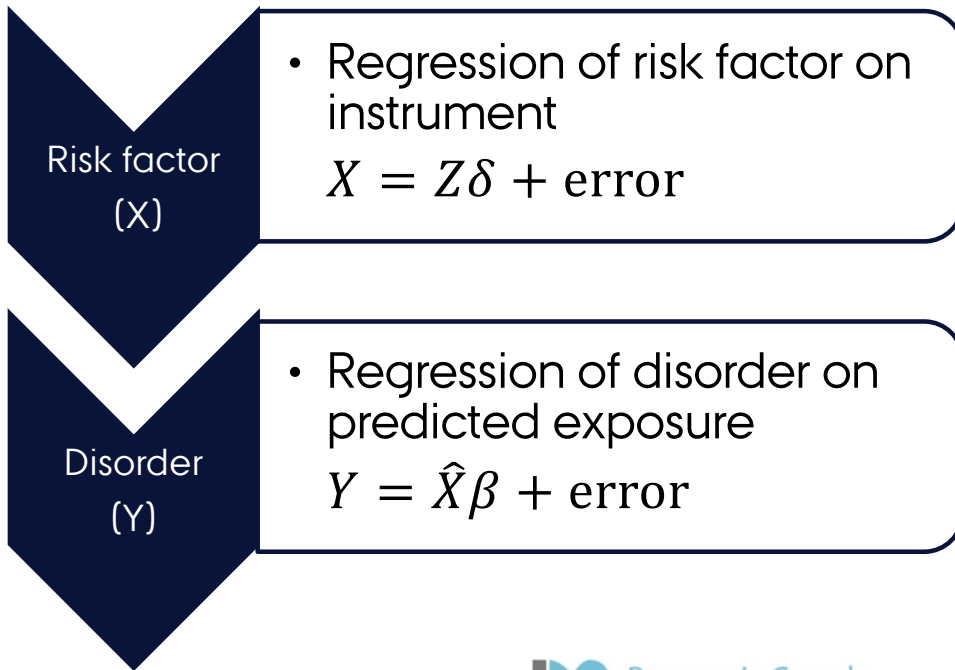
Note: Z should be associated with x, 1)  $P_Z x \neq 0$ , 2) attenuated effect

SNP instruments are independent of environmental factors,  $Z^T e = 0$

$$E(\hat{\beta}_{2LSL}) = \beta$$

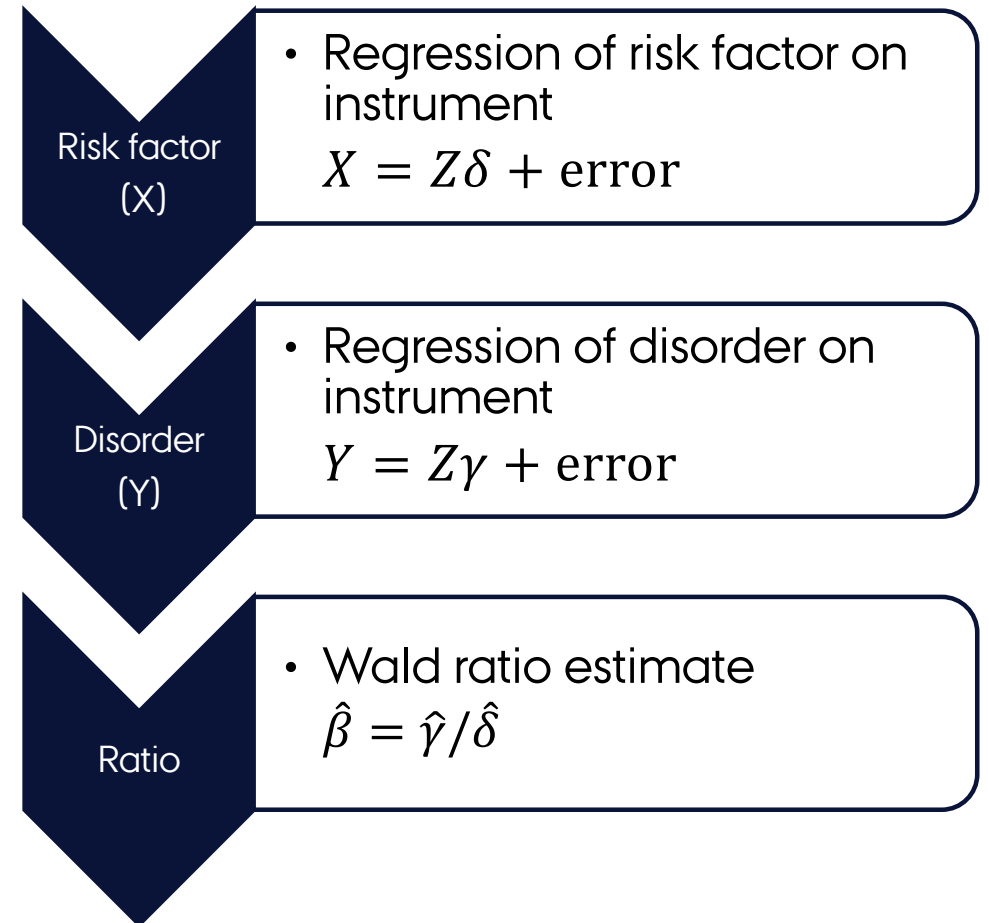
# MR using summary statistics

Individual-level data



=

Summary-level data



# Summary-data based method

$$E(\hat{\beta}_{2LSL}) = (\hat{x}^T \hat{x})^{-1} \hat{x}^T y = \frac{x^T P_Z y}{x^T P_Z x} = (\hat{x}^T \hat{x})^{-1} \hat{x}^T \hat{y} = \hat{\gamma} / \hat{\delta}$$

For a single SNP instrument

$\hat{\delta}$  from mQTL, eQTL, sQTL, etc.

$\hat{\gamma}$  from GWAS etc.



# Summary-data-based MR

|              | 2LSL – single instrument | Summary-data-based MR |
|--------------|--------------------------|-----------------------|
| Data         | Individual-level data    | Summary-level data    |
| Availability | May not be available     | eQTL, GWAS, etc.      |

# Risk gene - *CACNA2D4*

| Gene            | SNP       | A1 / A2 | Data                    | <i>b</i> | SE     | <i>P</i> -value |
|-----------------|-----------|---------|-------------------------|----------|--------|-----------------|
| <i>CACNA2D4</i> | rs1044825 | G / T   | eQTL<br>(blood)         | 0.447    | 0.0186 | 4.1E-128        |
|                 |           |         | GWAS<br>(schizophrenia) | -0.0377  | 0.0087 | 1.3E-5          |

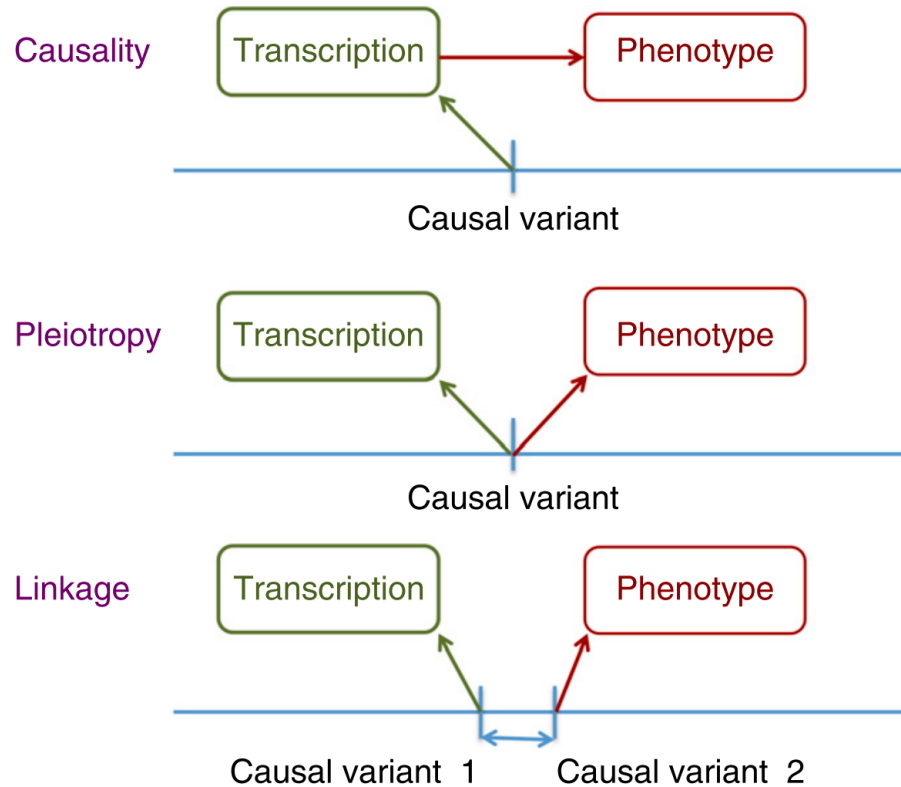
$$\hat{\beta} = -\frac{0.0377}{0.447} = -0.084$$

$$SE(\hat{\beta}) \approx \sqrt{\left(\frac{\gamma}{\delta}\right)^2 \left[ \frac{var(\delta)}{\delta^2} + \frac{var(\gamma)}{\gamma^2} \right]} = 0.020$$



*P*-value = 2.0E-5

# Linkage model

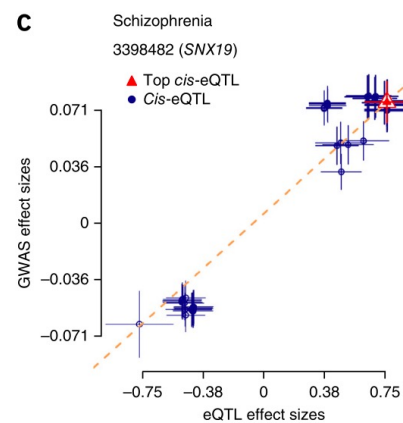
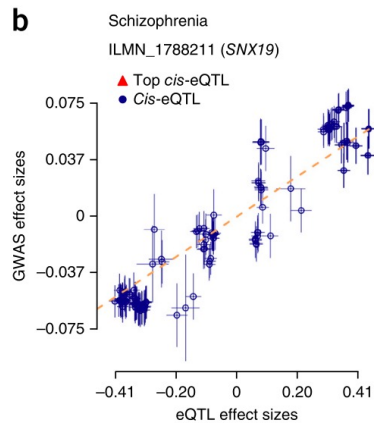
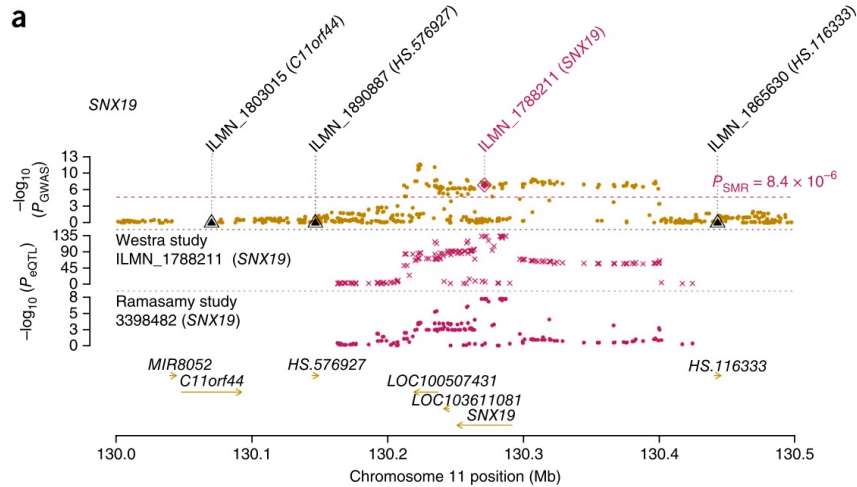


Unable to distinguish pleiotropy from causality

HEIDI (HEterogeneity In Dependent Instruments).

Using SNPs in LD with top *cis*-SNP

# HEIDI



The top SNP

- $\hat{\beta}_{top} = \hat{\gamma}_{top} / \hat{\delta}_{top}$

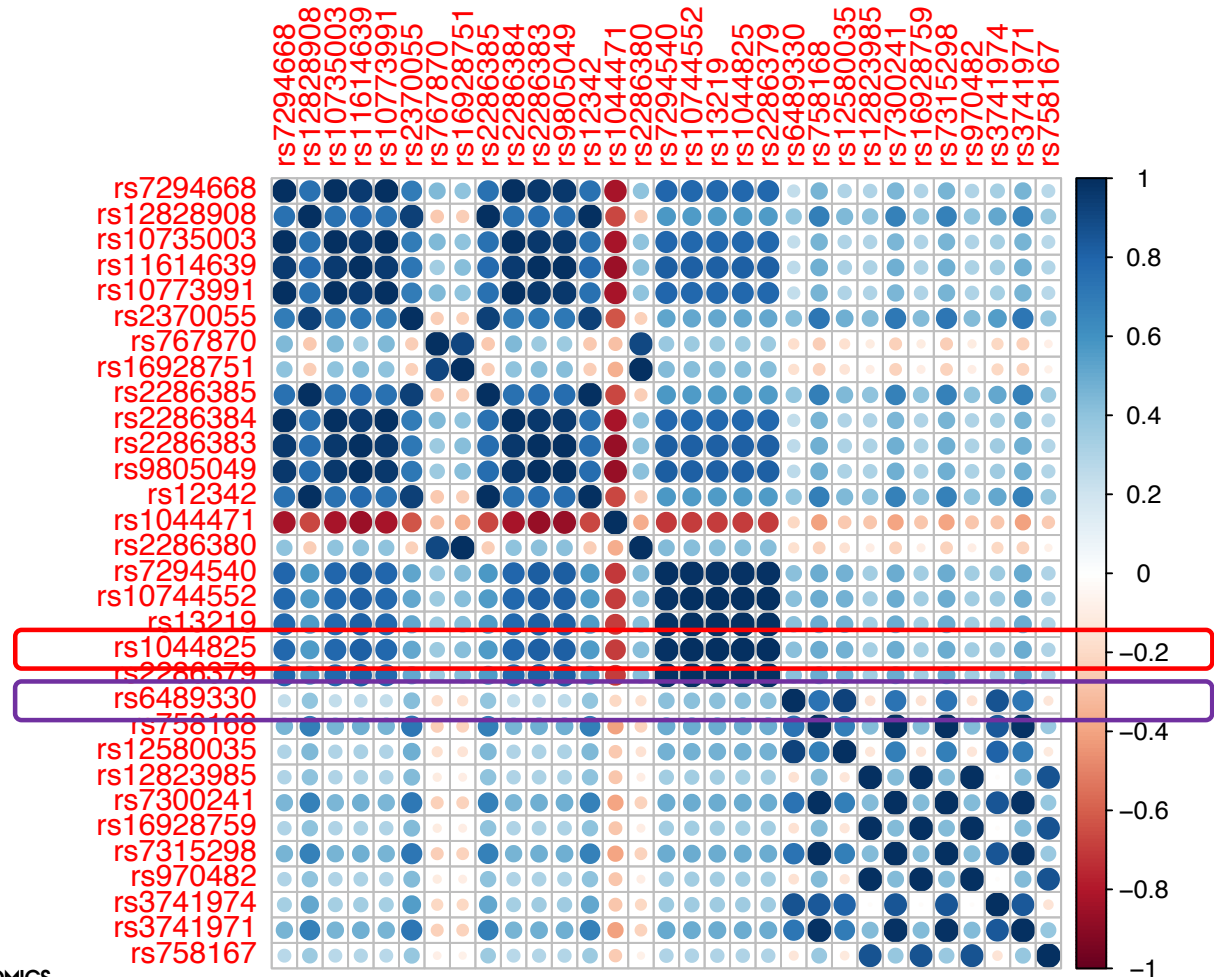
SNPs in LD

- $\hat{\beta}_{SNP} = \hat{\gamma}_{SNP} / \hat{\delta}_{SNP}$

Test

- $\hat{d}_{SNP} = \hat{\beta}_{SNP} - \hat{\beta}_{top}$
- $H_0: \hat{d}_{SNP(1)} = \hat{d}_{SNP(2)} = \dots = 0$
- $H_1: \text{Any } \hat{d}_{SNP(i)} \neq 0$
- Wald test for hypothesis testing

# Risk gene - *CACNA2D4*



The top-associated SNP  
The SNP to test difference

# Risk gene – *CACNA2D4*

| SNP              | A1 / A2 | Data                    | $b$     | SE      | $P$ -value |
|------------------|---------|-------------------------|---------|---------|------------|
| <b>rs1044825</b> | G / T   | eQTL<br>(blood)         | 0.447   | 0.0186  | 4.1E-128   |
|                  |         | GWAS<br>(schizophrenia) | -0.0377 | 0.0087  | 1.3E-5     |
| <b>rs6489330</b> | A / G   | eQTL<br>(blood)         | 0.211   | 0.02384 | 9.5E-19    |
|                  |         | GWAS<br>(schizophrenia) | -0.0378 | 0.0108  | 4.7E-4     |

$$\text{rs1044825, } \hat{\beta}_1 = -0.084, \text{SE}(\hat{\beta}_1) \approx 0.020$$

$$\text{rs6489330, } \hat{\beta}_2 = -0.179, \text{SE}(\hat{\beta}_2) \approx 0.055$$

$$\text{Difference, } \hat{d} = \hat{\beta}_2 - \hat{\beta}_1 = -0.179 + 0.084 = -0.095$$

$$\text{SE}(\hat{d}) = \sqrt{\text{var}(\hat{\beta}_2 - \hat{\beta}_1)} = \sqrt{\text{var}(\hat{\beta}_2) + \text{var}(\hat{\beta}_1) - 2 \times \text{cov}(\hat{\beta}_1, \hat{\beta}_2)} = 0.050$$



# Software

## - SMR

SMR | Yang Lab

GCTA | Yang Lab

yanglab.westlake.edu.cn/software/smr/#SMR&HEIDIanalysis

Funding NCRR\_Genetic Tools dbGap Imputation Datasets NCRR\_register

SMR Summary-data-based Mendelian Randomization

GCTA SMR GSMR OSCA

Bookmark added

Name SMR | Yang Lab

Folder Tutorial

More... Remove Done

SMR & HEIDI analysis

SMR

<https://yanglab.westlake.edu.cn/software/smr/#Overview>

# run SMR and HEIDI test

```
smr --bfile mydata --gwas-summary mygwas.ma --beqtl-summary myeqtl --out mysmr --thread-num 10
```

--bfile reads individual-level SNP genotype data (in PLINK binary format) from a reference sample for LD estimation, i.e. .bed, .bim, and .fam files.

--gwas-summary reads summary-level data from GWAS. The input format follows that for GCTA-COJO analysis (<http://cns.genomics.com/software/gcta/#COJO>).

```
smr --bld mybld --gwas-summary mygwas.ma --beqtl-summary myeqtl --out mysmr --thread-num 10
```

### Command line:

```
smr --bfile mydata --gwas-summary mygwas.ma --beqtl-summary myeqtl \ --out mysmr
```

--bld reads LD information from a binary file in BLD format

# SMR - Resources



yanglab.westlake.edu.cn/software/smr/#DataResource

Funding NCRR\_Genetic Tools dbGap Imputation Datasets NCRR\_register Conference Uni Visa Other Bookmarks

## SMR

Summary-data-based Mendelian Randomization

GCTA **SMR** GSMR OSCA CTG forum Yang Lab

### Overview

[SMR & HEIDI analysis](#)

[Data Management](#)

[SMR locus plot](#)

[Query eQTL Results](#)

[MeCS](#)

[Options Reference](#)

[Download](#)

### Data Resource

[sQTL summary data](#)

[eQTL summary data](#)

[mQTL summary data](#)

[caQTL summary data](#)

## Data Resource

### sQTL summary data

#### # BrainMeta v2 sQTL summary data (n = 2,865)

We developed a method, THISTLE, which uses individual-level genotype and RNA-seq data or summary-level isoform-eQTL data for splicing QTL (sQTL) mapping (Qi et al. 2022). We applied THISTLE, in combination with a complementary sQTL mapping strategy, for sQTL mapping using RNA-seq data of 2,865 brain cortex samples from 2,443 unrelated individuals of European ancestry with genome-wide SNP data. See below for the link to download the full summary statistics of the sQTLs in SMR binary (BESD) format. You can also query or visualize the sQTL summary statistics using the [BrainMeta portal](#).

**BrainMeta v2 cis-sQTL summary data** (Qi et al. 2022) in SMR binary (BESD) format:

[BrainMeta\\_cis\\_sqtl\\_summary.tar.gz](#) (hg19) (9.0 GB)

These are pooled cis-sQTLs identified by THISTLE and LeafCutter & QTLtools. Only SNPs within 2 Mb distance from

sQTL – Summary statistics of splicing QTLs

eQTL – Summary statistics from associations of gene expression

mQTL – Summary statistics from associations of methylation



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# Misuse of MR

- Assuming that study is performed in a population
  - Time-frame (youths vs adults)
  - Sex (males vs females)
  - Environment (e.g. low altitude vs high altitude)
- Tissue
  - Blood – the largest sample size, shared effects with other tissues
  - Mental disorders - brain
  - BMI – adipose
  - ...

# Summary

- Regression – bias due to environmental confounding factor
- Mendelian randomisation - similar concept to randomised controlled trial
  - RCT is the gold-standard approach
  - using genetic variant (e.g. SNP) as instrument
  - instrument should be strongly associated with exposure
  - 2SLS – individual-level data
  - Summary-data-based method – summary-level data
- Genetic architecture
  - Large genetic variation at a single SNP, large LD blocks  
*CACNA2D4* -> schizophrenia
- SMR method
  - SMR – using a single SNP instrument
  - HEIDI – distinguishing linkage model from pleiotropy model
  - Misuse of SMR

# Data agreement

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Access to this data requires agreement to the following in to comply with human genetic data ethics regulations.

Please send an email to [pctgadmin@imb.uq.edu.au](mailto:pctgadmin@imb.uq.edu.au) with your name and the below statement to confirm that you agree with the following:

**"I agree that access to data is provided for educational purposes only and that I will not make any copy of the data outside the provided computing account. "**

# Practical

- 
- Software
    - SMR V1.3.1
  - Data
    - eQTL dataset - the Westra eQTL data, Westra et al. 2013 Nature Genetics
    - GWAS dataset – GWAS of schizophrenia, Trubetskoy et al. 2022 Nature
    - LD reference cohort

# eQTL dataset

- SMR format
  - .besd - summary statistics of eQTL dataset
  - .epi - probes

|       |              |   |         |          |   |
|-------|--------------|---|---------|----------|---|
| 1     | ILMN_1653466 | 0 | 934380  | HES4     | - |
| 1     | ILMN_2349633 | 0 | 1140818 | TNFRSF18 | - |
| 1     | ILMN_2112256 | 0 | 1146750 | TNFRSF4  | - |
| ..... |              |   |         |          |   |

- .esi - SNPs

|       |           |   |        |   |   |
|-------|-----------|---|--------|---|---|
| 1     | rs3131968 | 0 | 754192 | A | G |
| 1     | rs2905035 | 0 | 775659 | A | G |
| 1     | rs2980319 | 0 | 777122 | A | T |
| ..... |           |   |        |   |   |

# GWAS dataset

- COJO format

| SNP        | A1 | A2 | FREQ  | BETA                 | SE     | P      | N        |
|------------|----|----|-------|----------------------|--------|--------|----------|
| rs62513865 | C  | T  | 0.927 | 0.0119977384336167   | 0.0171 | 0.4847 | 58749.13 |
| rs79643588 | G  | A  | 0.906 | -0.00859684722551828 | 0.0148 | 0.5605 | 58749.13 |
| rs17396518 | T  | G  | 0.566 | -0.0021022080918702  | 0.0087 | 0.8145 | 58749.13 |
| ...        |    |    |       |                      |        |        |          |

# Command

- LD reference cohort (PLINK format)
- Command  
*CACNA2D4* -> schizophrenia  
smr \  
    --bfile ld\_reference \  
    --gwas-summary sz\_2022.ma \  
    --beqtl-summary westra \  
    --out smr\_westra\_sz

# Thank you!

Zhihong Zhu, Ph.D

[z.zhu@econ.au.dk](mailto:z.zhu@econ.au.dk) | [z.zhu1@uq.edu.au](mailto:z.zhu1@uq.edu.au)



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