

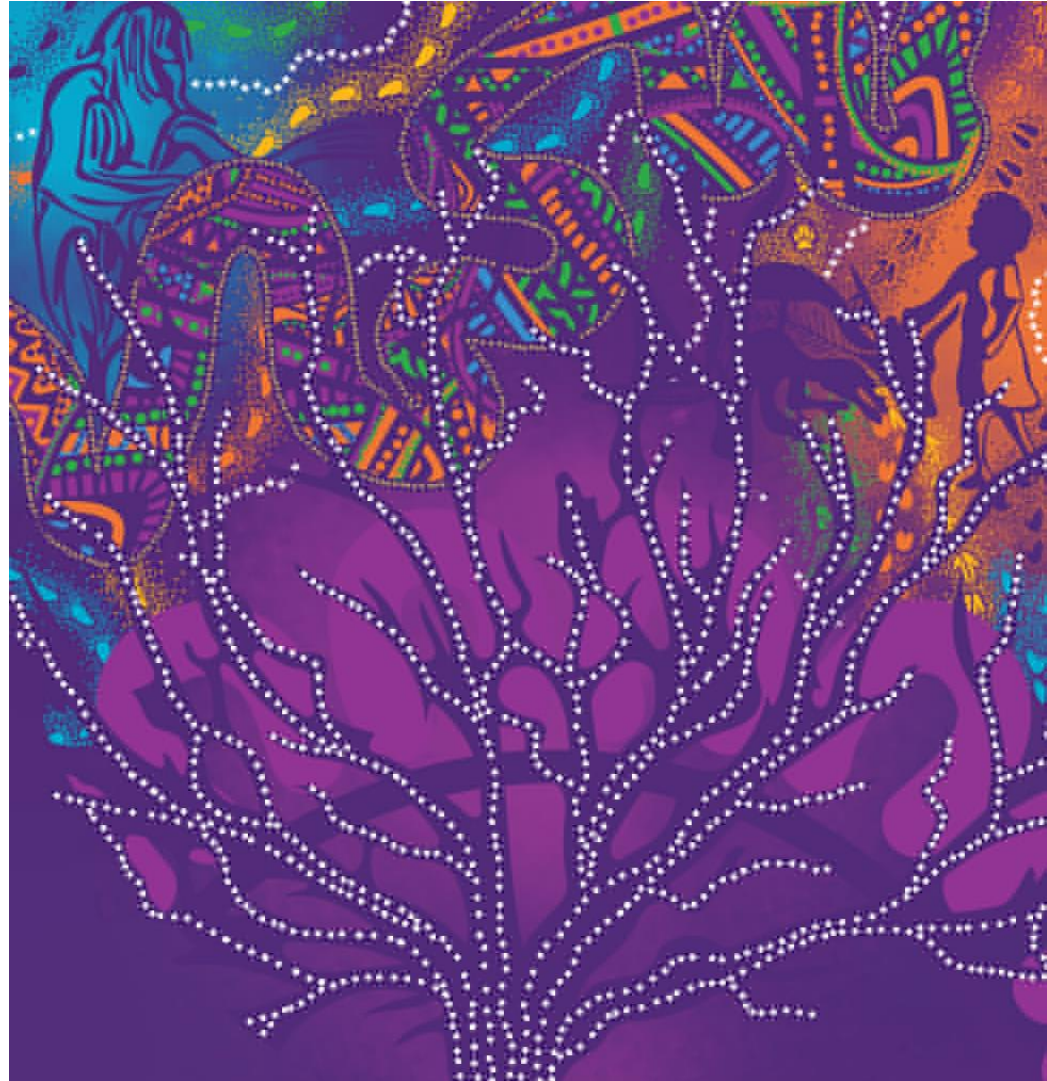
# Acknowledgement of Country

The University of Queensland (UQ) acknowledges the Traditional Owners and their custodianship of the lands on which we meet.

We pay our respects to their Ancestors and their descendants, who continue cultural and spiritual connections to Country.

We recognise their valuable contributions to Australian and global society.

Image: Digital reproduction of *A guidance through time* by Casey Coolwell and Kyra Mancktelow



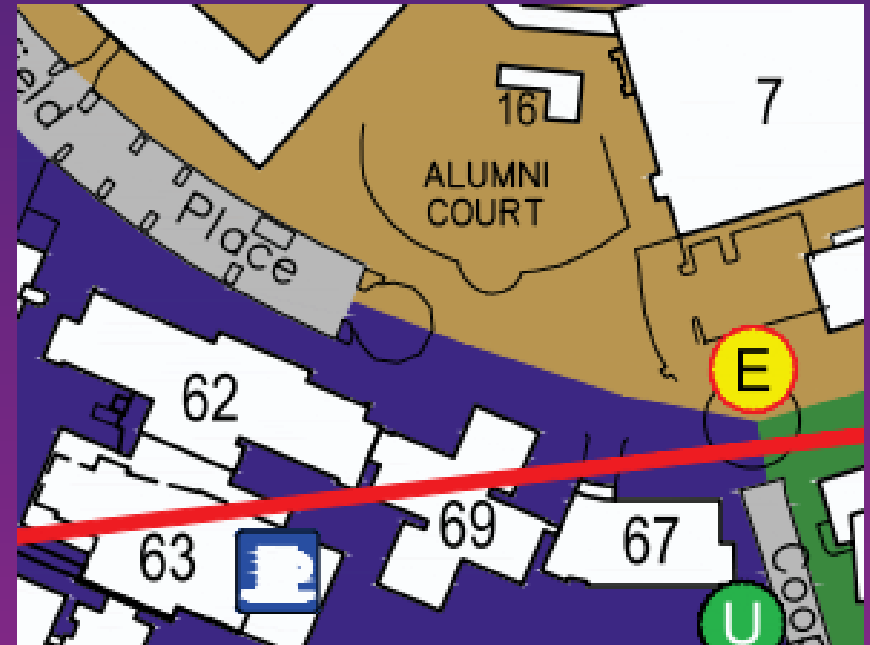
# General Information:

- We are currently located in Building 69



Emergency evacuation point

- Food court and bathrooms are located in Building 63
- If you are experiencing cold/flu symptoms or have had COVID in the last 7 days please ensure you are wearing a mask for the duration of the module



# Data Agreement

To maximize your learning experience, we will be working with genuine human genetic data, during this module.

Access to this data requires agreement to the following in to comply with human genetic data ethics regulations

Please email [pctgadmin@imb.com.au](mailto:pctgadmin@imb.com.au) with your name and the below statement to confirm that you agree with the following:

“I agree that access to data is provided for educational purposes only and that I will not make any copy of the data outside the provided computing accounts.”

## Day 1 (June 21<sup>st</sup> Tuesday): Mendelian randomization

9:00-10:30am	<b>Lecture 1: Introduction to Mendelian randomization.</b> We will introduce the concept of Mendelian randomization, the assumptions underlying the approach, and empirical examples involving application of the method.	David Evans
10:30-11:00am	Break	
11:00-12:30pm	<i>Practical 1:</i> Single sample Mendelian randomization. Software: R.	Daniel Hwang John Kemp Gunn-Helen Moen Nicole Warrington
12:30-1:30pm	<b>Lunch break</b>	
1:30pm-3:00pm	<b>Lecture 2: Sensitivity Analyses in Mendelian randomization.</b> We will introduce methods for detecting and/or correcting for horizontal pleiotropy in Mendelian randomization analyses including heterogeneity testing, MR Egger, MR weighted median and MR modal approaches.	David Evans
3:00-3:30pm	Break	
3:30-4:30pm	<i>Practical 2:</i> Two sample Mendelian randomization. Software: R, MR Base.	Daniel Hwang John Kemp Gunn-Helen Moen Nicole Warrington
4:30-5pm	<b>Questions and Discussion</b>	

## Day 2 (June 22<sup>nd</sup> Wednesday): Structural Equation Modelling

9-10:30am	<b>Lecture 3: Introduction to Structural Equation Modelling.</b> We will introduce the technique of structural equation modelling. Concepts that will be covered include full information maximum likelihood (FIML), optimization, path analysis and covariance algebra. We will discuss examples of structural equation modelling for genetically informative data.	David Evans
10:30-11:00am	Break	
11:00-12:30pm	<i>Practical 3:</i> Path Tracing Rules, Covariance Algebra, Likelihood	Daniel Hwang John Kemp Gunn-Helen Moen Nicole Warrington
12:30-1:30pm	<b>Lunch break</b>	
1:30pm-3:00pm	<b>Lecture 4: Structural Equation Modelling (continued) and Genomic SEM.</b> We introduce Genomic SEM, an exciting new method to analyse summary results statistics from GWAS.	David Evans
3:00-3:30pm	Break	
3:30-4:30pm	<b>Lecture 5: Directed Acyclic Graphs (DAGs).</b> We will introduce Directed Acyclic Graphs and illustrate how they can be used to inform study design, analysis of data and understand the implications of confounding, bias and missing data.	David Evans
4:30-5:00pm	<b>Questions and Discussion</b>	All speakers

# Introduction to Mendelian Randomization

David Evans<sup>1,2,3</sup>

1 Institute for Molecular Bioscience, University of Queensland

2 University of Queensland Diamantina Institute

3 MRC Integrative Epidemiology Unit, University of Bristol

# This Session

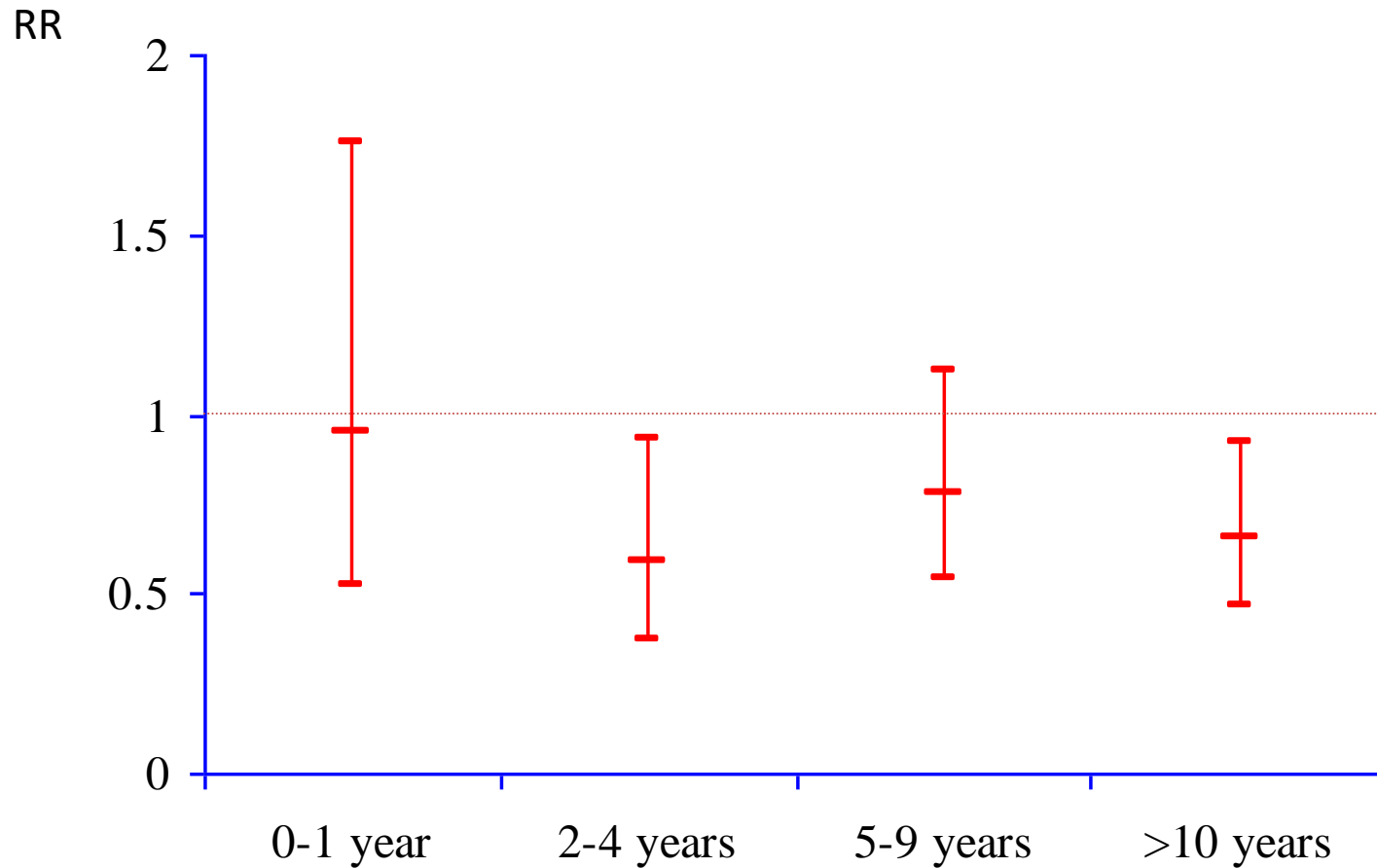
- Problems with observational data
- Randomized controlled trials
- Mendelian Randomization (MR):
  - How it works
  - Core assumptions
  - Calculating causal effect estimates
- MR example
- Limitations of MR

# The Problem with Inferring Causality in Observational Studies



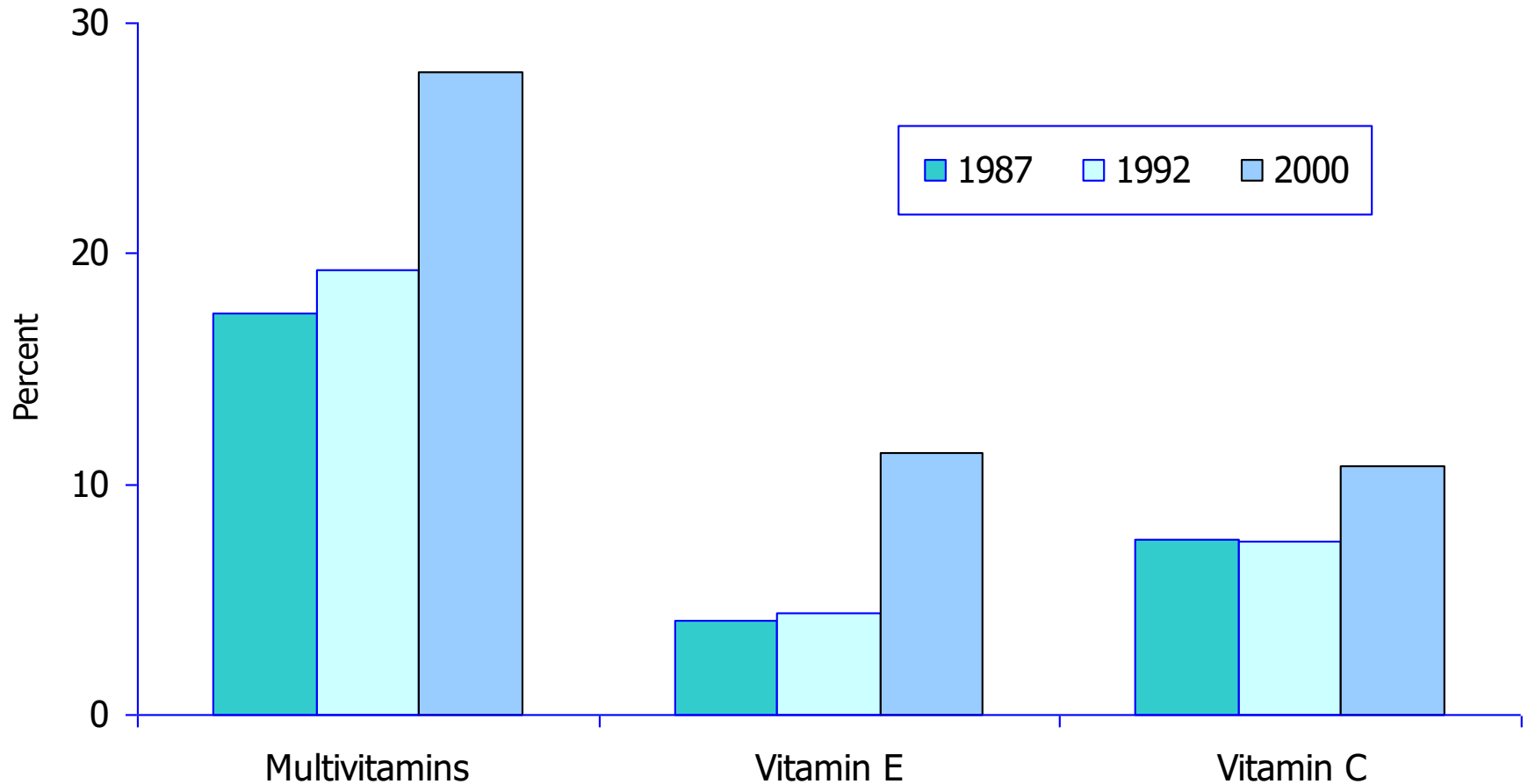


# CHD risk according to duration of current Vitamin E supplement use compared to no use

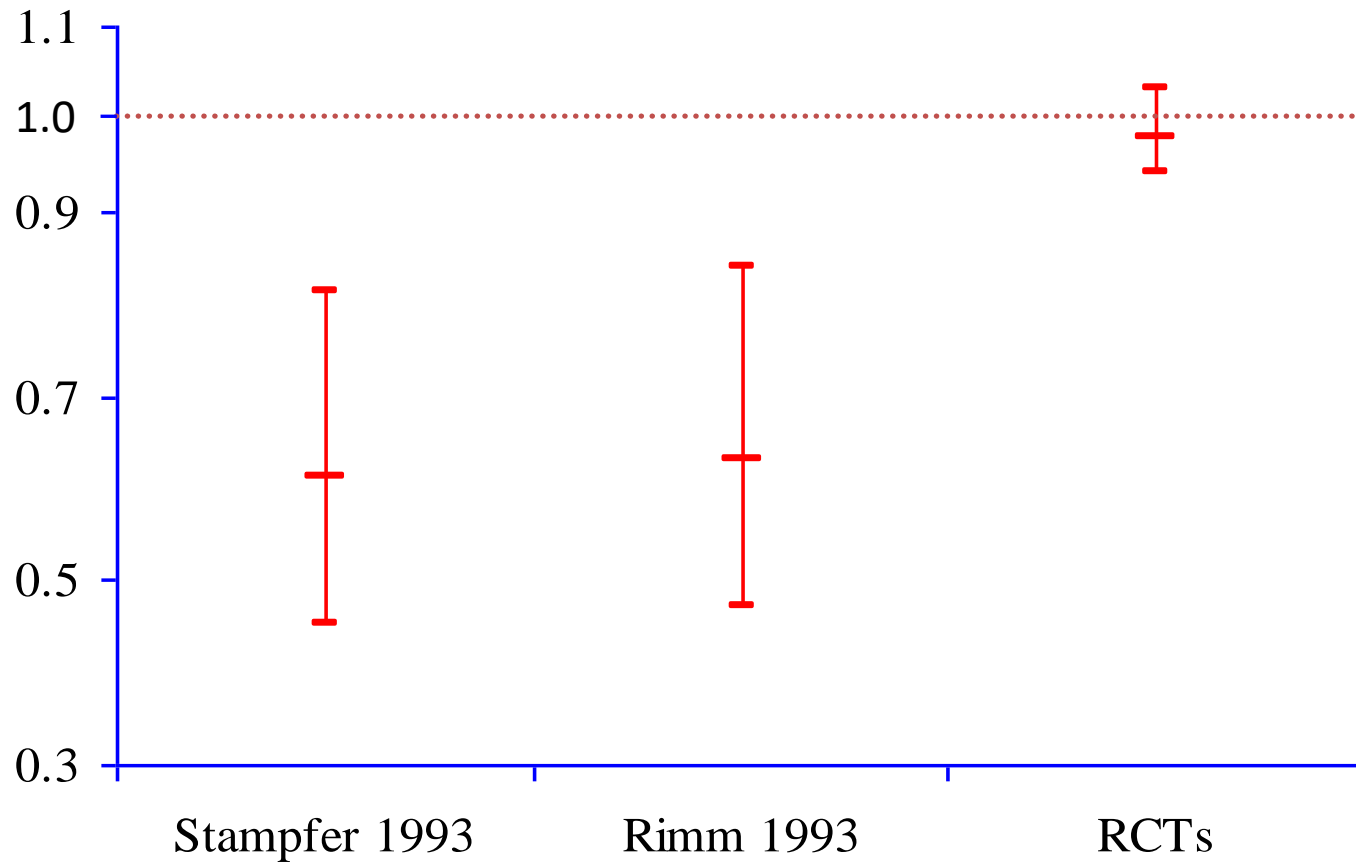


Rimm et al NEJM 1993; 328: 1450-6

# Use of vitamin supplements by US adults, 1987-2000



# Vitamin E supplement use and risk of Coronary Heart Disease



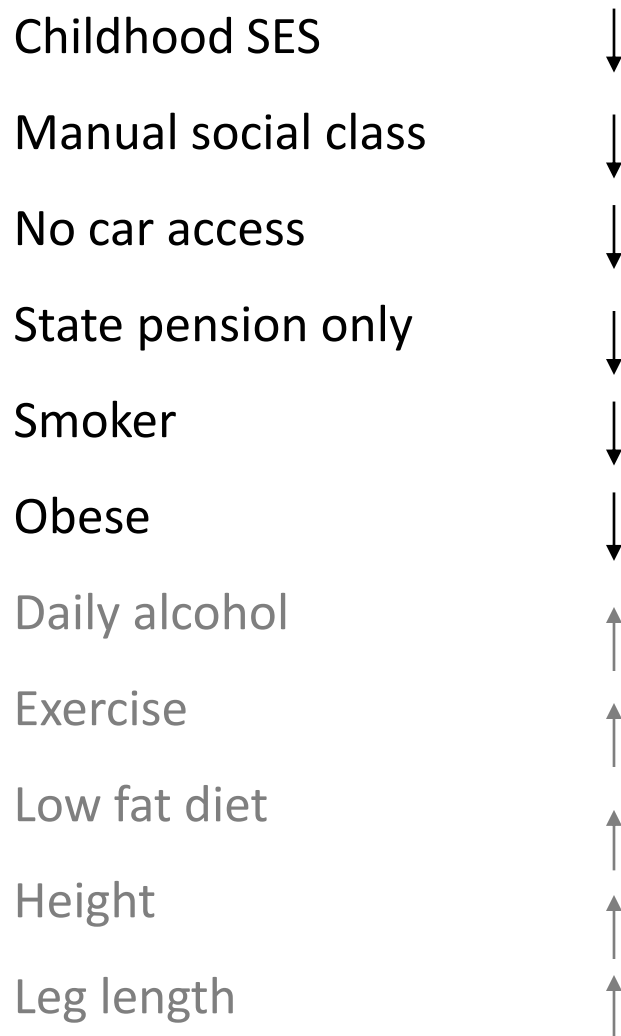
Stampfer et al NEJM 1993; 328: 144-9; Rimm et al NEJM 1993; 328: 1450-6; Eidelman et al Arch Intern Med 2004; 164:1552-6

# **MANY OTHER EXAMPLES**

**VITAMIN C, VITAMIN A, HRT,  
MANY DRUG TARGETS.....**

# **WHAT'S THE EXPLANATION?**

# Vitamin E levels and confounding risk factors:

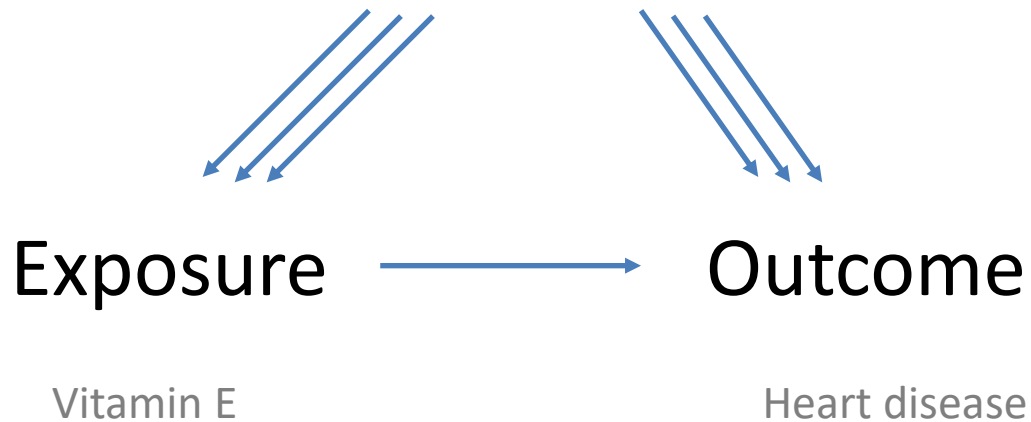


Women's Heart and Health Study  
Lawlor et al, Lancet 2004

# Confounding

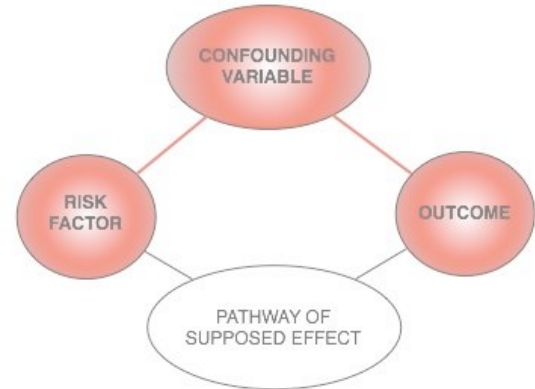
Smoking, diet, alcohol, socioeconomic position....

## Confounders



# Classic limitations to “observational” science

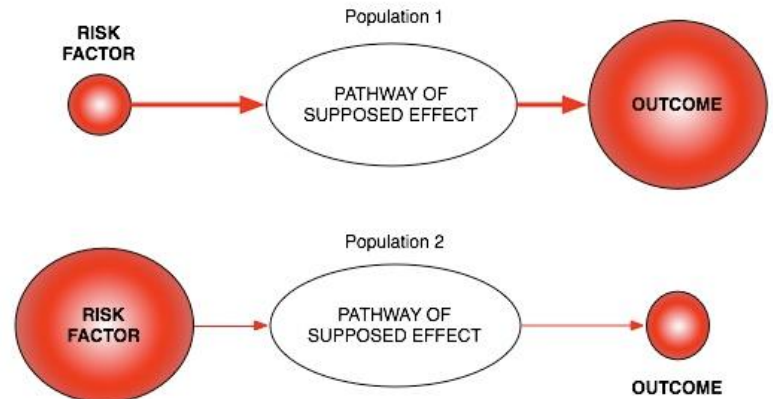
- **Confounding**



- **Reverse Causation**

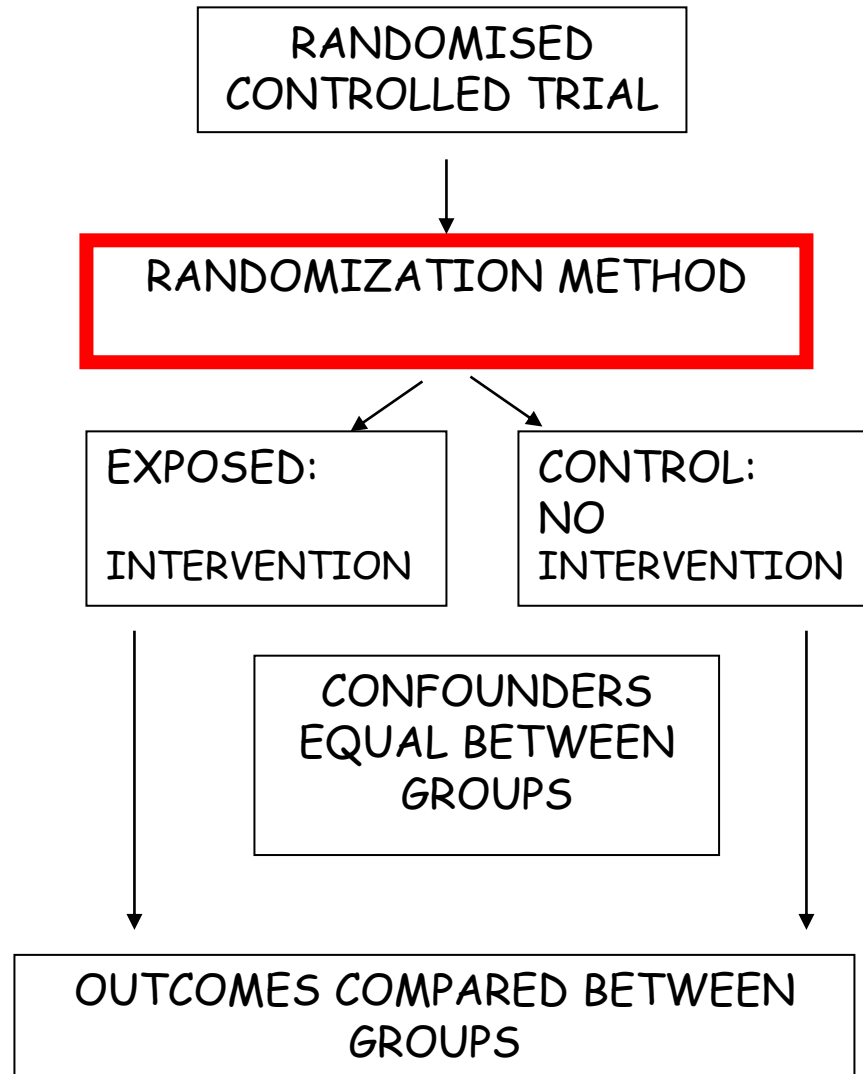


- **Bias**



# RCTs: the Gold Standard in Inferring Causality

Randomization  
makes causal inference  
possible





# The Need for Observational Studies

- **Randomized Controlled Trials (RCTs):**
  - Not always ethical or practically feasible eg anything toxic
  - Expensive, requires experimentation in humans
  - Impractical for long follow up times
  - Should only be conducted on interventions that show very strong observational evidence in humans
- **Observational studies:**
  - Association between environmental exposures and disease measured in observational designs (non-experimental)  
eg case-control studies or cohort studies
  - Reliably assigning causality in these types of studies is *very limited*

# Mendelian randomization



How can it help  
observational epidemiology?

# What does MR do?

- **Assess causal relationship between two variables**
- Estimate magnitude of causal effect

How does it do this?

By harnessing Mendel's laws of inheritance

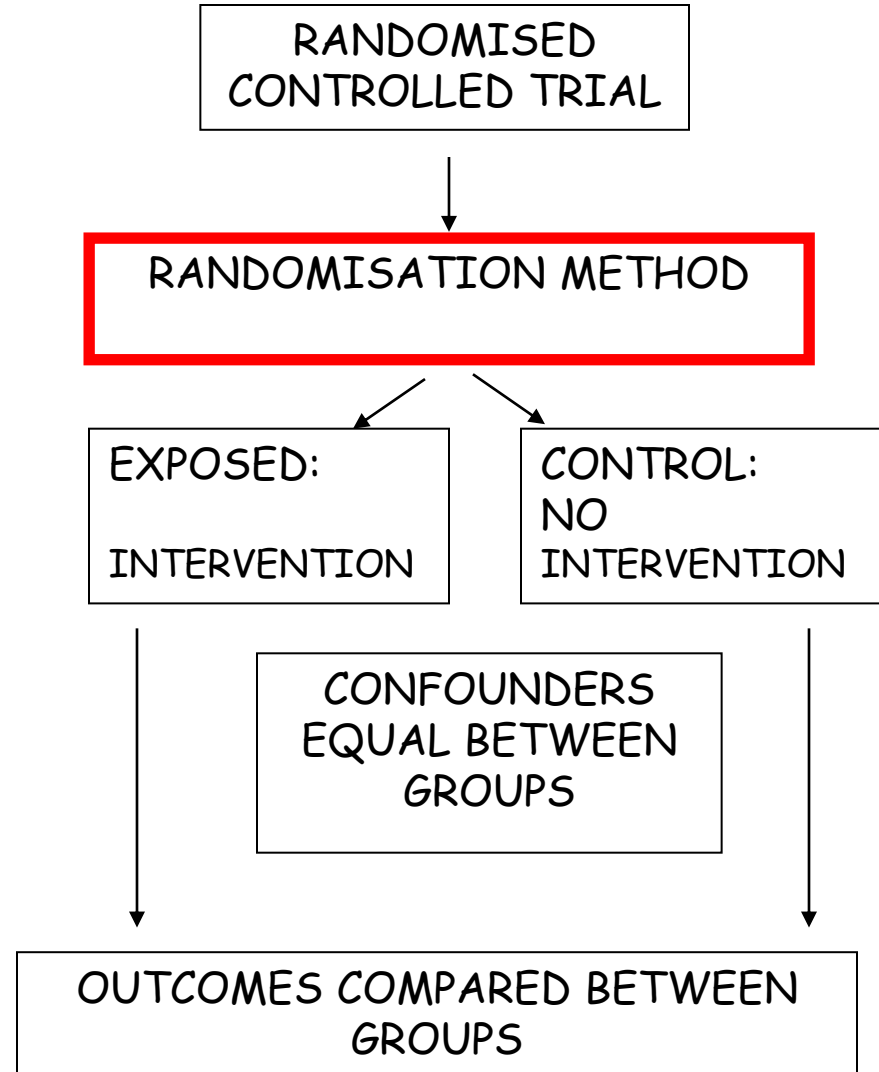
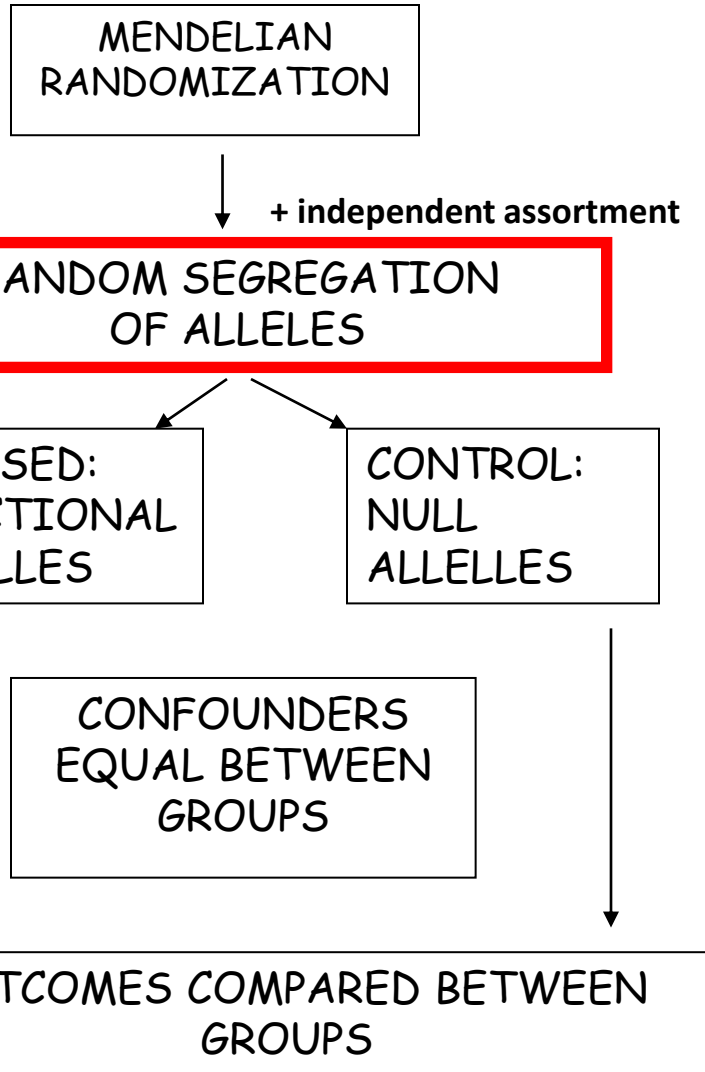
# Mendel's Laws of Inheritance



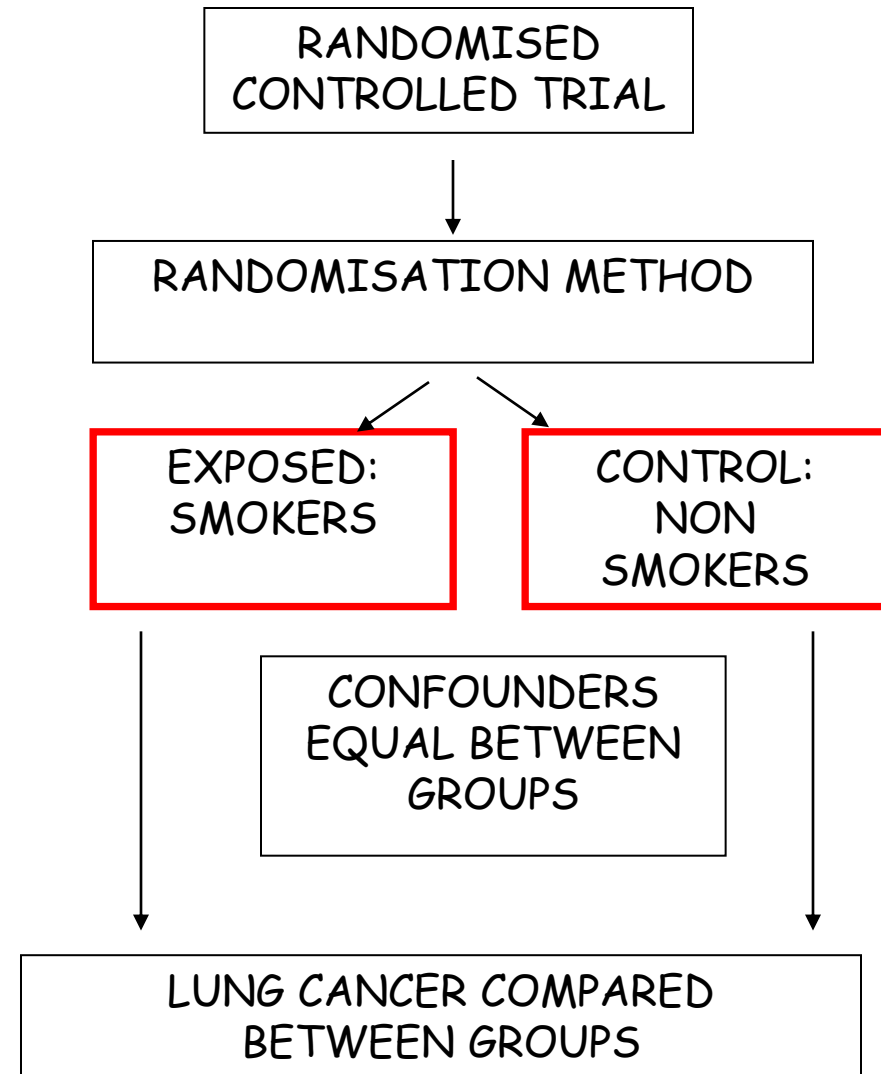
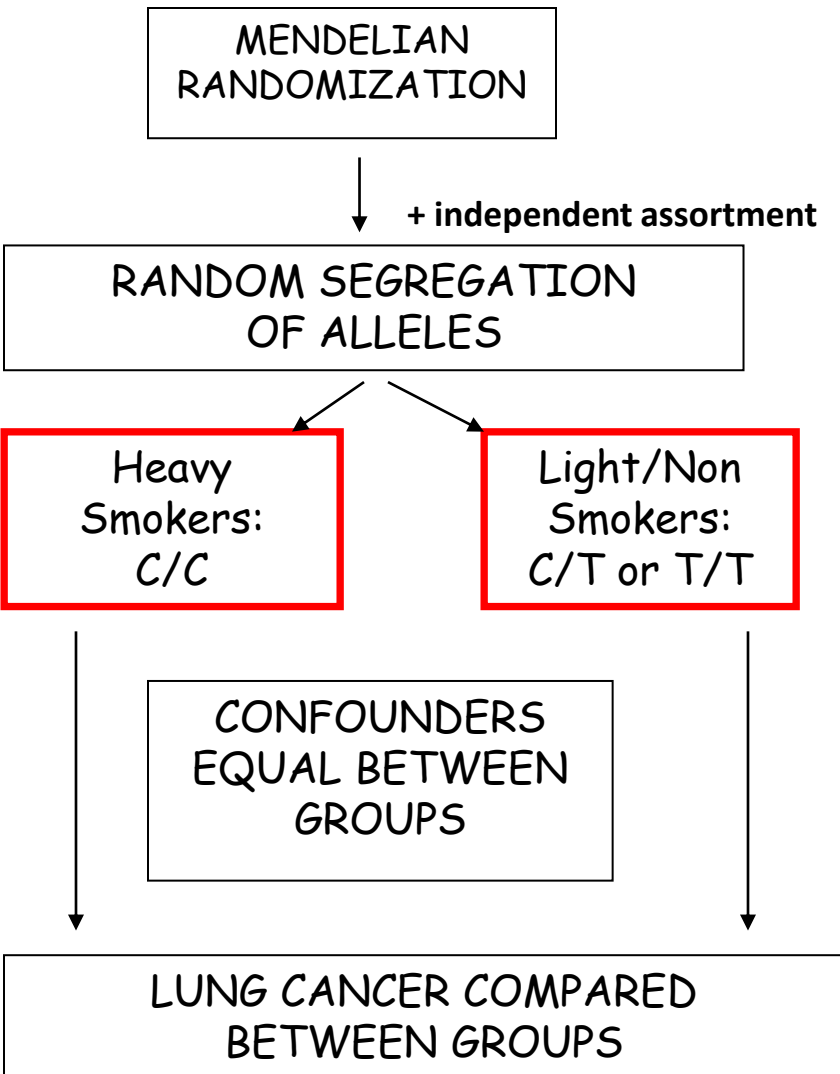
Mendel in 1862

- 1. Segregation:** alleles separate at meiosis and a randomly selected allele is transmitted to offspring
- 2. Independent assortment:** alleles for separate traits are transmitted independently of one another

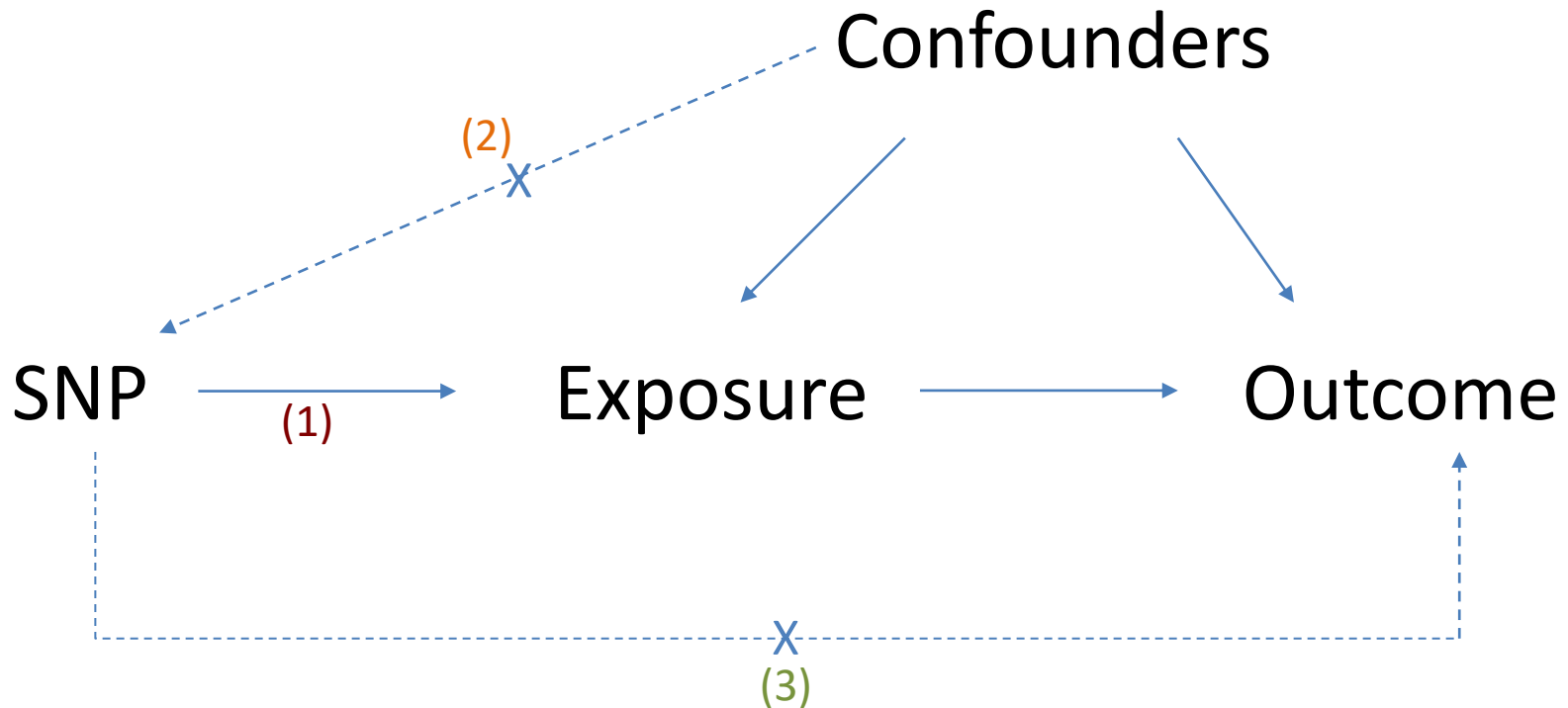
# Mendelian randomization and RCTs



# Mendelian randomization: Smoking and Lung Cancer



# Mendelian Randomization: 3 Core Assumptions



(1) SNP is associated with the exposure

(2) SNP is NOT associated with confounding variables

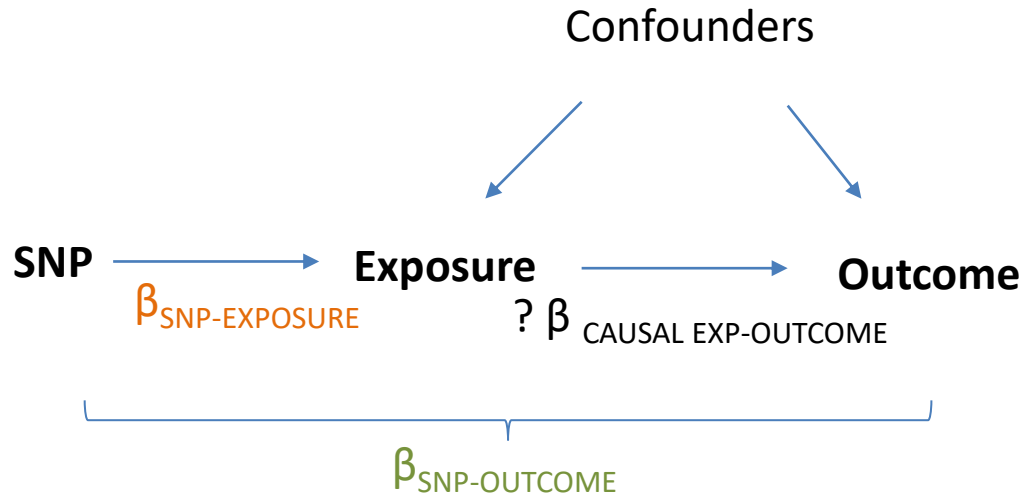
(3) SNP ONLY associated with outcome through the exposure

# Why are genetic associations special?

- Robustness to confounding due to Mendel's laws:
  - Law of segregation: inheritance of an allele is random and independent of environment etc
  - Law of independent assortment: genes for different traits segregate independently (assuming not in LD)
- The direction of causality is known – always from SNP to trait
- Genetic variants are **potentially** very good instrumental variables
- Using genetic variants as IVs is a special case of IV analysis, known as Mendelian randomization



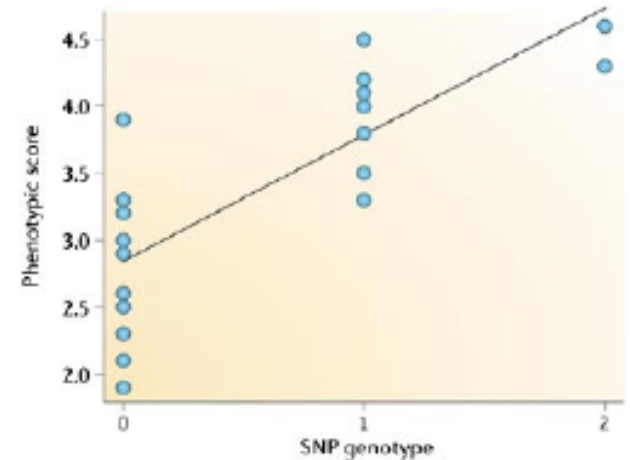
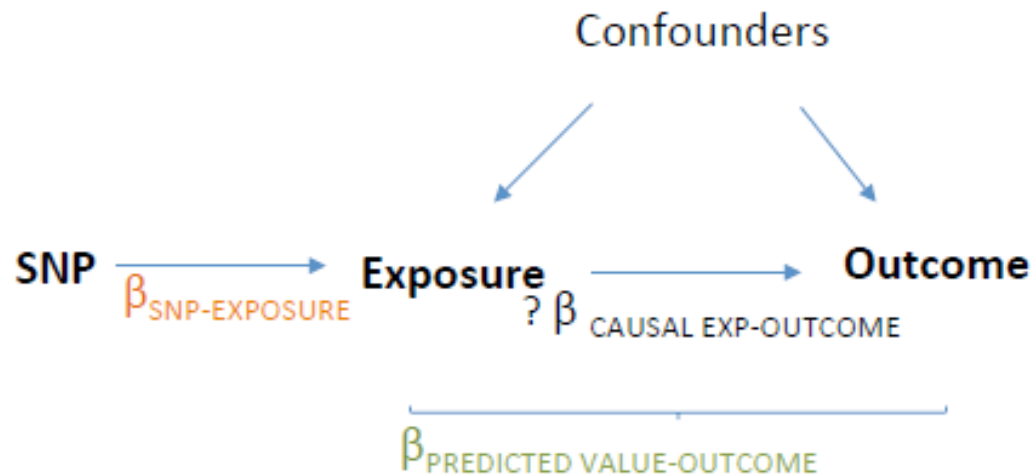
# Calculating Causal Effect Estimates



After SNP identified robustly associated with exposure of interest:

- Wald Estimator
- Two-stage least-squares (TSLS) regression

# Calculating Causal Effect Estimates



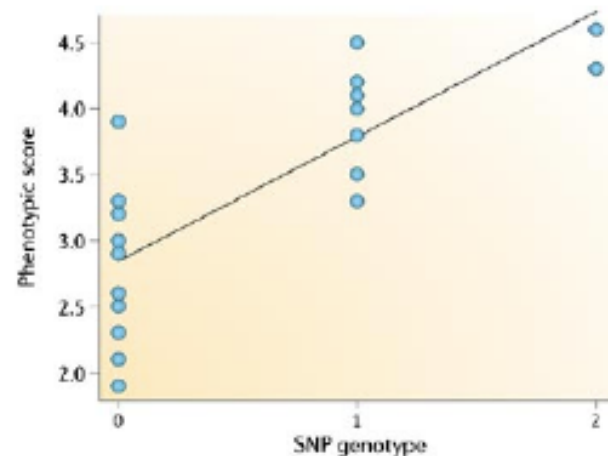
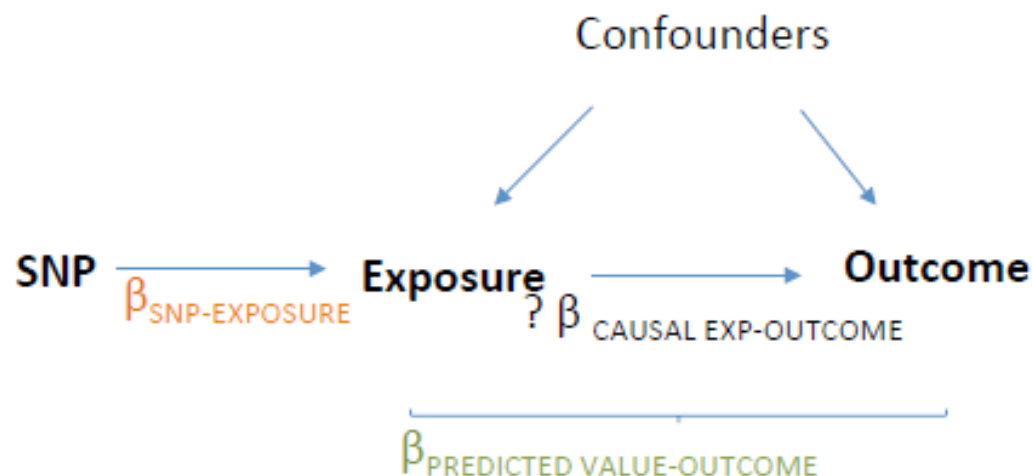
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Nature Reviews | Genetics

## Two-stage Least Squares (2SLS):

- (1) Regress exposure on SNP & obtain predicted values
- (2) Regress outcome on **predicted** exposure (from 1<sup>st</sup> stage regression)
- (3) Adjust standard errors

\*Needs to be done in the one sample ("Single sample MR")

# Calculating Causal Effect Estimates



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## Two-stage Least Squares (2SLS):

- (1) Regress exposure on SNP & obtain predicted values
- (2) Regress outcome on **predicted** exposure (from 1<sup>st</sup> stage regression)
- (3) Adjust standard errors

This gives you: difference in outcome per unit change in (genetically-predicted) exposure

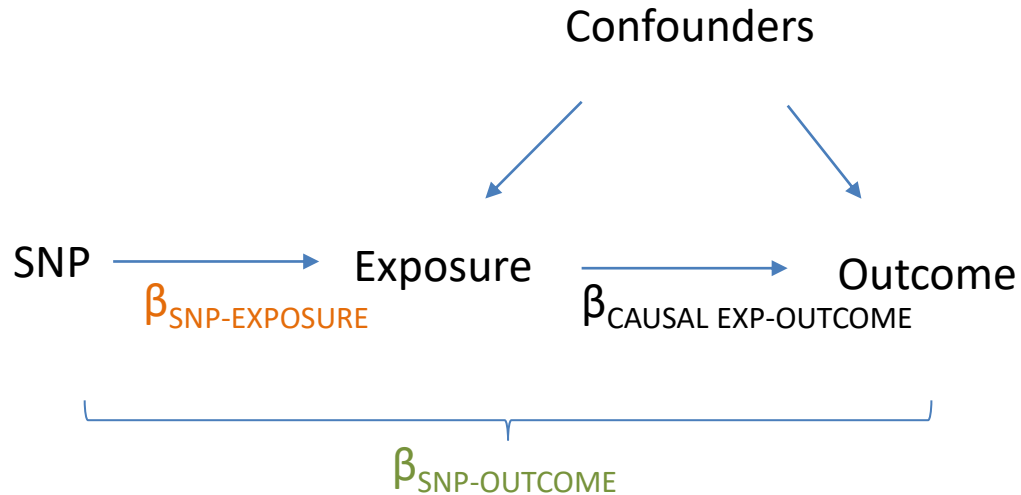
Genetically determined exposure → “randomized” → can ascribe causality  
(if assumptions are met)

\*Needs to be done in the one sample (“Single sample MR”)

# MR can also be performed using just the results from GWAS

- Also known as two-sample MR, SMR, or MR with summary data etc
- Advantages:
  - The data is readily available, non-disclosive, free, open source
  - The exposure and outcome might not be measured in the same sample
  - The sample size of the outcome variable, key to statistical power, is not limited by requiring overlapping measures of the exposure
- Disadvantages:
  - Some extensions of MR not possible, e.g. non-linear MR, use of GxE for negative controls, various sensitivity analyses

# Calculating Causal Effect Estimates



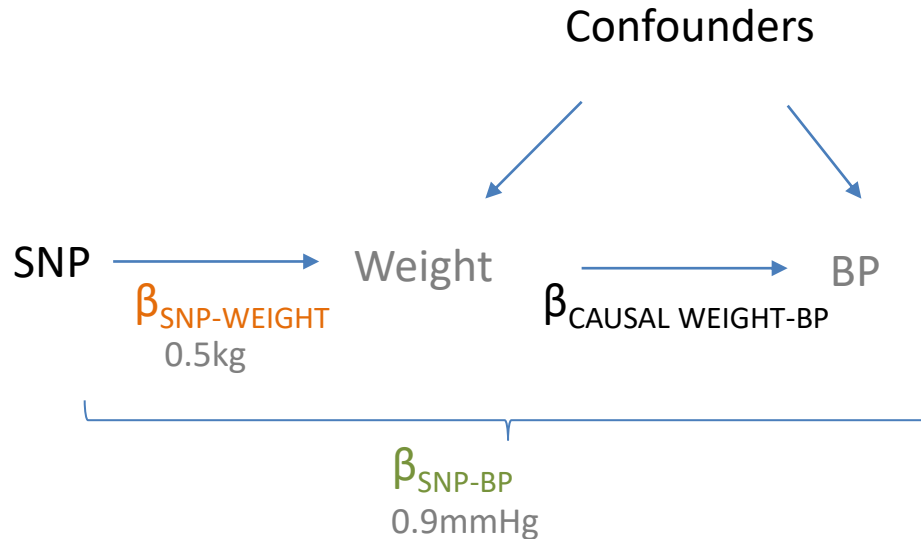
Causal effect by  
Wald Estimator\* :

$$\frac{\hat{\beta}_{\text{SNP-OUTCOME}}}{\hat{\beta}_{\text{SNP-EXPOSURE}}}$$

$$\beta_{\text{SNP-OUTCOME}} = \beta_{\text{CAUSAL EXP-OUTCOME}} \times \beta_{\text{SNP-EXPOSURE}}$$

\*Can be used in different samples ("Two sample MR")

# Calculating Causal Effect Estimates



**Causal effect by Wald Estimator\* :**

$$\frac{\hat{\beta}_{\text{SNP-OUTCOME}}}{\hat{\beta}_{\text{SNP-EXPOSURE}}}$$

= change in outcome per unit change in exposure

BP and weight:

$$\frac{0.9 \text{ mmHg/allele}}{0.5 \text{ kg/allele}}$$

$$= 1.8 \text{ mmHg/kg}$$

\*Can be used in different samples (“Two sample MR”)

# Generate causal estimate

## Two-stage least squares

```
library(sem)
```

```
mod1 <- tsls(outcome ~ exposure, ~ allele.score, data=data)
```

```
  # two-stage least squares with allele score
```

```
mod2 <- tsls(outcome ~ exposure, ~ rs123 + rs456 + rs789 + rs1011 + rs1213, data=data)
```

```
  # two-stage least squares with individual SNPs
```

```
library(AER)
```

```
mod3 <- ivreg(outcome ~ exposure | allele.score, data=data)
```

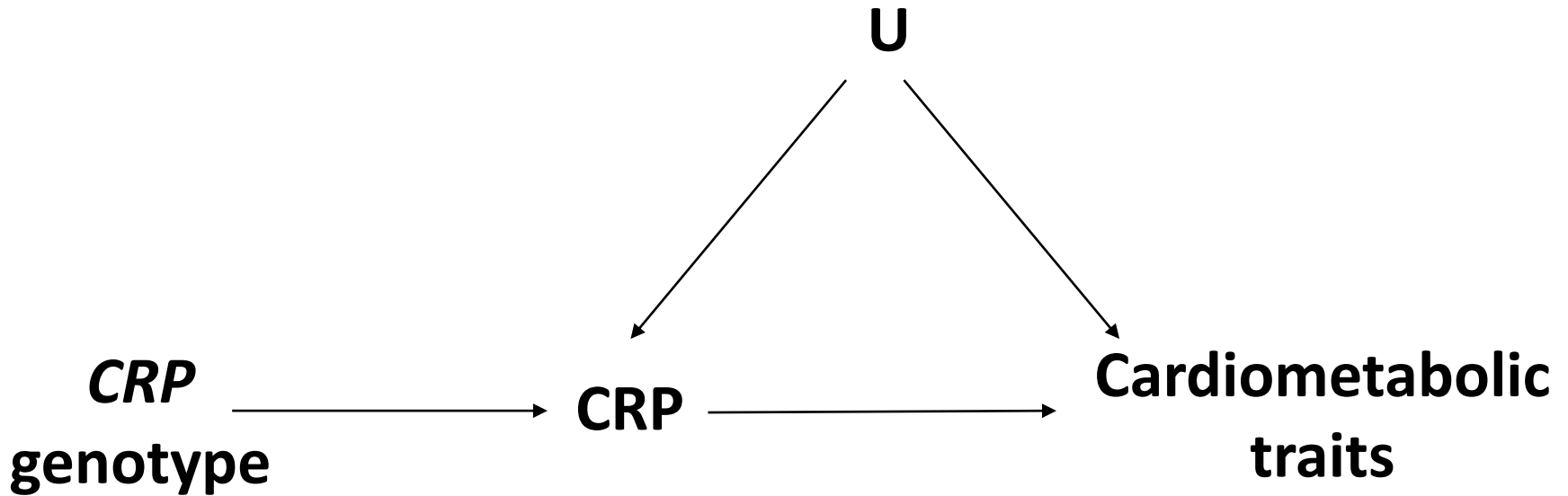
```
mod4 <- ivreg(outcome ~ exposure | rs123 + rs456 + rs789 + rs1011 + rs1213, data=data)
```

# MR Example using CRP

- C-Reactive Protein (CRP) is a biomarker of inflammation
- It is associated with BMI, metabolic syndrome, CHD and a number of other diseases
- It is unclear whether these observational relationships are causal or due to confounding or reverse causality
- This question is important from the perspective of intervention and drug development



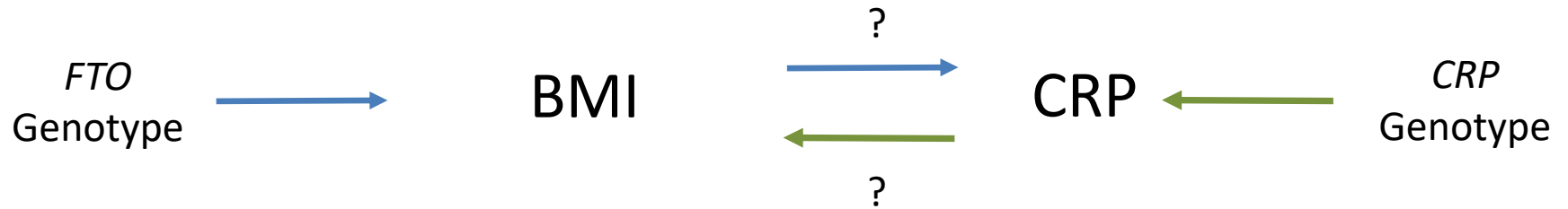
# Using a genetic instrument for proinflammatory CRP



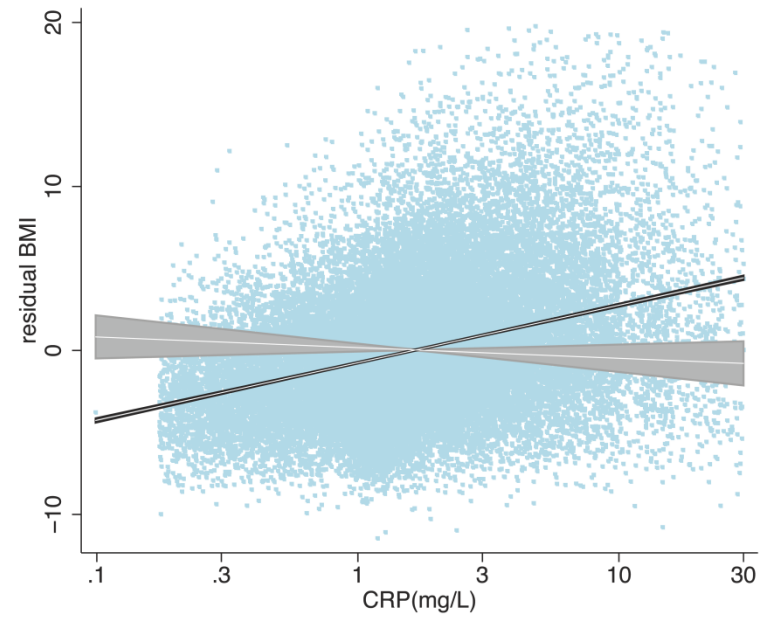
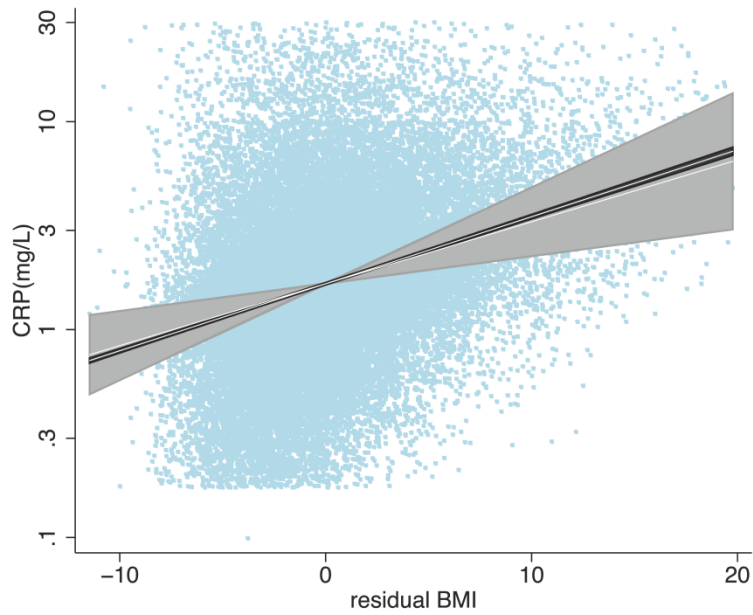
## TWO ALTERNATIVES

1. If CRP DOES NOT causally affect cardiometabolic traits:  
*CRP* gene variant should NOT be related to cardiometabolic traits
2. If CRP CAUSALLY affects metabolic traits:  
*CRP* gene variant should also be related to these metabolic traits

# “Bi-directional Mendelian Randomization”: Testing causality and reverse causation



	Effect estimates				
Outcome / explanatory variable	Observational	Instrumental variable	$P_{IV}$	$P_{diff}$	$F_{first}$
CRP/BMI	1.075 (1.073, 1.077)	1.06 (1.02, 1.11)	0.002	0.6	50.2



# Limitations to Mendelian Randomization

1- Population stratification

2- Canalisation (“Developmental compensation”)

3- The existence of instruments

**4- Power and “weak instrument bias”**

5- Pleiotropy

# Power and Weak Instruments

- Power:
  - Genetic variants explain very small amounts of phenotypic variance in a given trait
  - VERY large sample sizes are generally required
- Weak instruments:
  - Genetic variants that are weak proxies for the exposure
  - Results in biased causal estimates from MR
- Different impact of the bias from weak instruments:
  - **Single Sample MR:** to the confounded estimate
  - **Two-Sample MR:** to the null

# Using Multiple Genetic Variants as Instruments

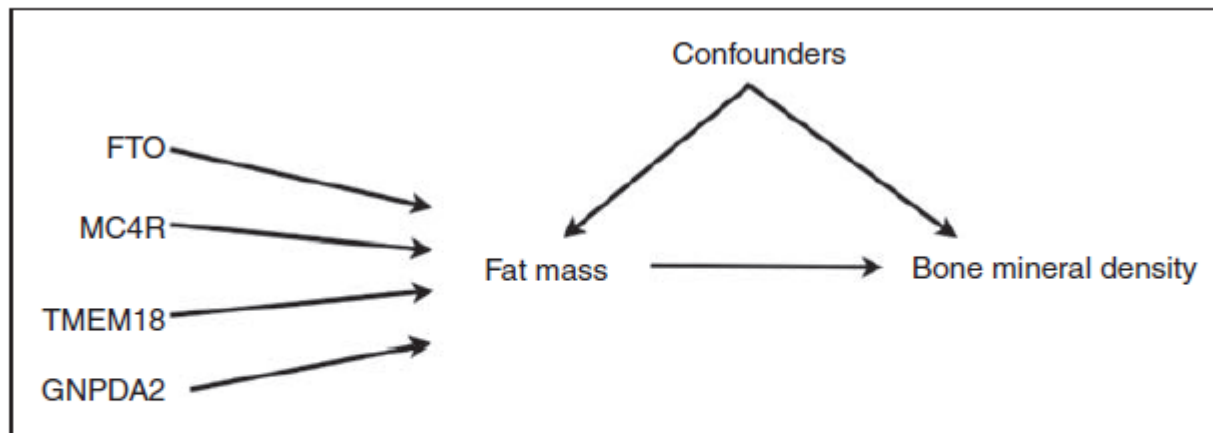
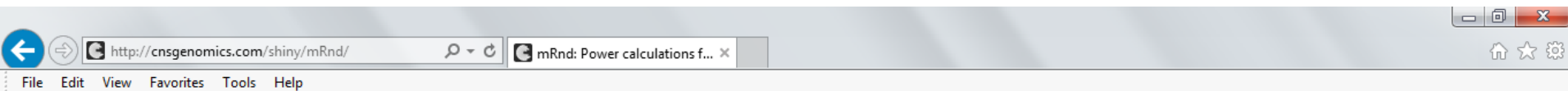


Figure 1. DAG for a Mendelian randomisation analysis using four genetic variants as instrumental variables for the effect of fat mass on bone mineral density.

*Palmer et al (2011) Stat Method Res*

- Allelic scores
- Testing multiple variants individually
- Meta-analyse individual SNPs

# Calculating Power in Mendelian Randomization Randomization Studies



## mRnd: Power calculations for Mendelian Randomization

### Input

Calculate:

- Power
- Sample size

Provide:

**Sample size**

1000

$\alpha$

0.05

Type-I error rate

$\beta_{YZ}$

0

Continuous outcome

Binary outcome

Binary outcome derivations

Citation

About

### Two-stage least squares

Power	0.05	
NCP	0.00	Non-Centrality-Parameter
F-statistic	11.10	The strength of the instrument

Power or sample size calculations for two-stage least squares Mendelian Randomization studies using a genetic instrument  $Z$  (a SNP or allele score), a continuous exposure variable  $X$  (e.g. body mass index [BMI,  $\frac{kg}{m^2}$ ]) and a continuous outcome variable  $Y$  (e.g. blood pressure [mmHg]).

### YZ association

Power	0.05	
NCP	0.00	Non-Centrality-Parameter

Power or sample size calculations for the regression association of a genetic instrument  $Z$  (e.g. a BMI SNP), with a continuous outcome variable  $Y$  (blood pressure).



# Limitations to Mendelian Randomization

1- Population stratification

2- Canalisation (“Developmental compensation”)

3- The existence of instruments

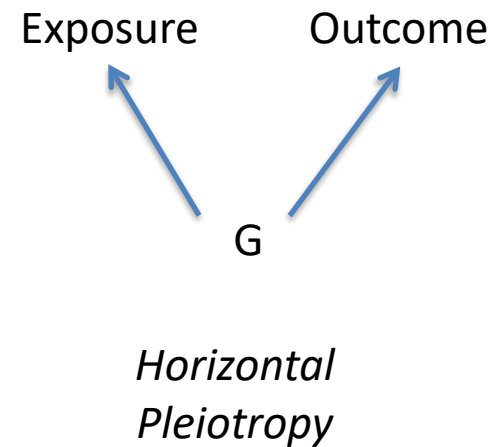
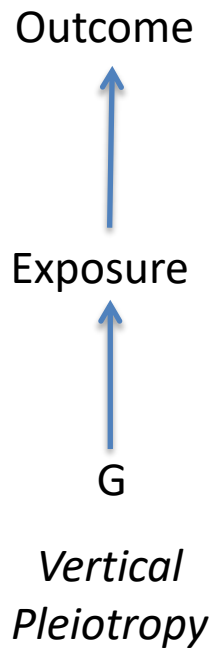
4- Power (also “weak instrument bias”)

**5- Pleiotropy**



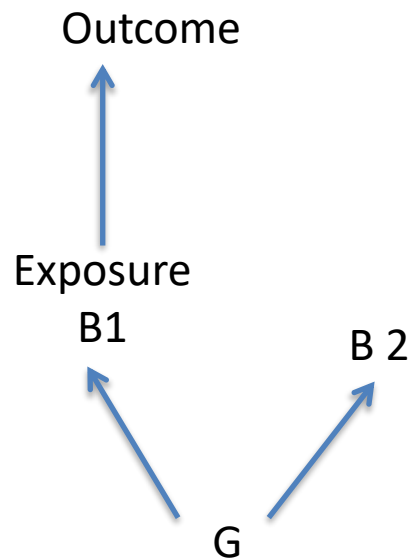
# Pleiotropy

- Genetic variant influences more than one trait
- Horizontal vs Vertical pleiotropy

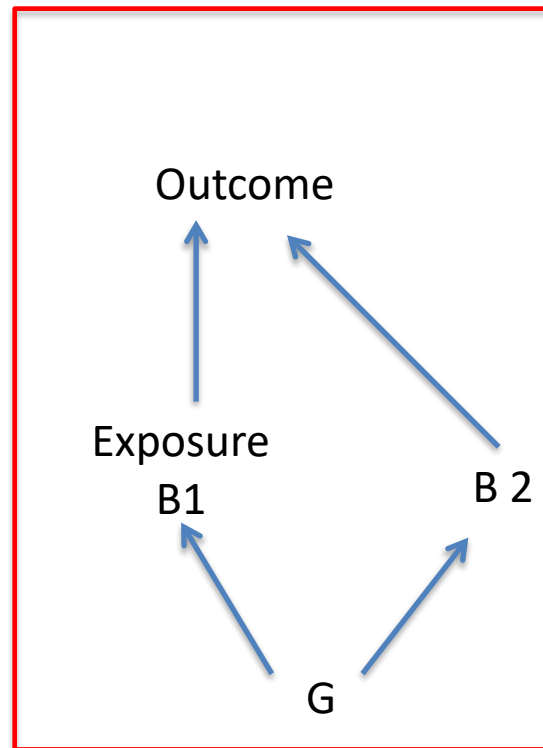


# Pleiotropy

- Genetic variant influences more than one trait
- Pleiotropy only violates MR's assumptions if it involves a pathway outside that of the exposure and is a pathway that affects your outcome



Violation



# MR Base

<http://www.mrbase.org/>



Jie "Chris" Zheng



Gib Hemani



Phil Haycock

The screenshot shows the MR Base website homepage in a web browser. The browser's address bar displays [www.mrbase.org/alpha/](http://www.mrbase.org/alpha/). The website features a dark sidebar on the left with the MR Base logo and navigation links: "Welcome to MR Base", "About", "Acknowledgements", and "Data access agreement". The main content area has a large MR Base logo and the text: "A platform for Mendelian randomisation using summary data from genome-wide association studies". Below this, a blue button labeled "Review access agreement" is visible. To the right, two statistics are displayed: "SNP-PHENOTYPE ASSOCIATIONS" with a value of 3,417,657,704 and "TRAITS WITH INSTRUMENTS" with a value of 340,164. The browser's taskbar at the bottom shows various application icons and the system clock indicating 12:14 AM on 21/06/2016.



Welcome to MR Base

About

Acknowledgements

Data access agreement

Logged in as  
**David Evans**  
epxde@bristol.ac.uk

Perform MR analysis

Choose exposures

Choose outcomes

Run MR

Quick SNP lookup

### Choosing instruments for the exposure

To use two sample MR to estimate the causal effect of an exposure on an outcome, the first step is to identify SNPs that are robustly associated with the exposure. These summary statistics for these SNPs can be taken from a sample from which there is no data on the outcome.

Please provide instruments by choosing from one of the data sources below, or by uploading your own data. You can choose multiple exposures to be analysed, and multiple instruments per exposure.

#### Choose instruments

##### Select exposure source

- Manual file upload
- NHGRI-EBI GWAS catalog
- MR Base GWAS catalog
- Gene expression QTLs
- Protein level QTLs
- Metabolite level QTLs
- Methylation level QTLs

#### Manual file upload

The file must be a plain text file.

To do simple SNP look ups it must have at least one column with the header **SNP**.

To do an MR analysis it must have the following column headers:

- **SNP** - rs IDs of the instruments for the exposure
- **beta** - effect sizes for each SNP
- **se** - standard errors
- **effect\_allele** - Effect allele

It's useful to have these columns too:

- **other\_allele** - Other allele
- **eaf** - Effect allele frequency

You can see an example file here: [telomere\\_length.txt](#)

#### Upload plain text file

Preview of uploaded table

Browse No files s



Welcome to MR Base

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epxde@bristol.ac.uk

Perform MR analysis

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Choose outcomes

Run MR

Quick SNP lookup

### LD clumping

Most two sample MR methods require that the instruments do not have LD between them.

#### Linkage disequilibrium

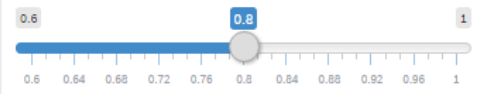
- Do not check for LD between SNPs
- Use clumping to prune SNPs for LD

### LD proxies

If a particular exposure SNP is not present in an outcome dataset, should proxy SNPs be used instead through LD tagging?

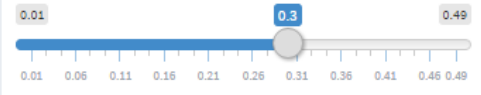
- Use proxies?

#### Minimum LD Rsq value



- Allow palindromic SNPs?

#### MAF threshold for aligning palindromes



### Select methods for analysis

Many methods exist for performing two sample MR. Different methods have sensitivities to different potential issues, accommodate different scenarios, and vary in their statistical efficiency.

#### Choose which methods to use:

- Wald ratio
- Fixed effects meta analysis (simple SE)
- Fixed effects meta analysis (delta method)
- Random effects meta analysis (delta method)
- Maximum likelihood
- MR Egger
- MR Egger (bootstrap)
- Weighted median
- Penalised weighted median
- Inverse variance weighted

### Submit

Once you have selected exposures, outcomes, and analysis options you are ready to perform the analysis.

Perform MR analysis

5e-08

Perform clumping

**Display columns**

- ID
- Trait
- Note
- First author
- Consortium
- Number of cases
- Number of controls
- Sample size
- Number of variants
- Year
- PubmedID
- Access
- Category
- Population
- Priority
- Sd
- Sex
- Subcategory
- Unit

Search:

ID	Trait	Note	First author	Consortium	Number of cases	Number of controls	Sample size	Number of variants	Year	PubmedID	Access	Category	Pop
300	300 LDL cholesterol		Willer CJ	GLGC			173082	2437752	2013	24097068	public	Risk factor	
781	781 LDL cholesterol	Metabo-chip	Willer CJ	GLGC			83198	120251	2013	24097068	public	Risk factor	
880	880 Total cholesterol in large LDL	L.LDL.C	Kettunen				21552	11871461	2016	27005778	public	Metabolites	
881	881 Cholesterol esters in large VLDL	L.LDL.CE	Kettunen				19273	11820655	2016	27005778	public	Metabolites	

- About
- Acknowledgements
- Data access agreement
- Logged in as **David Evans**  
epxde@bristol.ac.uk
- Perform MR analysis
- Choose exposures
- Choose outcomes
- Run MR
- MR Results
- Quick SNP lookup

**Display columns**

<input type="checkbox"/> ID	<input checked="" type="checkbox"/> First author	<input checked="" type="checkbox"/> Number of controls	<input type="checkbox"/> PubMedID	<input type="checkbox"/> Population	<input checked="" type="checkbox"/> Subcategory
<input checked="" type="checkbox"/> Trait	<input checked="" type="checkbox"/> Consortium	<input checked="" type="checkbox"/> Sample size	<input type="checkbox"/> Access	<input type="checkbox"/> Priority	<input type="checkbox"/> Unit
<input checked="" type="checkbox"/> Note	<input checked="" type="checkbox"/> Number of cases	<input checked="" type="checkbox"/> Number of variants	<input type="checkbox"/> Category	<input type="checkbox"/> Sd	<input type="checkbox"/> Sex
		<input checked="" type="checkbox"/> Year			

Show  entries

Search:

Trait	Note	First author	Consortium	Number of cases	Number of controls	Sample size	Number of variants	Year	Subcategory
6	Coronary heart disease	Peden	C4D	15420	15062	30482	540233	2011	Cardiovascular
7	Coronary heart disease	Nikpay	CARDIoGRAMplusC4D	60801	123504	184305	9455779	2015	Cardiovascular
8	Coronary heart disease	Schunkert H	CARDIoGRAM	22233	64762	86995	2420361	2011	Cardiovascular
9	Coronary heart disease	Deloukas	CARDIoGRAMplusC4D	63746	130681	194427	79129	2013	Cardiovascular

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Welcome to MR Base

About

Acknowledgements

Data access agreement

Logged in as  
**David Evans**  
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Perform MR analysis <

Choose exposures

Choose outcomes

Run MR

MR Results

Quick SNP lookup <

### Linkage disequilibrium

- Do not check for LD between SNPs
- Use clumping to prune SNPs for LD

### LD proxies

If a particular exposure SNP is not present in an outcome dataset, should proxy SNPs be used instead through LD tagging?

- Use proxies?

### Allele harmonisation

An important step in two sample MR is making sure that the effects of the SNPs on the exposure correspond to the same allele as their effects on the outcome. This is potentially difficult with palindromic SNPs.

#### Handling reference alleles

- All effect alleles are definitely on the positive strand
- Attempt to align strands for palindromic SNPs
- Exclude palindromic SNPs

potential issues, accommodate different scenarios, and vary in their statistical efficiency.

#### Choose which methods to use:

- Wald ratio
- Fixed effects meta analysis (simple SE)
- Fixed effects meta analysis (delta method)
- Random effects meta analysis (delta method)
- Maximum likelihood
- MR Egger
- MR Egger (bootstrap)
- Weighted median
- Penalised weighted median
- Inverse variance weighted

**Perform MR analysis**



# Useful References

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- ▶ [Brion et al \(2013\). Calculating statistical power in Mendelian randomization studies. \*Int J Epidemiol\*, 42\(5\), 1497-501.](#)
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- ▶ [Davies et al \(2018\). Reading Mendelian randomization studies: a guide, glossary, and checklist for clinicians. \*BMJ\*, Jul 12, 362:k601.](#)
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- ▶ [Hemani et al. \(2018\). The MR-Base platform supports systematic causal inference across the human phenome. \*Elife\*, May 30, 7, e34408.](#)
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- ▶ [Zheng et al. \(2017\). Recent developments in Mendelian randomization studies. \*Curr Epidemiol Rep\*, 4\(4\), 330-345.](#)