

# Sensitivity analyses in Mendelian randomization studies

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(Some slides adapted from Prof David Evans')

# Acknowledgment of **Country**

The University of Queensland (UQ) acknowledges the Traditional Owners and their custodianship of the lands on which we meet.

We pay our respects to their Ancestors and their descendants, who continue cultural and spiritual connections to Country.

We recognise their valuable contributions to Australian and global society.

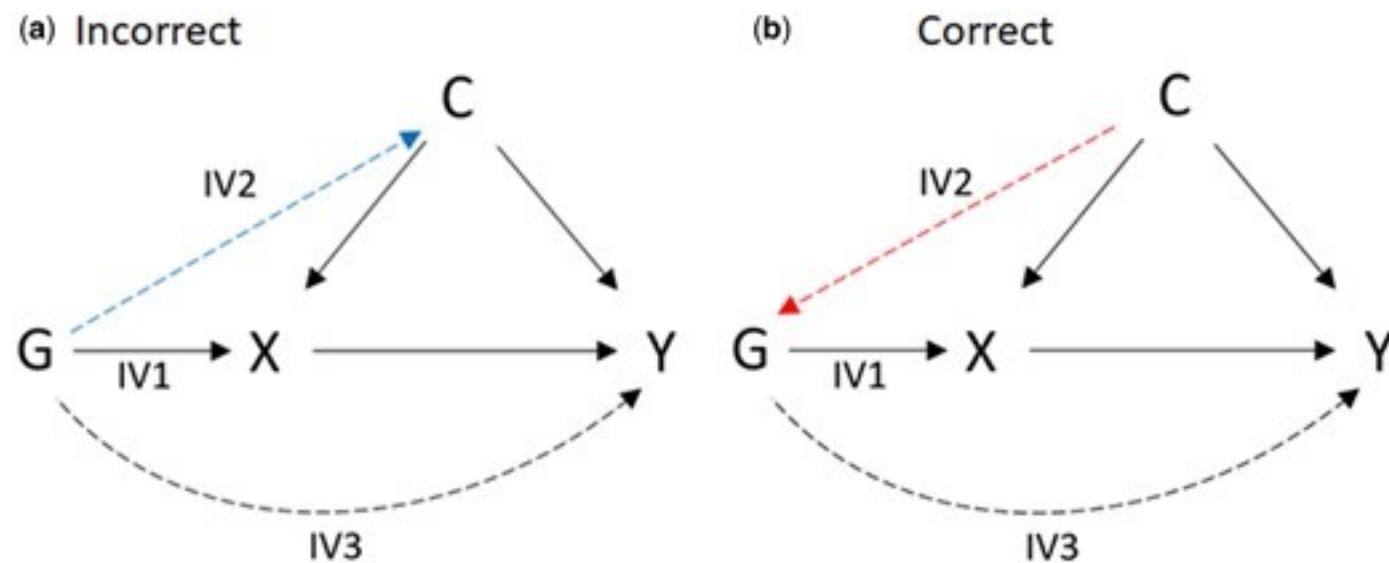


# Recap

- Mendelian randomization is a technique that uses genetically informative observational data to inform causality.
- Three core assumptions:
  - (1) **Relevance assumption:** SNP is associated with the exposure
  - (2) **Independence assumption:** SNP is NOT associated with confounding variables
    - There are no **confounders** of the association between the **instrumental variables (IVs)** and the **outcome**.
  - (3) **Exclusion restriction:** SNP ONLY associated outcome through the exposure
- Pleiotropy: Genetic variant influences more than one trait
- One-sample MR is where the SNP, exposure and outcome are all available in the same study.
- Two-sample MR is where the SNP-exposure association is measured in one study and the SNP outcome association is measured in a second study.

# Independence assumption (Second MR assumption)

There are no **confounders** of the association between the **instrumental variables (IVs)** and the **outcome**. As genetic variants are determined at conception it is not possible for them to be affected by confounders of exposure-outcome associations. When referring to the second MR assumption, factors that could influence the genetic variants and outcome include **population stratification** or structure, **intergenerational (dynastic)** effects and **assortative mating**. (MR Dictionary)



Carter & Anderson (2024) *International Journal of Epidemiology*

# Delta method to estimate SE of Wald ratio

$$\text{BETA}_{\text{SNP-exposure}} = X$$

$$\text{BETA}_{\text{SNP-outcome}} = Y$$

$$\text{Var}(\text{BETA}_{\text{Wald ratio}}) = \text{Var}(Y/X)$$

$$\approx \text{Var}(Y)/X^2 + (Y^2/X^4) * \text{Var}(X) - 2 * (Y/X^3) * \text{Cov}(X, Y) \leftarrow \text{This is based on the Delta method}$$

$$\approx \text{Var}(Y)/X^2$$

$$\text{SE}(\text{BETA}_{\text{Wald ratio}}) \approx \sqrt{\text{Var}(Y)/X^2}$$

$$= \text{SE}(Y)/X$$

$$= \text{SE}_{\text{SNP-outcome}} / \text{BETA}_{\text{SNP-exposure}}$$

# Outline

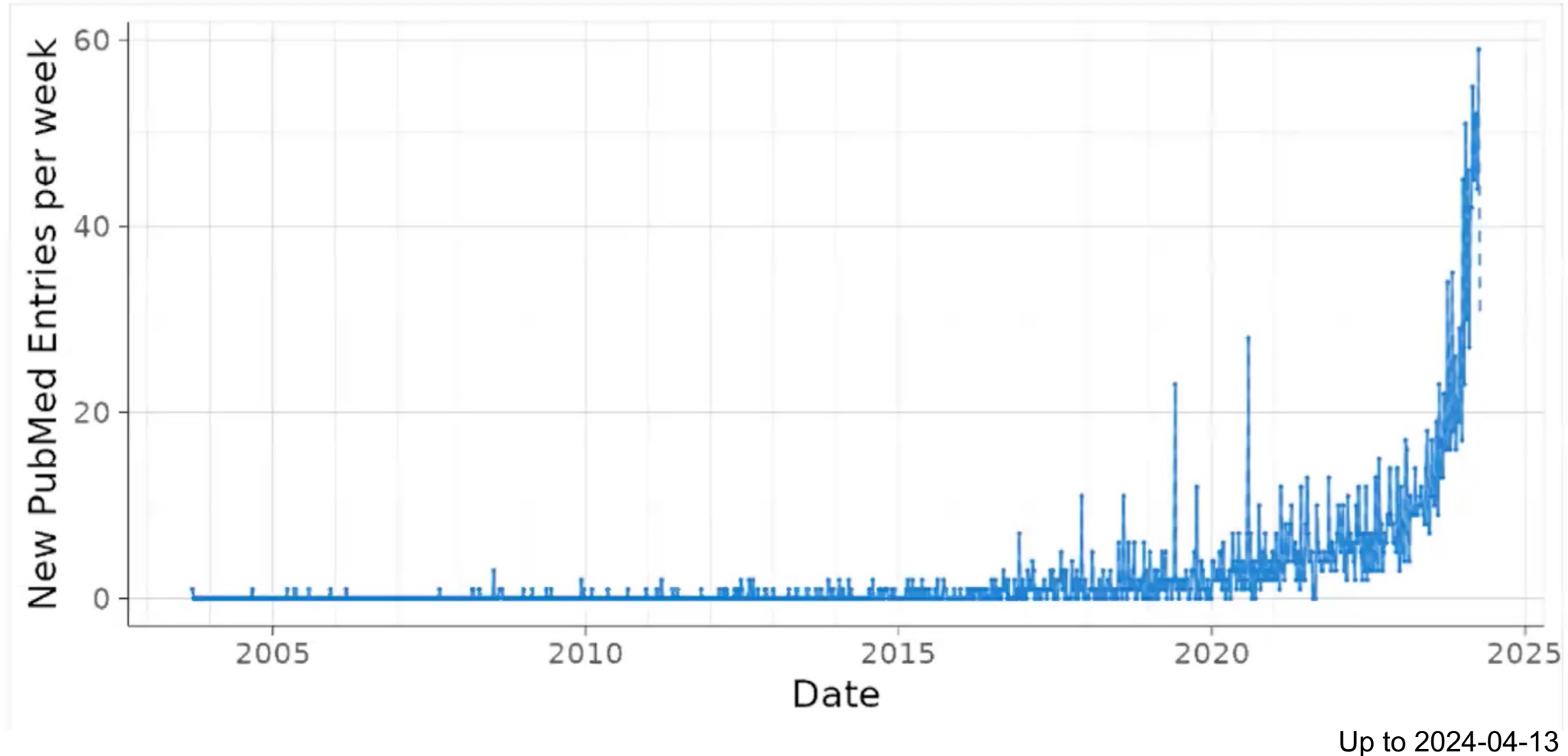
Set up a two-sample MR analysis using multiple genetic variants

Problems with pleiotropy and heterogeneity

15 minutes Break

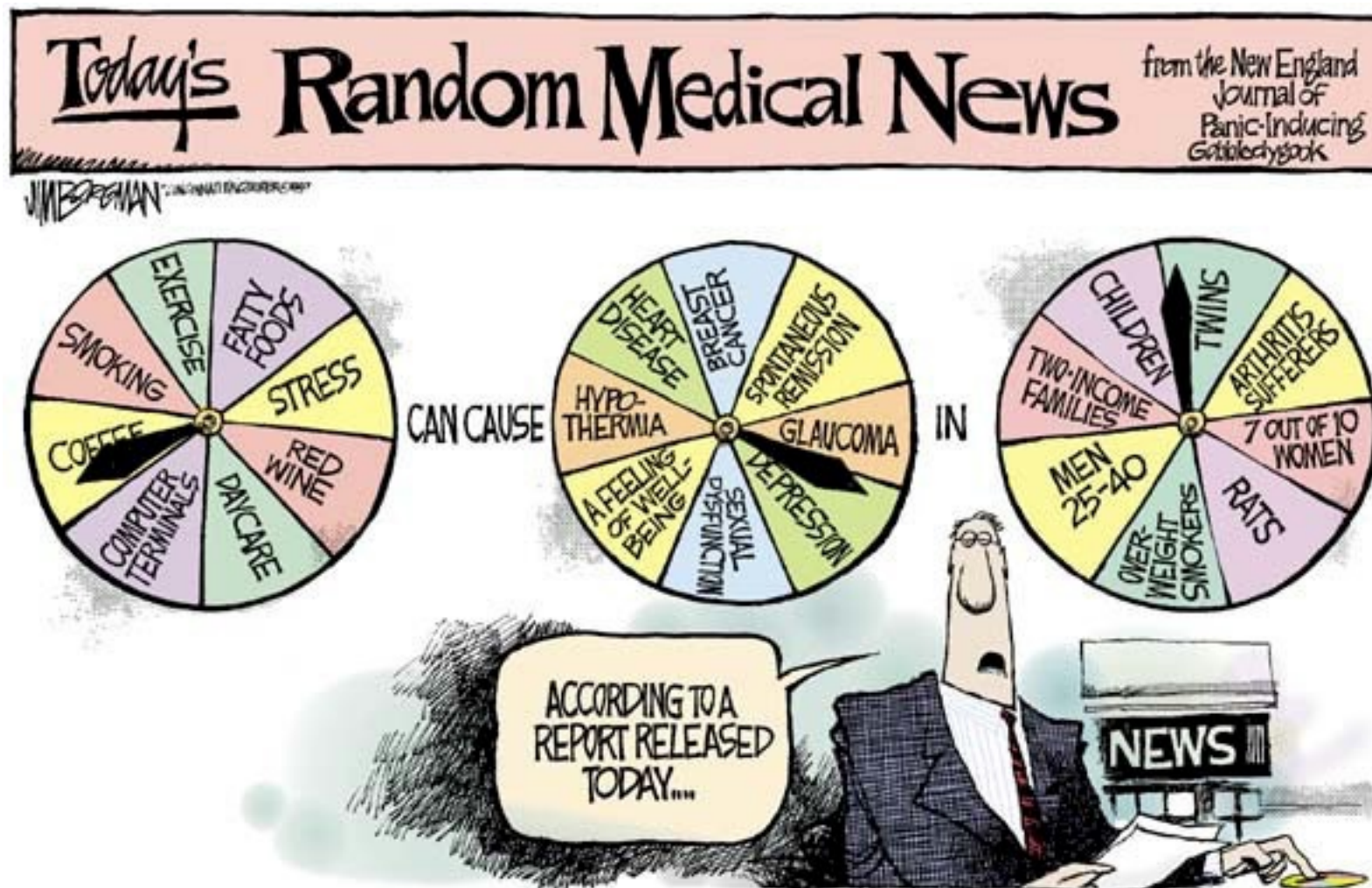
Methods for handling pleiotropy

# PubMed search for Mendelian randomi[z/s]ation (title only)





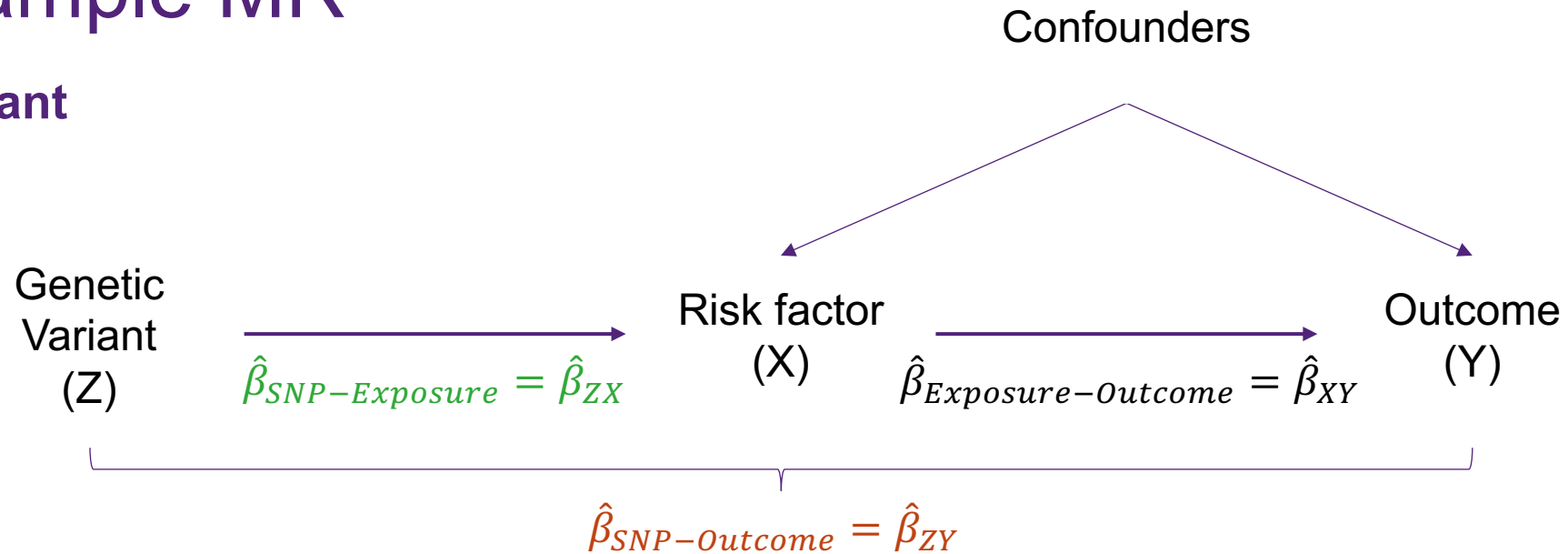
# MR studies today have become yesterday's observational studies





# Two-sample MR

## Single variant



Causal effect ( $\hat{\beta}_{XY}$ ) by Wald estimator:  $\frac{\hat{\beta}_{SNP-Outcome}}{\hat{\beta}_{SNP-Exposure}}$

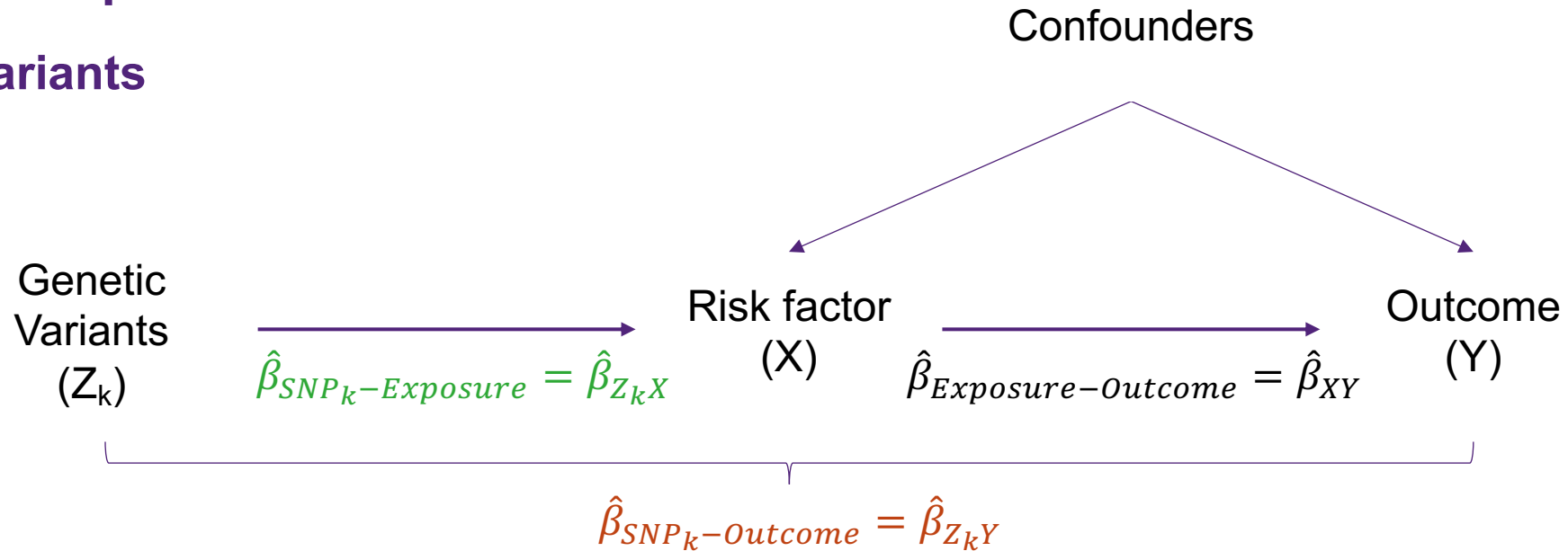
Standard error ( $\hat{\sigma}_{XY}$ ) by Delta method:  $\frac{\sigma_{SNP-Outcome}}{\hat{\beta}_{SNP-Exposure}}$

$$\hat{\beta}_{SNP-Outcome} = \hat{\beta}_{SNP-Exposure} \times \hat{\beta}_{Exposure-Outcome}$$

Can be estimated in different samples (e.g. two-sample MR)

# Two-sample MR

## Multiple variants



Causal effect by Wald estimator:

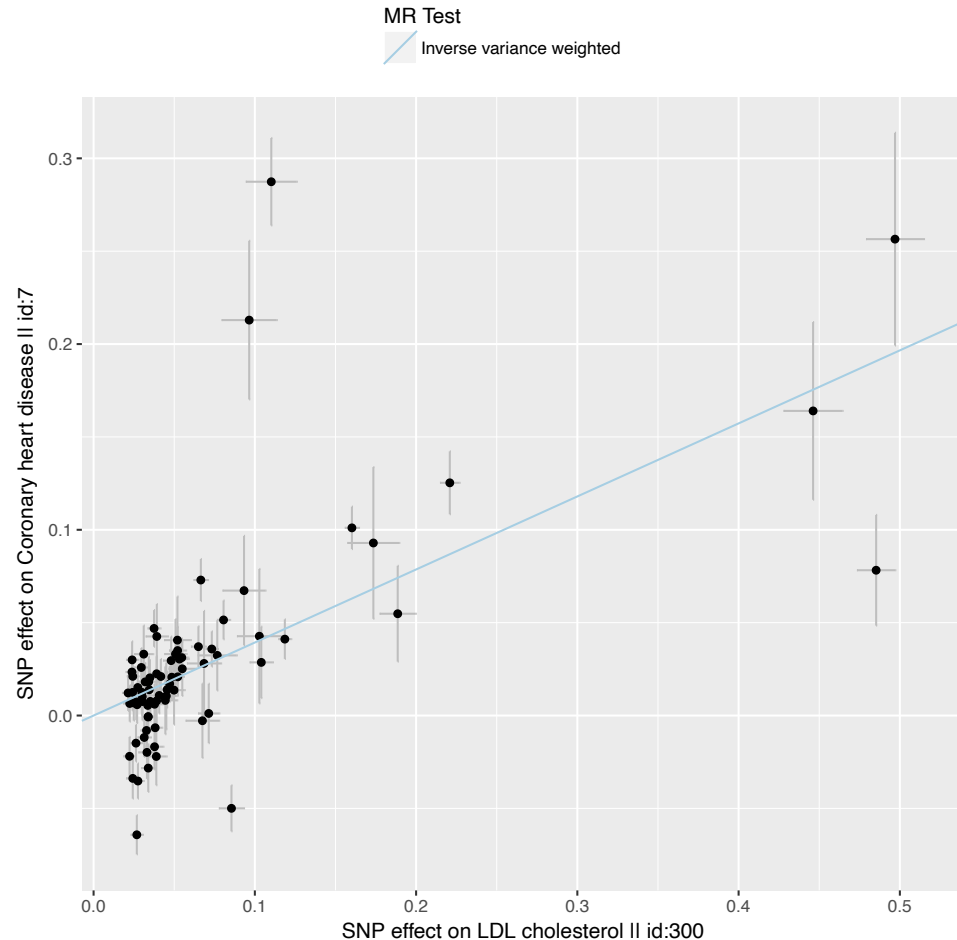
$$\hat{\beta}_{XY_k} = \frac{\hat{\beta}_{SNP_k-Outcome}}{\hat{\beta}_{SNP_k-Exposure}}$$

Inverse variance weighted (IVW) average causal effect:

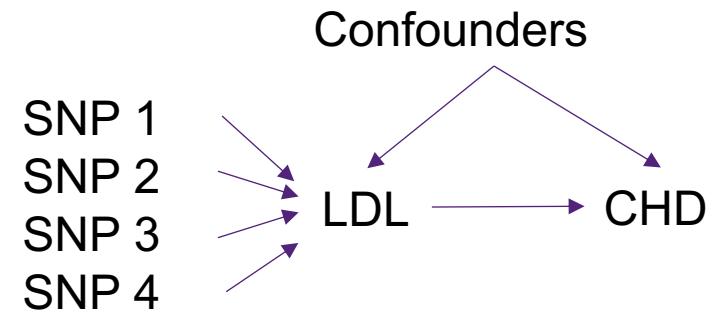
$$\hat{\beta}_{IVW} = \frac{\sum_{k=1}^K \hat{\beta}_{XY_k} w_k}{\sum_{k=1}^K w_k}$$

Where  $w_k = \frac{1}{\text{var}(\hat{\beta}_{XY_k})} = \frac{1}{\hat{\sigma}_{XY_k}^2}$  is the inverse variance of the causal effect estimated from the  $k^{\text{th}}$  genetic variant

# Fixed effects IVW-MR and weighted linear regression



- IVW is equivalent to a weighted regression of SNP-outcome effects on SNP-exposure effects passing through the origin
- The weights are the inverse of the variance of the individual causal effect estimates, i.e.,  $\frac{1}{\text{var}(\hat{\beta}_{XY_k})}$
- The slope is the estimate of the causal effect



# Assumptions for two-sample MR

If:

- The K genetic variants are perfectly uncorrelated (SNPs not in LD) and do not interact
- The two samples are homogenous (same underlying populations)
- No sample overlap (this could be relaxed if all IVs are “valid”)
- Constant causal effect at each level of the exposure

Then two-sample MR can consistently estimate the true causal effect.

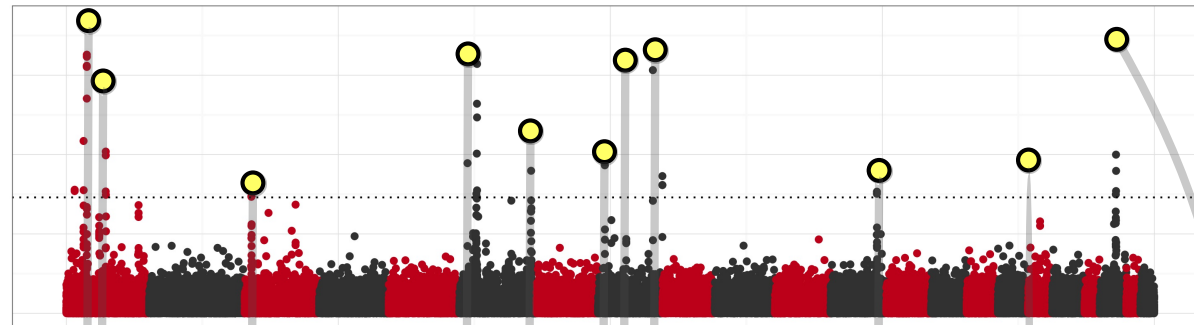
Two-sample MR is still vulnerable to weak instrument bias

- Bias towards the null effect, not the observational estimate
- If approximate F-statistic ( $\hat{\beta}_{Z_k X}^2 / \sigma_{Z_k X}^2$ ) is greater than 10, then the expected dilution  $\hat{\beta}_{XY_k}$  of towards zero is less than 10%

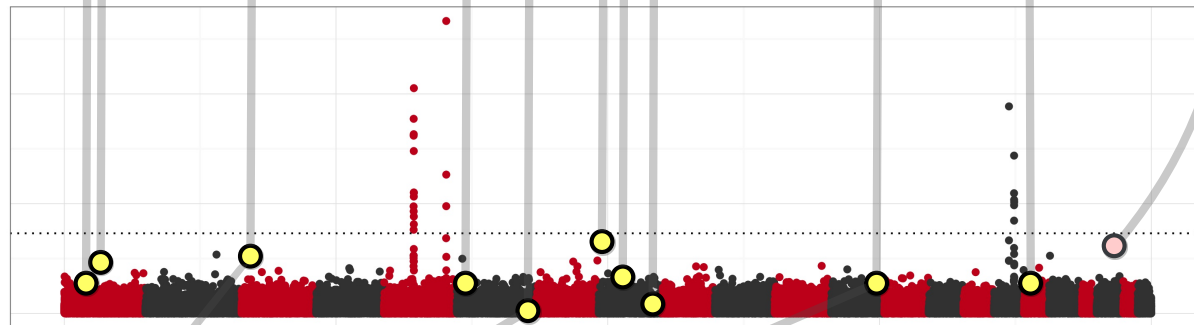
# Performing two-sample MR with summary statistics

A convenient approach when sharing individual level data is impractical

Obtain instruments from exposure GWAS

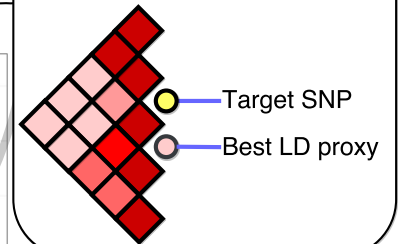


Extract SNP effects from outcome GWAS



## LD Proxies

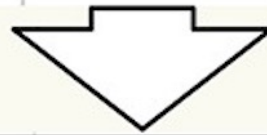
If an exposure instrument is not available in the outcome GWAS then look for LD proxies in 1000 genomes





# Harmonise exposure and outcome effects

SNP	Exposure GWAS				Outcome GWAS			
	Effect	Effect allele	Other allele	Effect allele frequency	Effect	Effect allele	Other allele	Effect allele frequency
rs12345	0.132	A	G	0.28	0.022	A	G	0.26
rs23456	-0.485	G	T	0.41	<b>0.056</b>	<b>T</b>	<b>G</b>	<b>0.61</b>
rs34567	0.203	G	C	0.11	<b>-0.046</b>	<b>G</b>	<b>C</b>	<b>0.88</b>



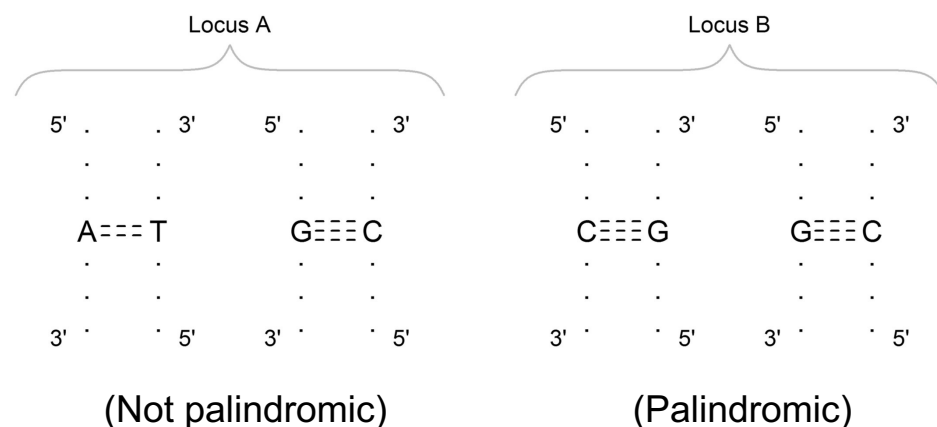
SNP	Exposure GWAS				Outcome GWAS			
	Effect	Effect allele	Other allele	Effect allele frequency	Effect	Effect allele	Other allele	Effect allele frequency
rs12345	0.132	A	G	0.28				
rs23456	-0.485	G	T	0.41				
rs34567	0.203	G	C	0.11				

# The issue of strand (palindromic variant)

SNP	Exposure GWAS				Outcome GWAS			
	Effect	Effect allele	Other allele	Effect allele frequency	Effect	Effect allele	Other allele	Effect allele frequency
rs12345	0.132	A	G	0.28	0.022	A	G	0.26
rs23456	-0.485	G	T	0.41	<b>0.056</b>	<b>T</b>	<b>G</b>	<b>0.61</b>
rs34567	0.203	G	C	0.11	<b>-0.046</b>	<b>G</b>	<b>C</b>	<b>0.88</b>



Palindromic



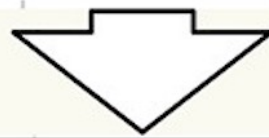
	Locus A	Locus B
Genotype of the forward strand (5' > 3')	A/G	C/G
Genotype of the reverse strand (3' > 5')	T/C	G/C

Exposure GWAS and outcome GWAS may be based on the genotypes of different strands. When there are palindromic SNPs, simply merging datasets based on effect alleles may result in the effect being the opposite.

# Harmonise exposure and outcome effects

SNP	Exposure GWAS				Outcome GWAS			
	Effect	Effect allele	Other allele	Effect allele frequency	Effect	Effect allele	Other allele	Effect allele frequency
rs12345	0.132	A	G	0.28	0.022	A	G	0.26
rs23456	-0.485	G	T	0.41	<b>0.056</b>	<b>T</b>	<b>G</b>	<b>0.61</b>
rs34567	0.203	G	C	0.11	<b>-0.046</b>	<b>G</b>	<b>C</b>	<b>0.88</b>

Palindromic



SNP	Exposure GWAS				Outcome GWAS			
	Effect	Effect allele	Other allele	Effect allele frequency	Effect	Effect allele	Other allele	Effect allele frequency
rs12345	0.132	A	G	0.28	0.022	A	G	0.26
rs23456	-0.485	G	T	0.41	<b>-0.056</b>	<b>G</b>	<b>T</b>	<b>0.39</b>
rs34567	0.203	G	C	0.11	<b>0.046</b>	<b>G</b>	<b>C</b>	<b>0.12</b>

# Strand issue exercise (5 mins)

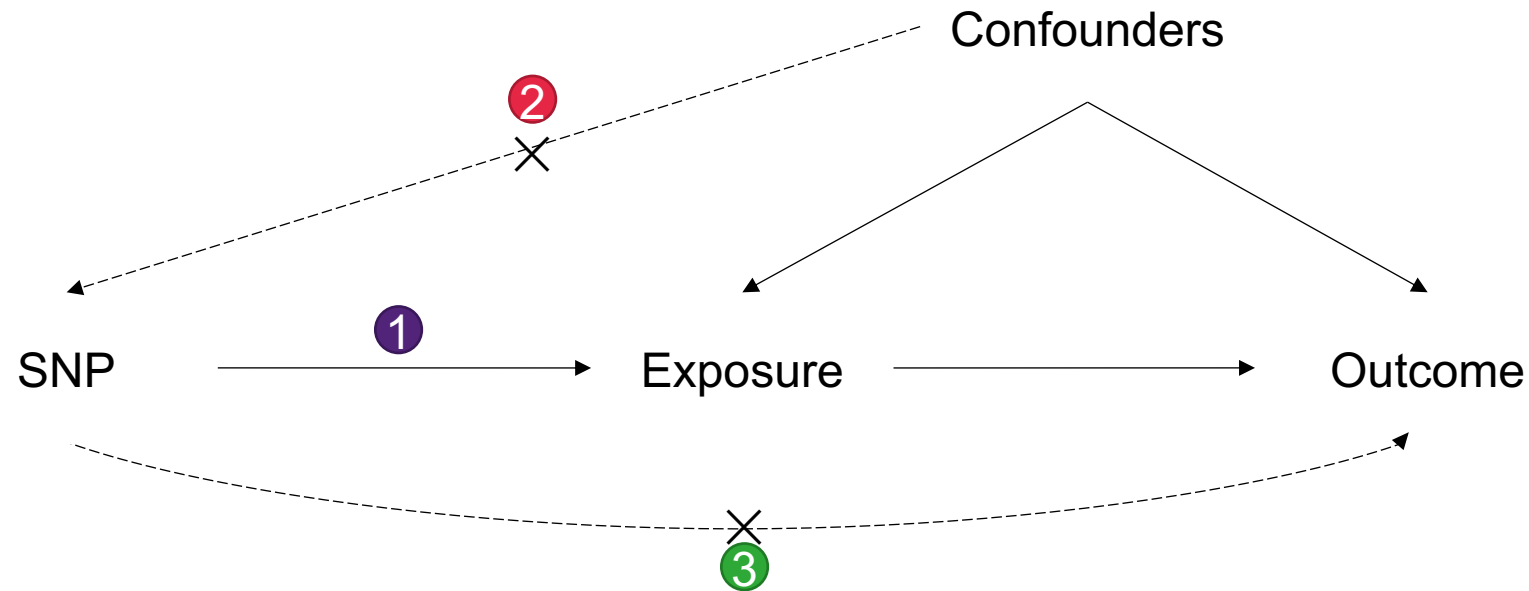
SNP	Study 1 alleles	Study 1 allele freq	Study 2 alleles	Study 2 allele freq	Verdict?
rs1	A/G	0.2	A/G	0.2	
rs2	G/T	0.3	T/G	0.72	
rs3	G/C	0.65	G/C	0.62	
rs4	A/T	0.49	A/T	0.5	
rs5	A/T	0.12	A/T	0.89	
rs6	A/G	0.4	A/T	0.4	

# WHAT IS THE PROBLEM WITH MR?

- MR uses genetic variants to test for causal relationships between phenotypic exposures and disease-related outcomes
- Due to the proliferation of GWAS, it is increasingly common for MR analyses to use large numbers of genetic variants
- Increased power but greater potential for **horizontal pleiotropy**
- Pleiotropic variants affect biological pathways other than the exposure under investigation and therefore can lead to biased causal estimates and false positives under the null



# Three core MR assumptions



- (1) Relevance assumption: SNP is associated with the exposure
- 👉 (2) Independence assumption: SNP is NOT associated with confounding variables (population stratification, assortative mating, dynastic effects).
- 👉 (3) Exclusion restriction: SNP ONLY associated outcome through the exposure

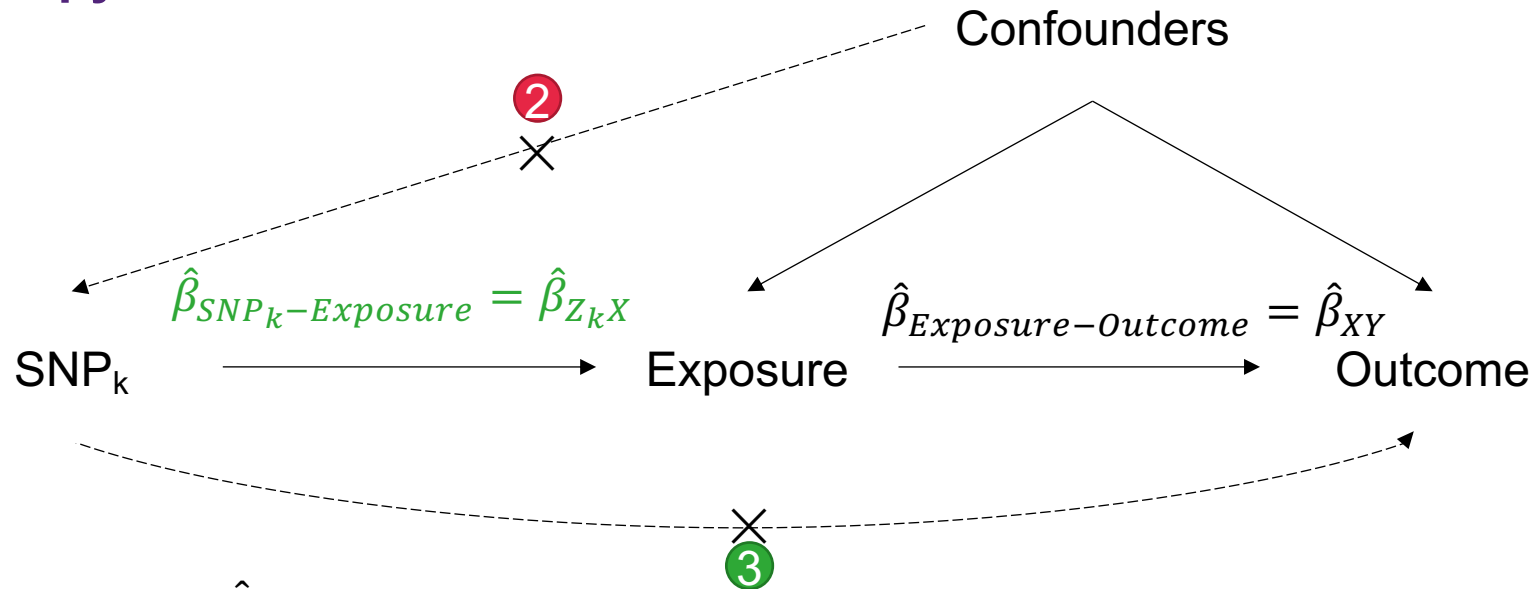
# MR methods for handling horizontal pleiotropy

Table 1 | List of MR estimation methods

Category	Core IV assumption relaxed	Individual-level data	Summary data
'Basic' MR method	None	Wald ratio estimation, 2SLS regression analysis <sup>a</sup>	Wald ratio estimation, IVW <sup>a,37</sup>
Weak instrument robust methods	IV1; allows for weak instruments	LIML <sup>26</sup> , allele score approaches <sup>26</sup>	MR RAPS <sup>87</sup> , debiased IVW <sup>187</sup> , MR GRAPPLE <sup>88</sup> , NOME adjustment <sup>188</sup> , two-sample AR <sup>189</sup>
Outlier/variant selection and removal	IV3; allows for balanced/sparse pleiotropy	Weighted median <sup>190</sup>	Weighted median <sup>a,82</sup>
Outlier/variant selection and removal	IV3; allows for (some) directional pleiotropy	sisVIVE <sup>70</sup> , adaptive LASSO <sup>71</sup> , weighted mode <sup>190</sup>	Weighted mode <sup>a,83</sup> , MR LASSO <sup>84</sup> , Steiger filtering <sup>a,93</sup> , Welch-weighted Egger <sup>94</sup> , contamination mixture <sup>191</sup> , GSMR <sup>79</sup> , MR-Clust <sup>192</sup> , Bayesian MIMR <sup>193</sup> , CIV <sup>72</sup>
Outlier/variant adjustment	IV3; allows for balanced pleiotropy	Limited approaches currently available	MR RAPS <sup>87</sup> , MRCIP <sup>194</sup>
Outlier/variant adjustment	IV3; allows for (some) directional pleiotropy	Limited approaches currently available	MR TRYX <sup>85</sup> , MR Robust <sup>84</sup> , MR CAUSE <sup>89</sup> , MR PRESSO <sup>86</sup> , MR GRAPPLE <sup>88</sup> , MRMix <sup>195</sup> , MR-LDP <sup>196</sup> , IMRP <sup>197</sup> , regularization <sup>198</sup> , MR-PATH (see preprint <sup>199</sup> )
Estimation adjustment	IV3; allows for balanced pleiotropy	Limited approaches currently available	Debiased IVW <sup>187</sup>
Estimation adjustment	IV3; allows for (some) directional pleiotropy	Constrained IVs <sup>72</sup> , multivariable MR <sup>73</sup>	MR Egger <sup>90</sup> , multivariable MR <sup>73,91</sup> , MR Link <sup>200</sup> , hJAM <sup>201</sup> , GIV <sup>202</sup> , Bayesian network analysis <sup>203</sup> , BMRE <sup>204</sup> , BayesMR <sup>205</sup>
Environmental control adjustment	IV3; allows for (some) directional pleiotropy	MR GxE <sup>75,76</sup> , MR GENIUS <sup>77</sup>	Limited approaches currently available

# Two-sample MR

No direct pleiotropy



$$\hat{\beta}_{SNP-Outcome} = \hat{\beta}_{SNP-Exposure} \times \hat{\beta}_{Exposure-Outcome}$$

Causal effect by Wald estimator:

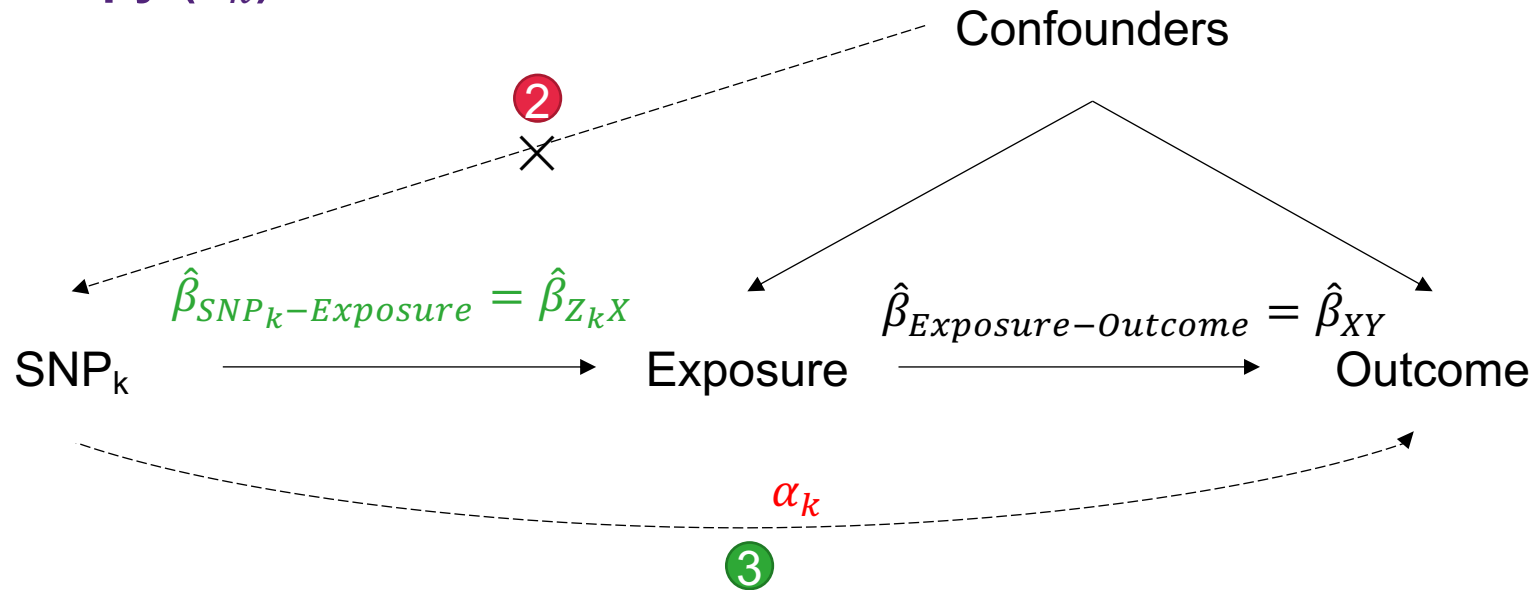
$$\hat{\beta}_{XY_k} = \frac{\hat{\beta}_{SNP_k-Outcome}}{\hat{\beta}_{SNP_k-Exposure}}$$

Inverse variance weighted (IVW) average causal effect:

$$\hat{\beta}_{IVW} = \frac{\sum_{k=1}^K \hat{\beta}_{XY_k} w_k}{\sum_{k=1}^K w_k}$$

# Two-sample MR

With direct pleiotropy ( $\alpha_k$ )



$$\hat{\beta}_{SNP-Outcome} = \hat{\beta}_{SNP-Exposure} \times \hat{\beta}_{Exposure-Outcome} + \alpha_k$$

Causal effect by Wald estimator:

$$\frac{\hat{\beta}_{SNP_k-Outcome}}{\hat{\beta}_{SNP_k-Exposure}} = \hat{\beta}_{Exposure-Outcome} + \frac{\alpha_k}{\hat{\beta}_{SNP_k-Exposure}}$$

Inverse variance weighted (IVW) average causal effect:

$$\frac{\sum_{k=1}^K \hat{\beta}_{XY_k} w_k}{\sum_{k=1}^K w_k} = \hat{\beta}_{Exposure-Outcome} + \text{Bias}(\alpha, \hat{\beta}_{SNP_k-Exposure})$$

# Heterogeneity

We expect that each SNP represents an independent study, and each should give an unbiased (if imprecise) estimate of the causal effect of x on y.

Heterogeneity, where effect estimates are more different than expected due to standard errors, arises because at least some of the instruments are invalid.

Cochran's Q statistic (heterogeneity test):

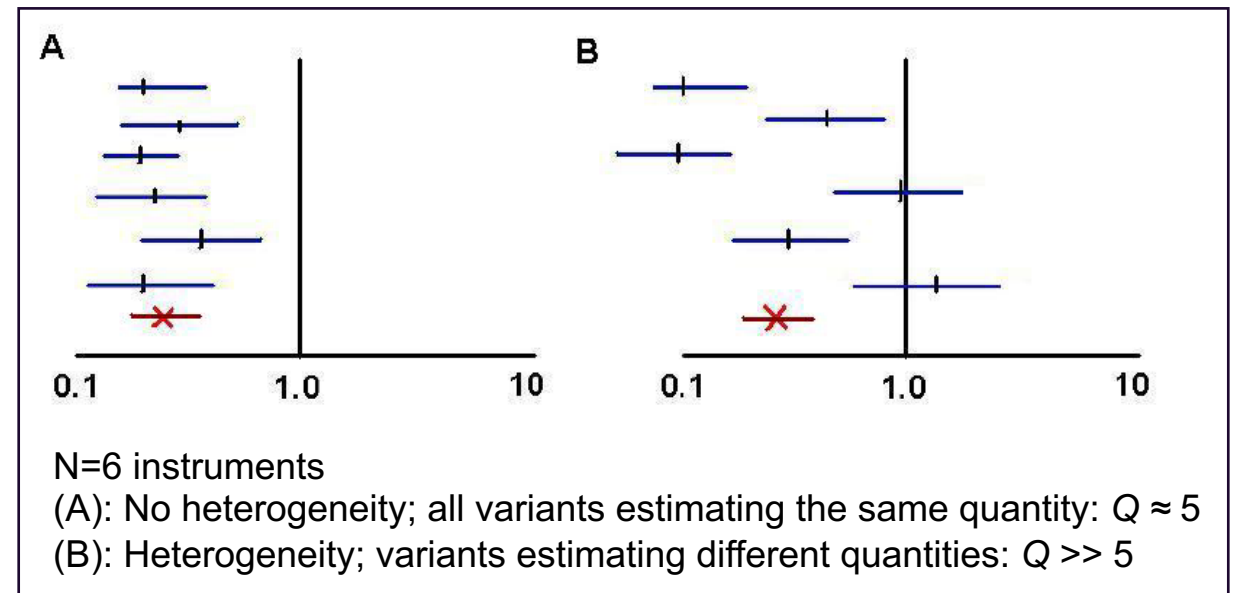
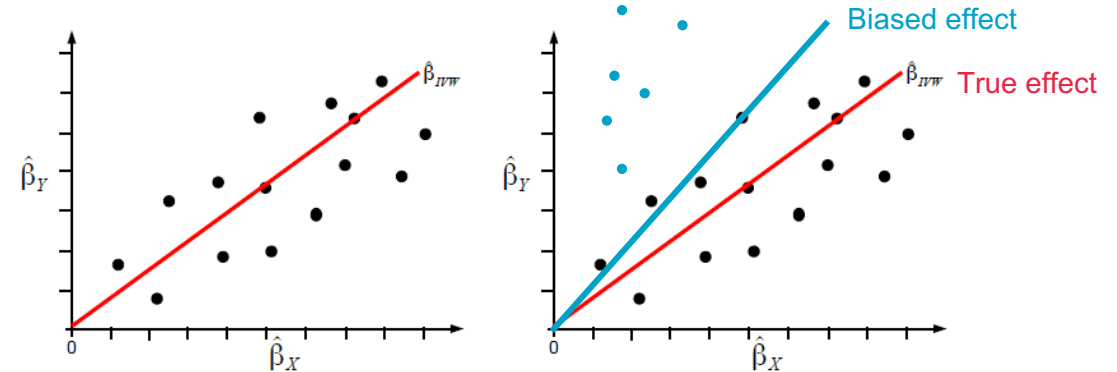
$$Q = \sum_{k=1}^K w_k (\hat{\beta}_{XY_k} - \hat{\beta}_{IVW})^2$$

Where  $w_k$  is the weight (i.e. inversed variance) of the causal estimate at SNP  $k$ .

If MR model is correct, Q follows a  $\chi^2$  distribution with expected value  $K-1$ .

If Q is larger than  $K-1$ , then the estimates exhibit over-dispersion.

- SNPs are valid instruments
- SNPs associated with outcome via an independent pathway.





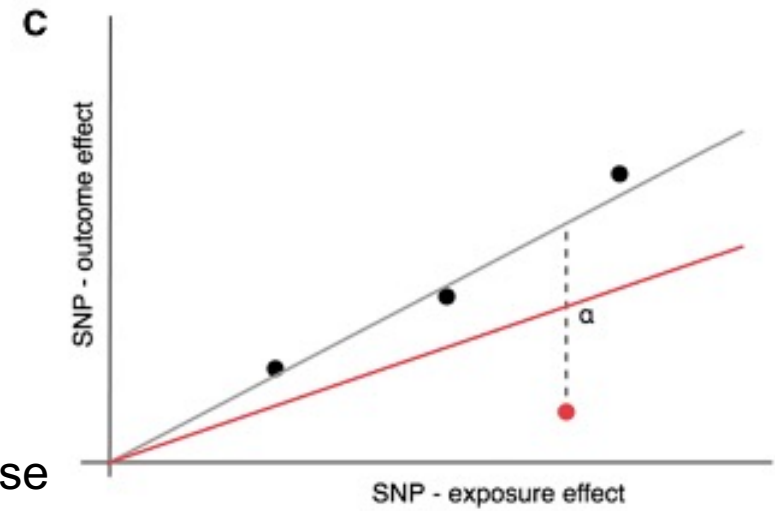
# Accounting for heterogeneity

## Option 1: Remove outliers

- Some SNPs might contribute to the majority of the heterogeneity.
- If we assume these are the invalid instruments, then the IVW estimate excluding them should be less biased.

However – beware of:

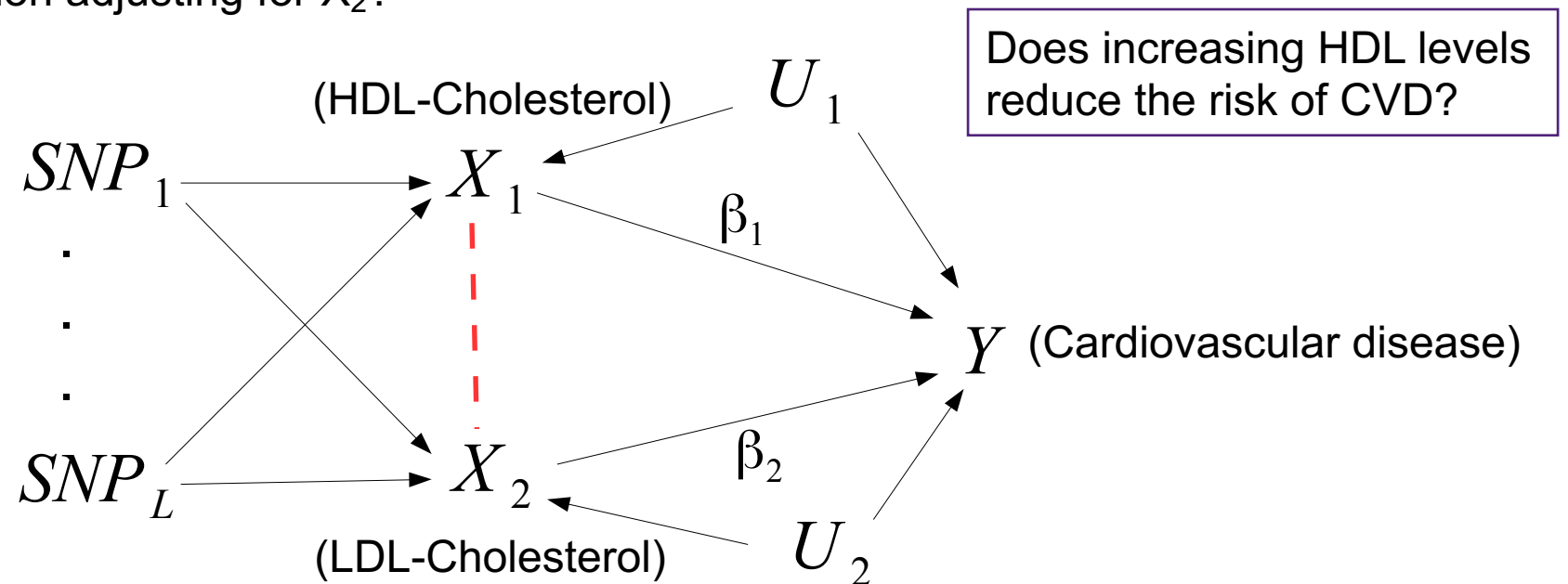
- Cherry picking – remove outliers will artificially provide a more precise estimate
- What if the outlier is the only valid instrument, and all the others are invalid?
- E.g. cis-variants for gene expression, DNA methylation, and protein levels. CRP levels are best instrumented by variants within the *CRP* gene region. Most other variants that come up in CRP GWAS are upstream effects related to inflammation.



# Accounting for heterogeneity

## Option 2: Multivariable MR

- We are testing for whether  $X_1$  has an influence on  $Y$
- We know that some instruments for  $X_1$  also have influences on  $X_2$
- This opens up the possibility of horizontal pleiotropy biasing our estimate
- What is the  $X_1$ - $Y$  association adjusting for  $X_2$ ?

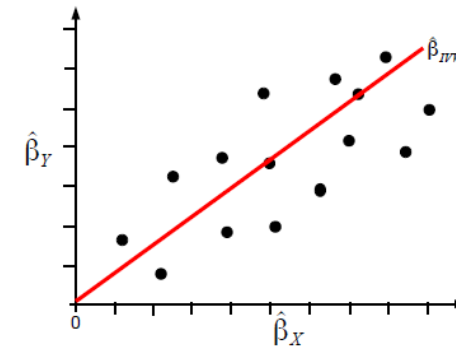


# Accounting for heterogeneity

## Option 3: Fit a model that is robust to some model of horizontal pleiotropy

IVW fixed effects estimator assumes all SNPs are valid instruments and averages across them all.

- Clear trend in estimates increasing with  $\hat{\beta}_{Z_kX}$  from origin
- Cochran's  $Q \approx K - 1$  (no heterogeneity)

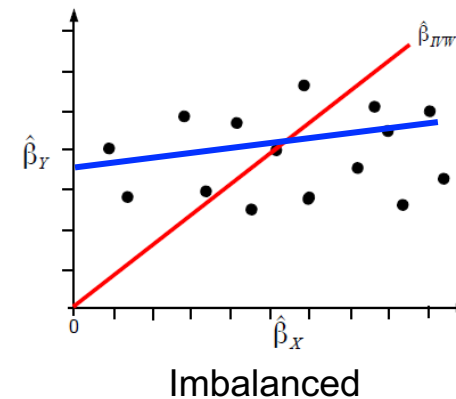
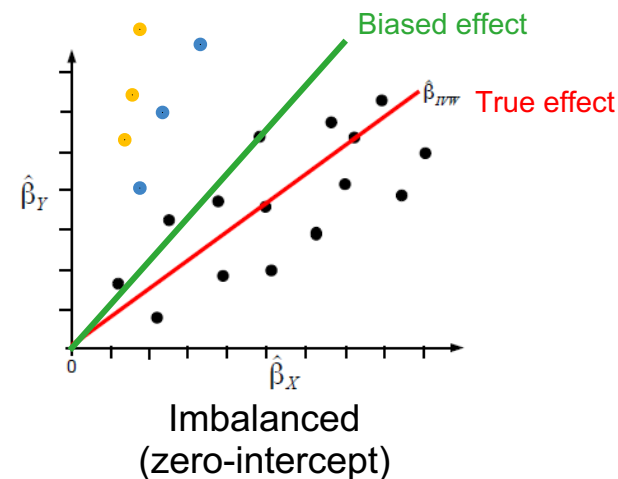
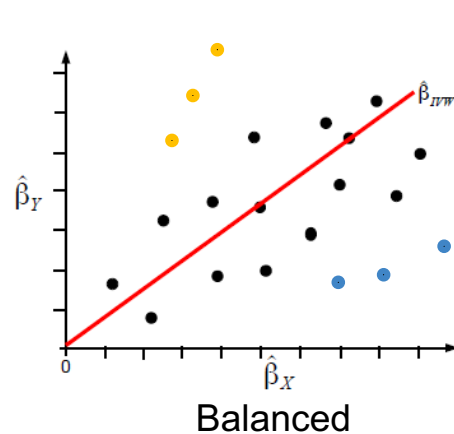


# Accounting for heterogeneity

## Option 3: Fit a model that is robust to some model of horizontal pleiotropy

IVW random effects estimator allows all SNPs to be invalid due to pleiotropy as long as the pleiotropy is balanced.

- The standard error of the causal estimate increases with the degree of heterogeneity.



We could therefore regress the SNP-outcome associations on the SNP-exposure associations, but allow for a **non-zero intercept** in the regression. This is the principal behind **MR-Egger regression**.

- SNPs are valid instruments
- SNP associated with outcome via confounder.
- SNP associated with outcome via an independent pathway.

Trend away from origin + heterogeneity

- Zero-intercept condition unreasonable
- IVW does not appear to be a good fit

Pleiotropy potentially causes heterogeneity and bias

# Break time

by Canva AI image generator





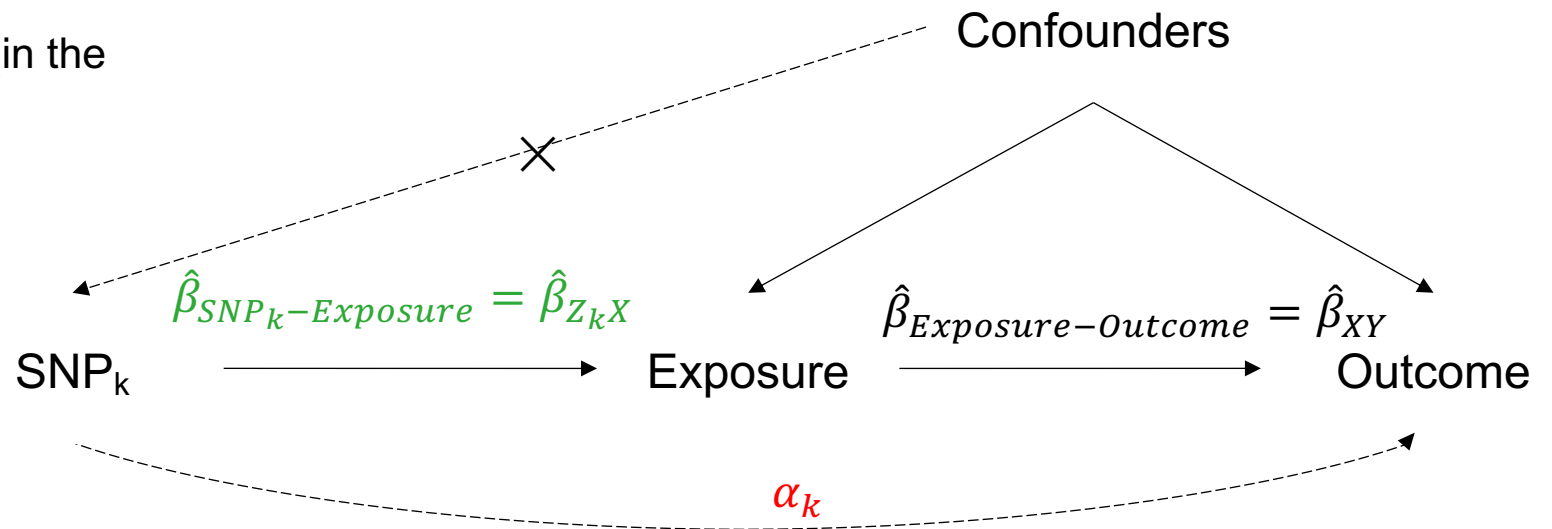
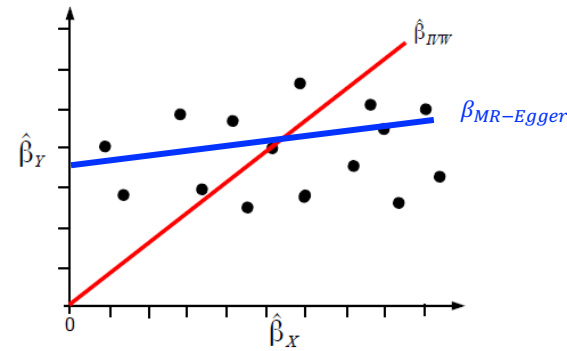
# MR-Egger regression: Central concept

MR-Egger allows for a **non-zero intercept** in the regression.

When multiple SNPs are used as instruments, MR-Egger can:

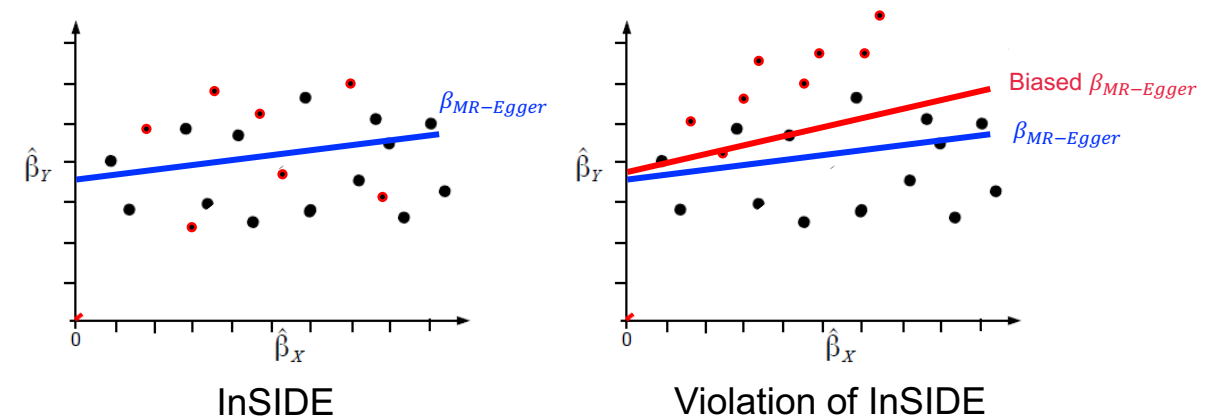
- Identify the presence of “directional” pleiotropy (biasing the causal estimate in IVW)
- Provide a less biased causal estimate (in the presence of pleiotropy)

MR-Egger lacks power.



# MR-Egger regression

MR-Egger regression relies on the InSIDE (INstrument Strength Independent of Direct Effect) assumption, which states that the pleiotropic effects of SNPs must be independent of their strength as instruments.

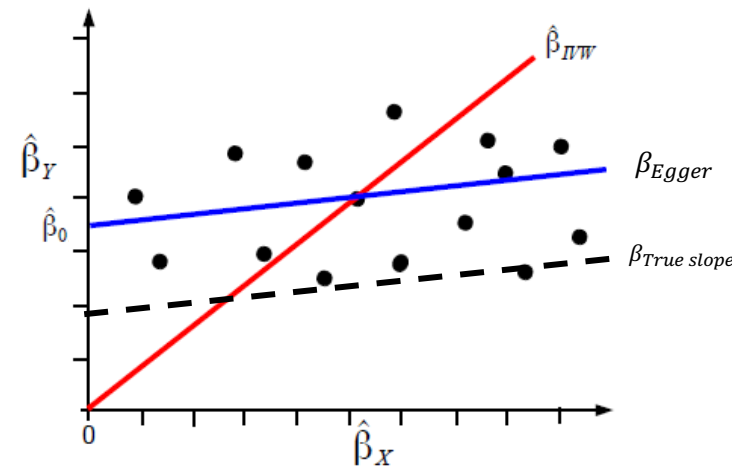


- SNP not associated with outcome via an independent pathway
- SNP associated with outcome via an independent pathway

IVW model:  $\hat{\beta}_{Yk} = \underbrace{\beta_{IVW}}_{\text{Slope}} \hat{\beta}_{Xk} + \varepsilon_{Yk}$

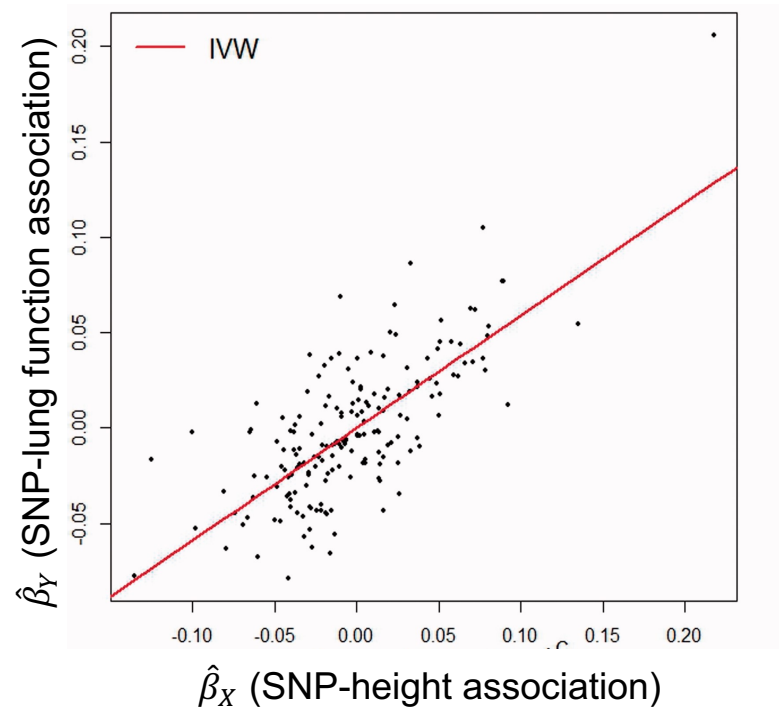
MR-Egger model:  $\hat{\beta}_{Yk} = \beta_0 + \underbrace{\beta_{Egger}}_{\text{Slope}} \hat{\beta}_{Xk} + \varepsilon_{Yk}$

- $\beta_0$  is the intercept term.  $\beta_0$  can be interpreted as the average pleiotropic effect across all genetic variants. A non-zero  $\beta_{0E}$  indicates directional pleiotropy.
- $\beta_{Egger}$  is the causal estimate adjusted for directional pleiotropy



# MR-Egger regression

## Example: height and lung function

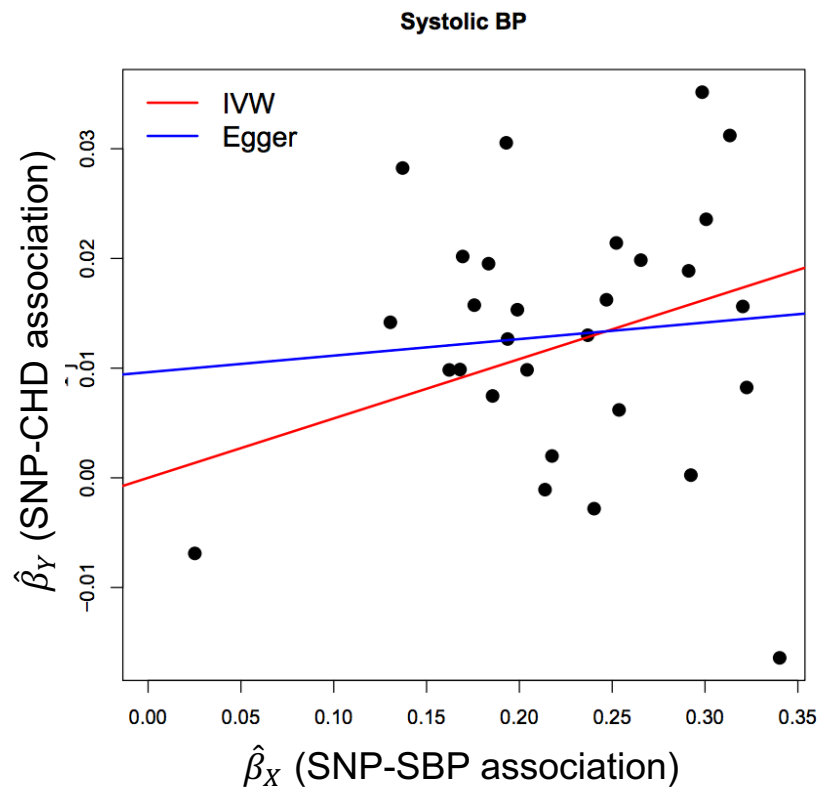


IVW = 0.59 (95% CI: 0.50, 0.67 )

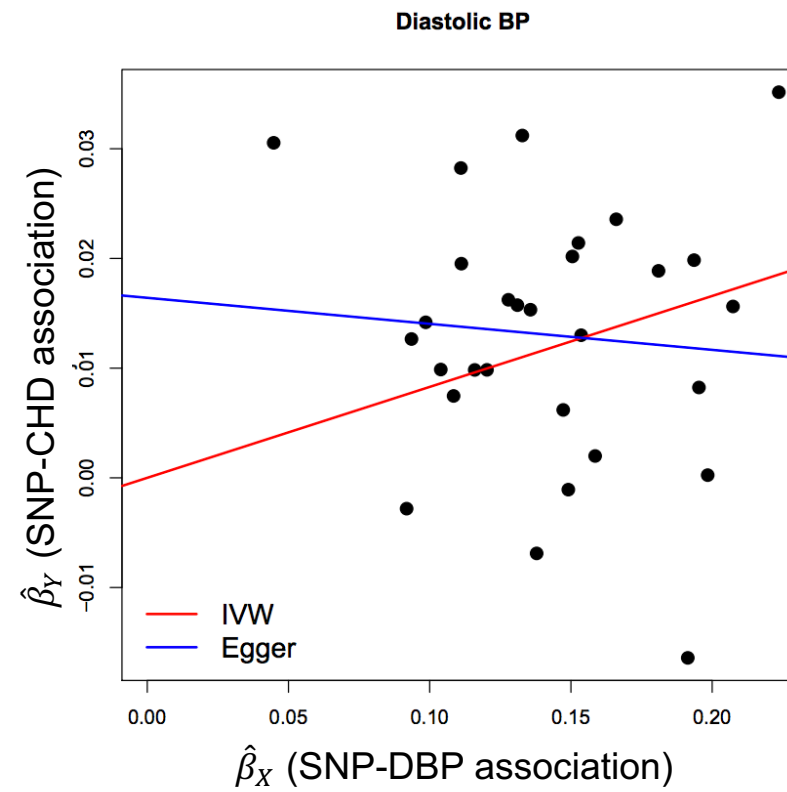
MR-Egger = 0.58 (95% CI: 0.50, 0.67);  
intercept = -0.001 (p = 0.5)

# MR-Egger regression

## Example: BP and Coronary Heart Disease



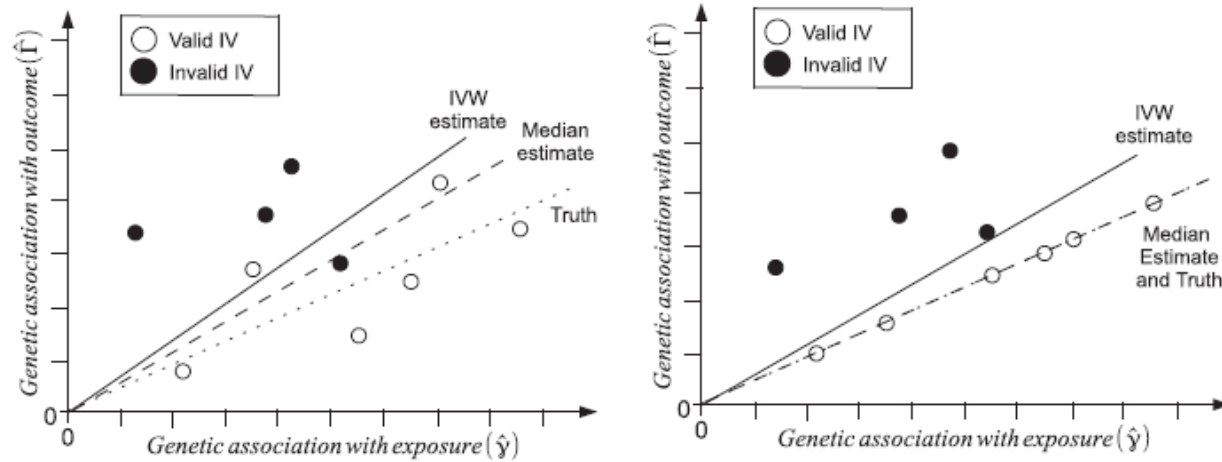
IVW = 0.054 logOR/mmHg;  $p = 4 \times 10^{-6}$   
 Egger = 0.015 logOR/mmHg;  $p = 0.6$



IVW = 0.083 logOR/mmHg;  $p = 1 \times 10^{-5}$   
 Egger = -0.024 logOR/mmHg;  $p = 0.7$

# Median based methods (Median Estimator)

Order causal estimates (Wald ratio) and take the median.



**Assumption: >50% of the instrumental variables are valid.**

No restrictions need to be placed on the invalid IVs:

- InSIDE assumption not required
- Violations of #2 and #3 MR assumptions are allowed

**Figure 2.** Fictional example of a Mendelian randomization analysis with 10 genetic variants—six valid instrumental variables (hollow circles) and four invalid instrumental variables (solid circles) for finite sample size (left) and infinite sample size (right) showing IVW (solid line) and simple median (dashed line) estimates compared with the true causal effect (dotted line). The ratio estimate for each genetic variant is the gradient of the line connecting the relevant datapoint for that variant to the origin; the simple median estimate is the median of these ratio estimates.

# Median based methods

## Simple median estimator

- Odd number of IVs: middle ratio estimate
- Even number of IVs: median is the average of the two middle estimates  $\left(\frac{1}{2}(\hat{\beta}_k + \hat{\beta}_{k+1})\right)$ 
  - Inefficient when the precision of individual variants varies considerably

	$\hat{\beta}_1$	$\hat{\beta}_2$	$\hat{\beta}_3$	$\hat{\beta}_4$	$\hat{\beta}_5$	$\hat{\beta}_6$	$\hat{\beta}_7$	$\hat{\beta}_8$	$\hat{\beta}_9$	$\hat{\beta}_{10}$
Simple median										
Weight ( $1/v_k$ )	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$
Percentile ( $p_k$ )	5	15	25	35	45	55	65	75	85	95
<b>Weighting 1</b>										
Weight ( $1/v_k$ )	$\frac{1}{30}$	$\frac{2}{30}$	$\frac{3}{30}$	$\frac{4}{30}$	$\frac{5}{30}$	$\frac{5}{30}$	$\frac{4}{30}$	$\frac{3}{30}$	$\frac{2}{30}$	$\frac{1}{30}$
Percentile	1.67	6.67	15.00	26.67	41.67	58.33	73.33	85.00	93.33	98.33
<b>Weighting 2</b>										
Weight ( $1/v_k$ )	$\frac{2}{36}$	$\frac{3}{36}$	$\frac{10}{36}$	$\frac{8}{36}$	$\frac{5}{36}$	$\frac{3}{36}$	$\frac{2}{36}$	$\frac{1}{36}$	$\frac{1}{36}$	$\frac{1}{36}$
Percentile ( $p_k$ )	2.78	9.72	27.78	52.78	70.83	81.94	88.89	93.06	95.83	98.61

$$\hat{\beta}_{\text{simple median}} = \frac{\hat{\beta}_5 + \hat{\beta}_6}{2}$$



# Median based methods

## Weighted median estimator

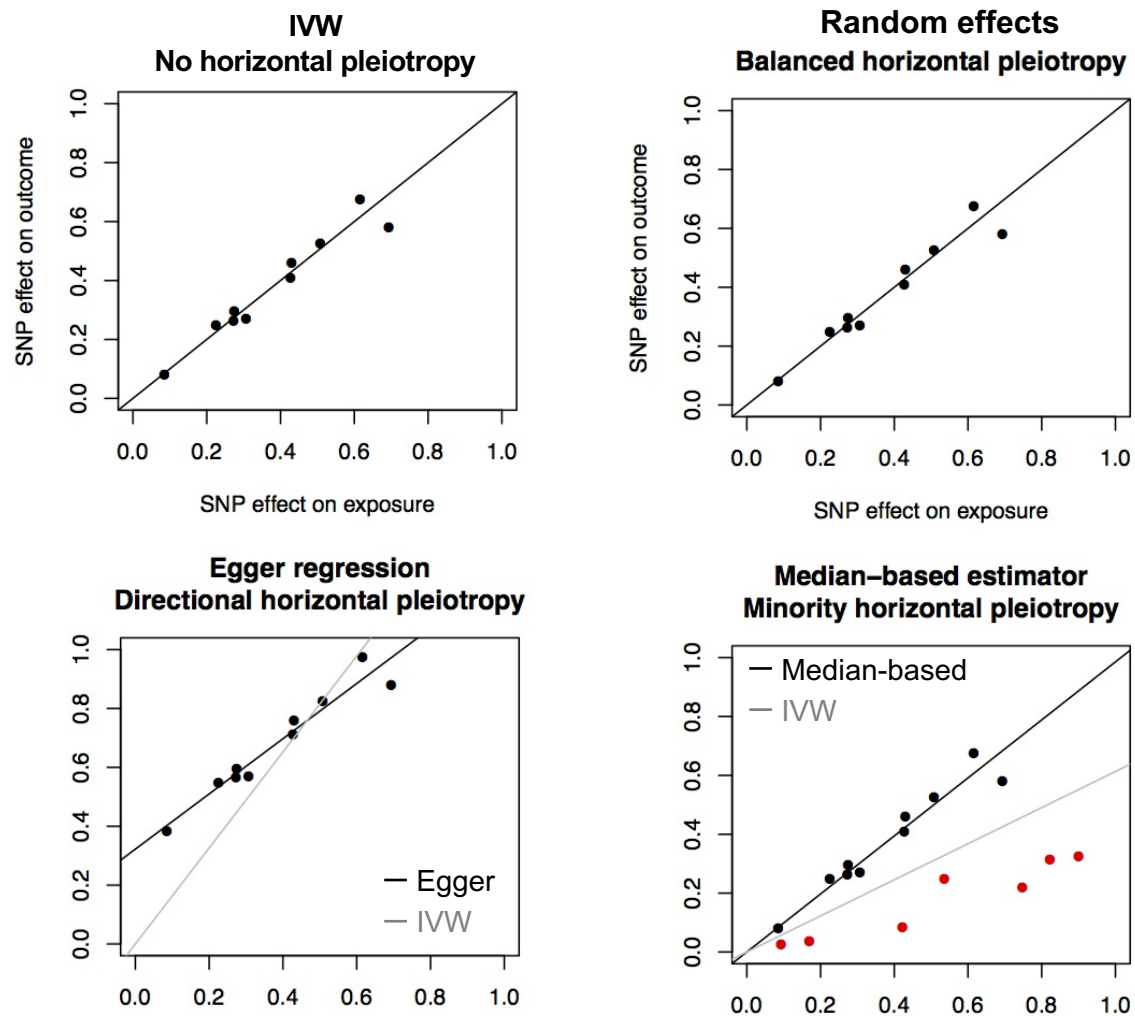
- Weighted median estimator takes into account the differing precisions
- Weighted median:  $\hat{\beta}_{WM} = \hat{\beta}_3 + (\hat{\beta}_4 - \hat{\beta}_3) \times \frac{50 - 27.78}{52.78 - 27.78}$
- Suggested weights: inversed variance of the ratio estimate:  $w'_k = \frac{1}{var(\hat{\beta}_{XY_k})}$

	$\hat{\beta}_1$	$\hat{\beta}_2$	$\hat{\beta}_3$	$\hat{\beta}_4$	$\hat{\beta}_5$	$\hat{\beta}_6$	$\hat{\beta}_7$	$\hat{\beta}_8$	$\hat{\beta}_9$	$\hat{\beta}_{10}$
Simple median										
Weight ( $1/v_k$ )	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$
Percentile ( $p_k$ )	5	15	25	35	45	55	65	75	85	95
<b>Weighting 1</b>										
Weight ( $1/v_k$ )	$\frac{1}{30}$	$\frac{2}{30}$	$\frac{3}{30}$	$\frac{4}{30}$	$\frac{5}{30}$	$\frac{5}{30}$	$\frac{4}{30}$	$\frac{3}{30}$	$\frac{2}{30}$	$\frac{1}{30}$
Percentile	1.67	6.67	15.00	26.67	41.67	58.33	73.33	85.00	93.33	98.33
<b>Weighting 2</b>										
Weight ( $1/v_k$ )	$\frac{2}{36}$	$\frac{3}{36}$	$\frac{10}{36}$	$\frac{8}{36}$	$\frac{5}{36}$	$\frac{3}{36}$	$\frac{2}{36}$	$\frac{1}{36}$	$\frac{1}{36}$	$\frac{1}{36}$
Percentile ( $p_k$ )	2.78	9.72	27.78	52.78	70.83	81.94	88.89	93.06	95.83	98.61

$$\hat{\beta}_{WM} = \hat{\beta}_5 + (\hat{\beta}_6 - \hat{\beta}_5) \times \frac{50 - 41.67}{58.33 - 41.67}$$

$$\hat{\beta}_{WM} = \hat{\beta}_3 + (\hat{\beta}_4 - \hat{\beta}_3) \times \frac{50 - 27.78}{52.78 - 27.78}$$

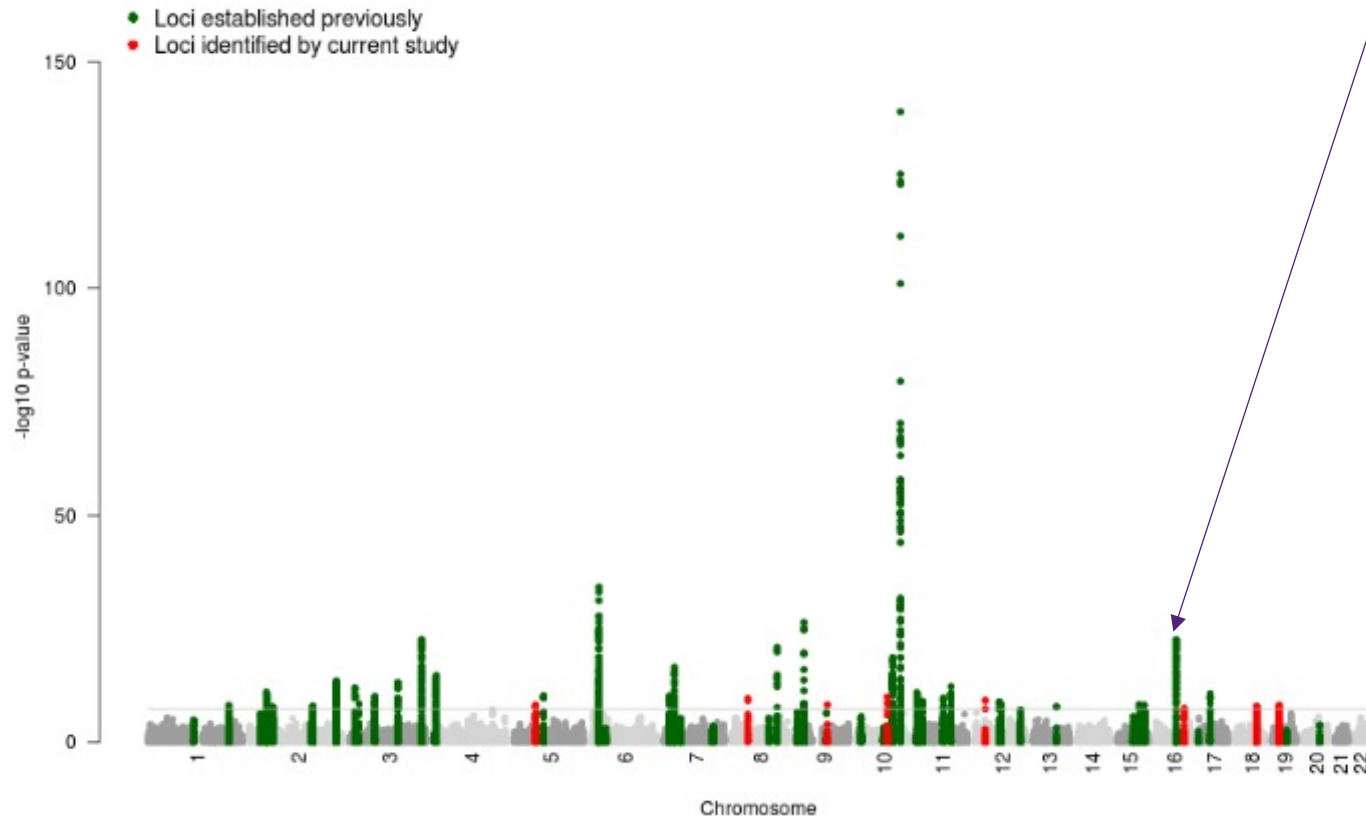
# Summary of robust estimators



● SNPs associated with outcome via an independent pathway.

# Reverse causal instruments

## Problem: MR of type 2 diabetes on BMI



GWAS of T2D reveals *FTO* variant  
 - Famously associated with BMI  
 - A reverse causal instrument?

$FTO \longrightarrow T2D \longrightarrow BMI$

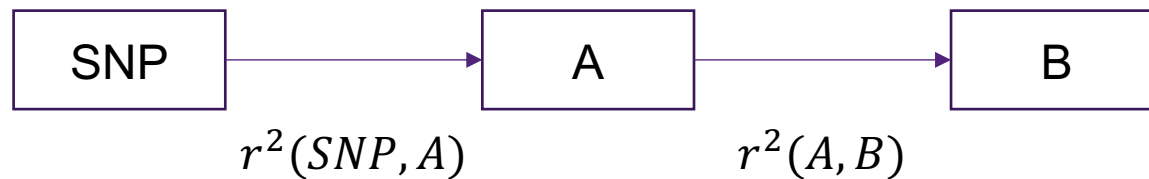
$T2D \longleftarrow BMI \longleftarrow FTO$

*FTO* may be associated with T2D through its effect on BMI  
 >> Not a good instrument for T2D

# Can we avoid including reverse-causal SNPs as instruments?

## Steiger filtering test

- If SNP causes A and A causes B
- The effect of SNP on A should be larger than the effect of SNP on B



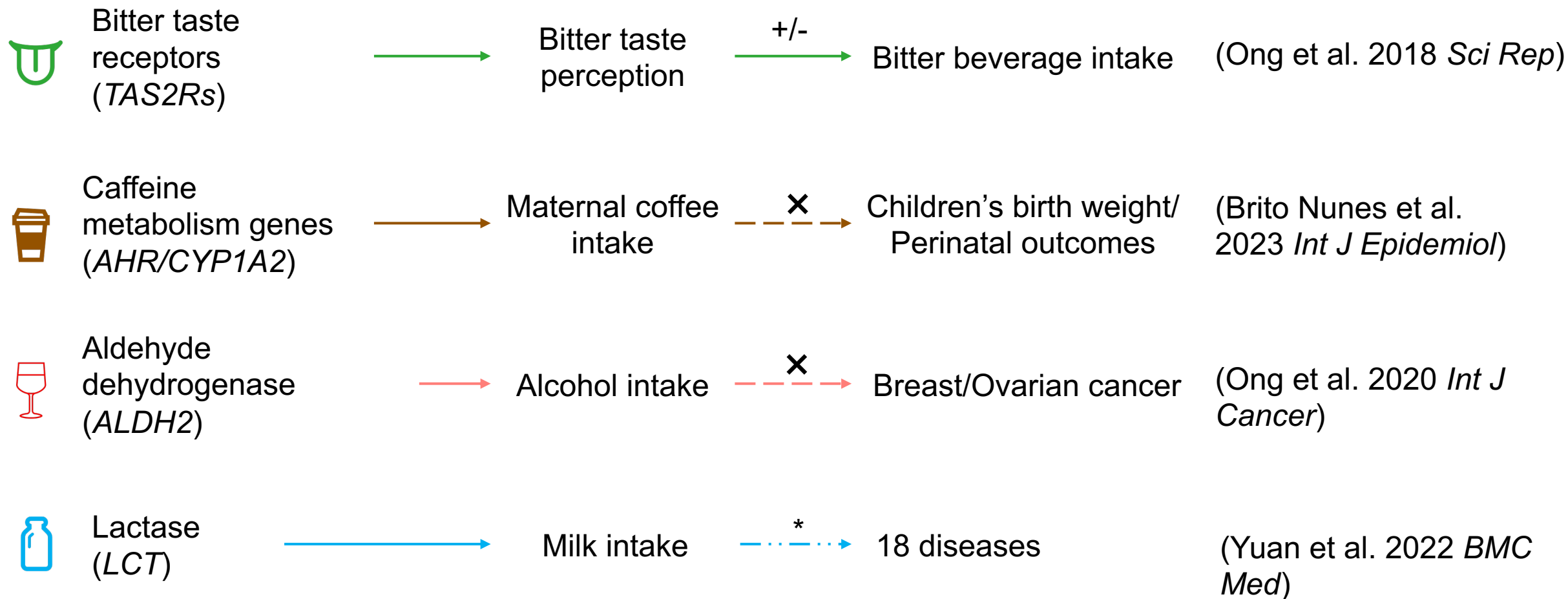
Expect that

$$r^2(SNP, B) = r^2(SNP, A) \times \underbrace{r^2(A, B)}$$

This term is <1

- Steiger test used to evaluate if  $r^2(SNP, A) > r^2(SNP, B)$
- If this is not satisfied, infer that this instrument is not influencing the exposure primarily.

# Ideal instruments are genetic variants with a known biological function related to the exposure



# TwoSampleMR R Package

TwoSampleMR 0.6.4 Guide ▾ Functions Changelog

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Source

## Mendelian randomization with GWAS summary data

A package for performing Mendelian randomization using GWAS summary data. It uses the [IEU GWAS database](#) to obtain data automatically, and a wide range of methods to run the analysis. You can use the [MR-Base web app](#) to try out a limited range of the functionality in this package, but for any serious work we strongly recommend using this R package.

### January 2020 major update

**We have made substantial changes to the package, database and reference panels.** For full details of the changes, please visit <https://mrcieu.github.io/TwoSampleMR/articles/gwas2020.html>

### Installation

Users running Windows and macOS, to install the latest version of TwoSampleMR please install from our MRC IEU r-universe

```
install.packages("TwoSampleMR", repos = c("https://mrcieu.r-universe.dev", "https://cloud.r-project.org"))
```

Users running Linux or WebR please see the [following instructions](#).

To update the package run the same command again.

### Installing from source

```
install.packages("remotes")
remotes::install_github("MRCIEU/TwoSampleMR")
```

To update the package just run the `remotes::install_github("MRCIEU/TwoSampleMR")` command again.

### Docker

A docker image containing R with the TwoSampleMR package pre-installed is available here: <https://hub.docker.com/r/mrcieu/twosamplemr>

#### Links

[Browse source code](#)

[Report a bug](#)

#### License

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#### Citation

[Citing TwoSampleMR](#)

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#### Dev status

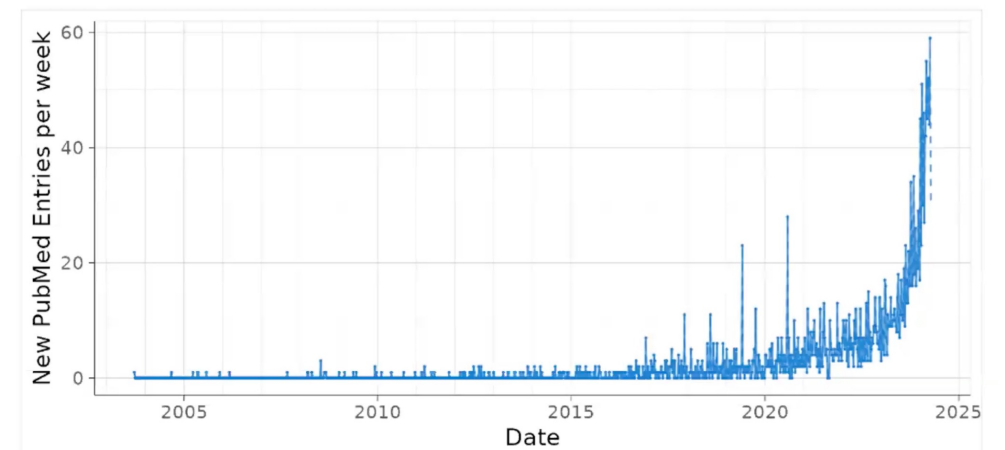
 R-CMD-check passing

 lifecycle experimental


DOI [10.5281/zenodo.10684540](https://doi.org/10.5281/zenodo.10684540)

 codecov 36%

 r-universe 0.6.4



# STROBE-MR



**STROBE-MR**  
Transparent reporting of Mendelian randomization studies

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## Welcome to the STROBE-MR website!

**About:** STROBE-MR stands for “Strengthening the Reporting of Observational Studies in Epidemiology using Mendelian Randomization”. Inspired by the original STROBE checklist, the STROBE-MR guidelines were developed to assist researchers in reporting their Mendelian randomization studies clearly and transparently. Adopting STROBE-MR should help readers, reviewers, and journal editors evaluate the quality of published MR studies.

The STROBE-MR **checklist** contains 20 items recommended to address in reports of Mendelian randomization studies.

The **Statement** document describes the process of developing the checklist and the complementary Explanation and Elaborations document.

The **Explanation and Elaboration** document explains the items of the STROBE-MR checklist, along with their rationale and examples of transparent reporting.

All documents and publications produced by the STROBE-MR Initiative are open-access and available for download on this website.


# MR Dictionary



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**The definitive list of terms for Mendelian randomization research**

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# Summary

- MR uses natural randomization to mimic an RCT
- It is useful, data is abundant, but it is not a panacea for causal inference
- Often valuable for proving that a hypothesized association is not causal
- Horizontal pleiotropy is one of the main threats to the validity of MR studies
  - Multiple methods developed to detect and adjust for horizontal pleiotropy
- Crucial to perform sensitivity analyses and obtain metrics regarding the likely reliability of the MR estimates
- Consistency of results across methods is key to reliable causal inference

# Additional References

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