

Mendelian Randomization

Daisy Crick

Data Agreement

To maximize your learning experience, we will be working with genuine human genetic data, during this module.

Access to this data requires agreement to the following in to comply with human genetic data ethics regulations

If you haven't done so, please email <ctr-pdg-admin@imb.uq.edu.au> with your name and the below statement to confirm that you agree with the following:

“I agree that access to data is provided for educational purposes only and that I will not make any copy of the data outside the provided computing accounts.”

Learning materials

Instructions to access WiFi/desktop/server:

<https://suave-pillow-de4.notion.site/Instruction-to-Computing-Resources-dcba658c9a584e6d80a443c5d64042d8?pvs=4>

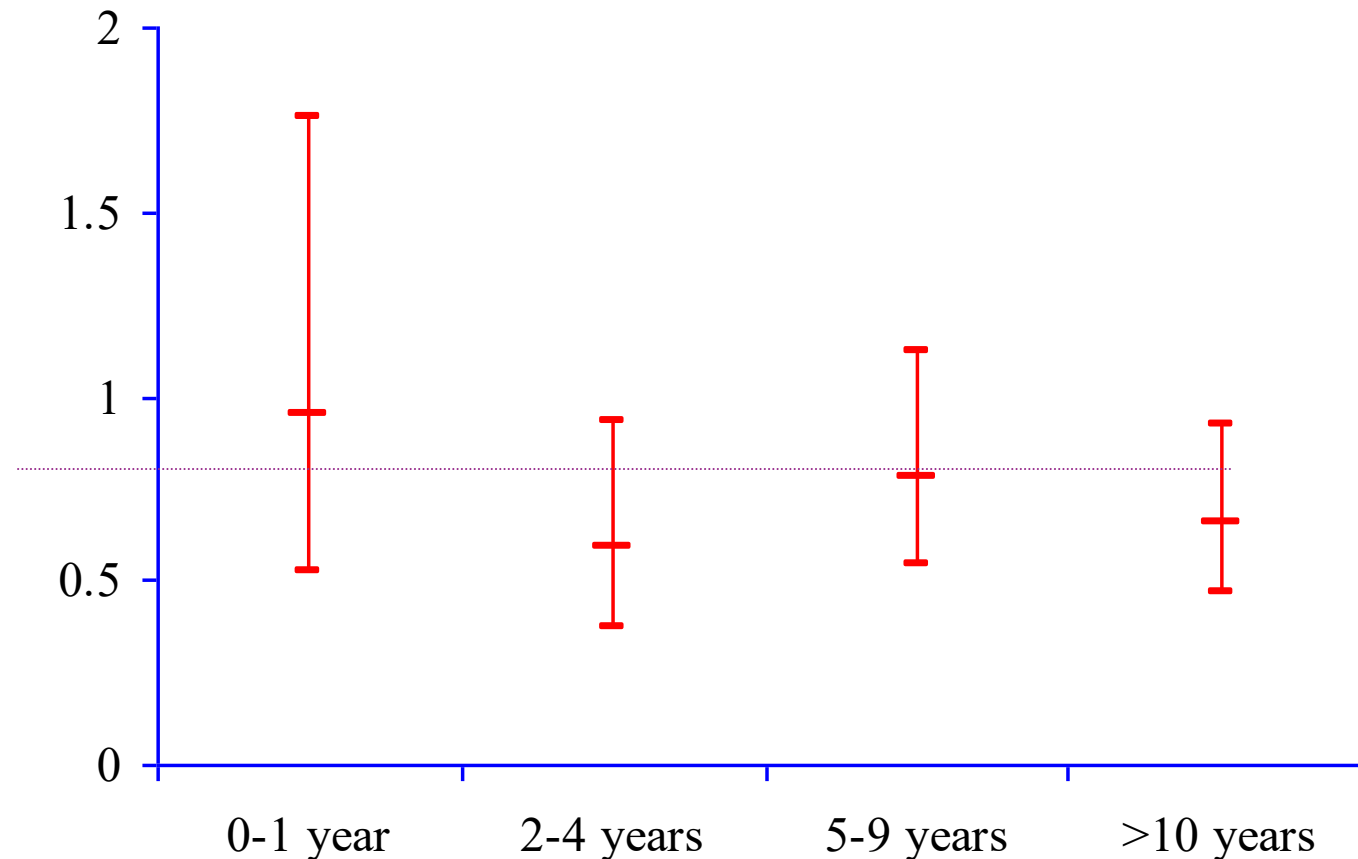
Slides and practical notes:

<https://cnsgenomics.com/data/teaching/GNGWS25/module4>

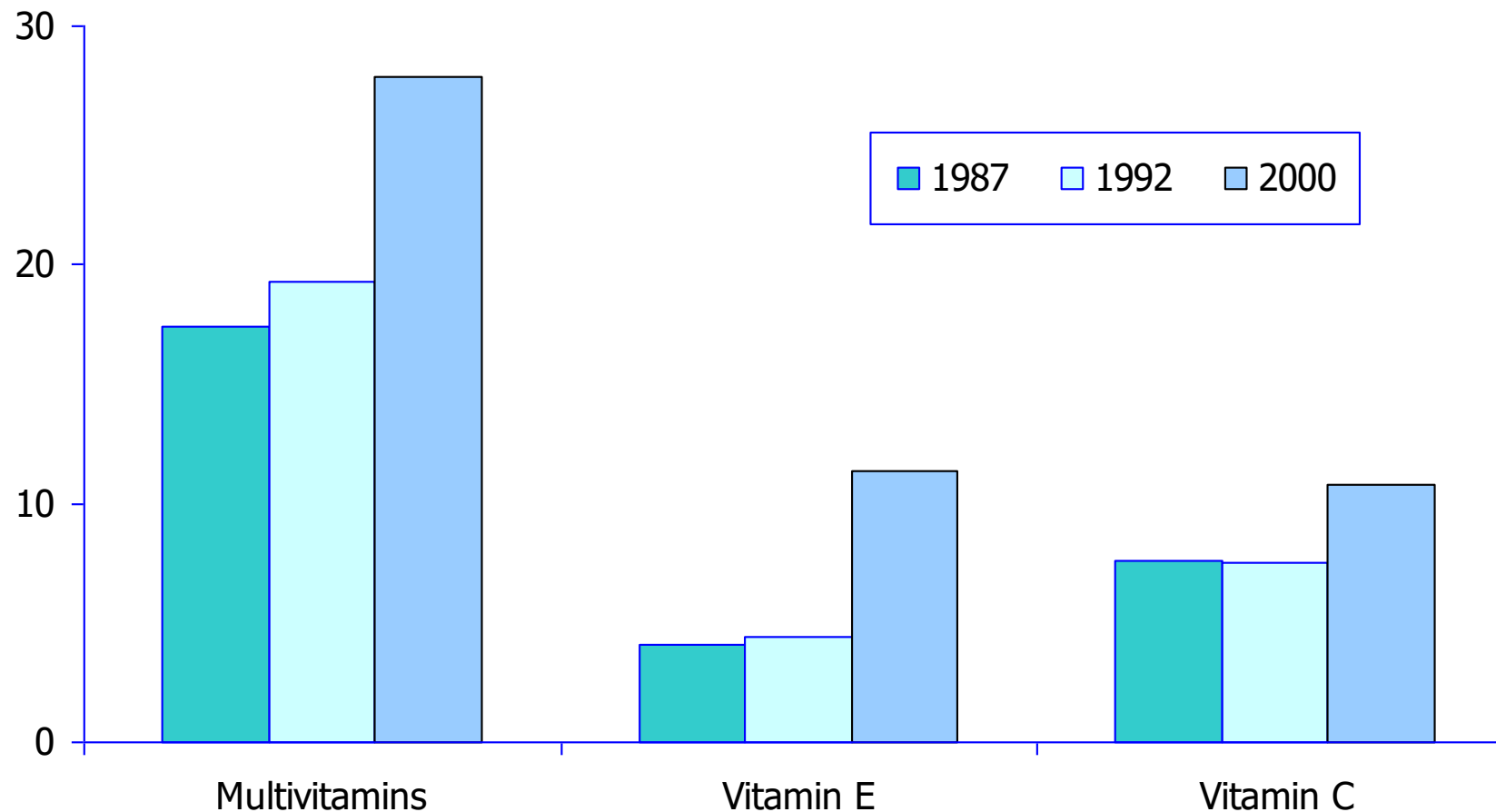
Learning Objectives

- Understand the issues of observational epidemiology.
- Understand how Mendelian randomization (MR) works, what its core assumptions are and how to calculate causal effect estimates.
- Understand what directed acyclic graphs (DAGs) are and how they can be used to inform study design.
- Cover the basic limitations to Mendelian randomization.

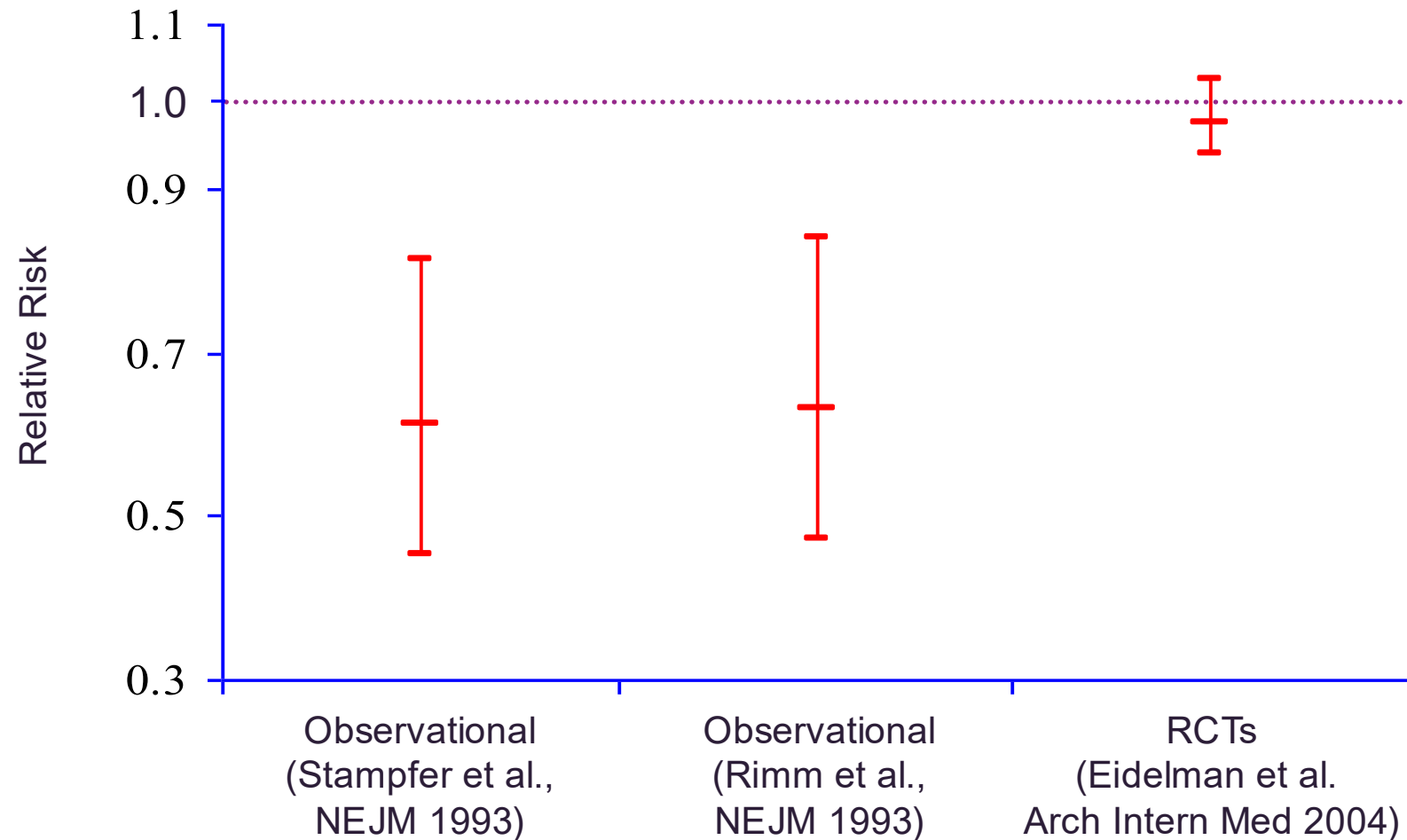
Vitamin E supplement use and risk of Coronary Heart Disease



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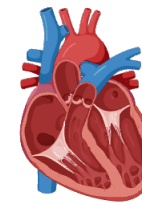


Inferring causality using observational data

- Results from observational studies can give the wrong answer.



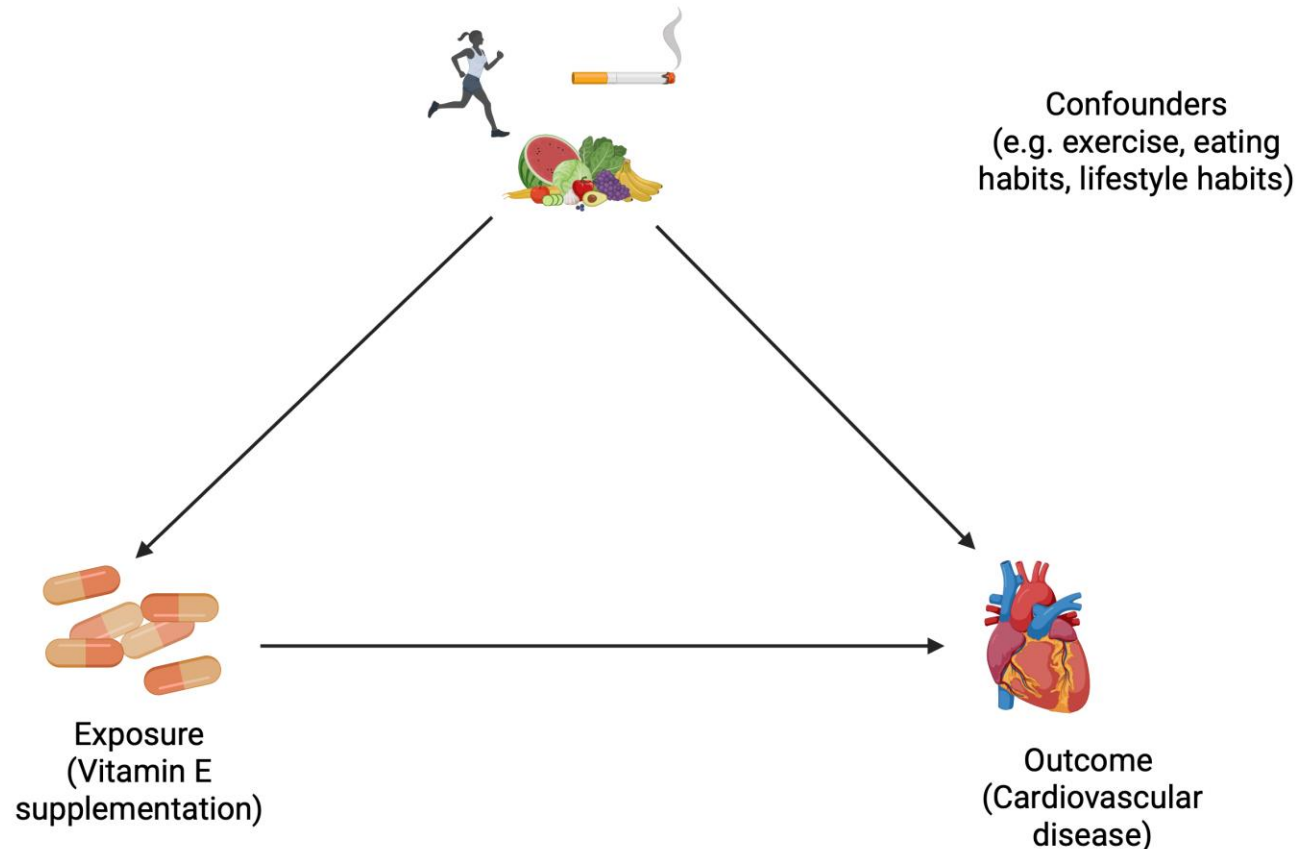
Exposure
(vitamin E)



Outcome
(Cardiovascular
Disease)

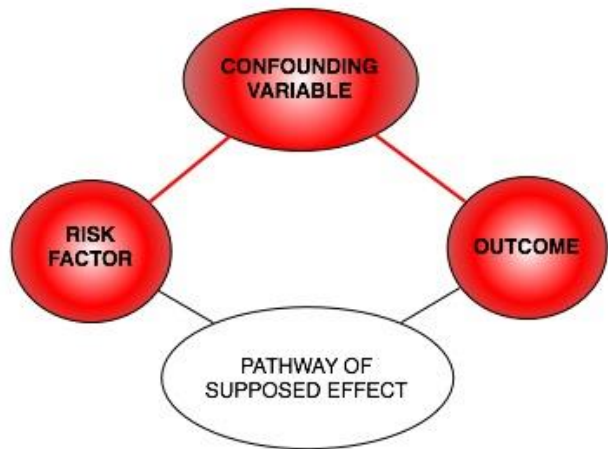
Inferring causality using observational data

- Results from observational studies can give the wrong answer.



Classic limitations to observational science

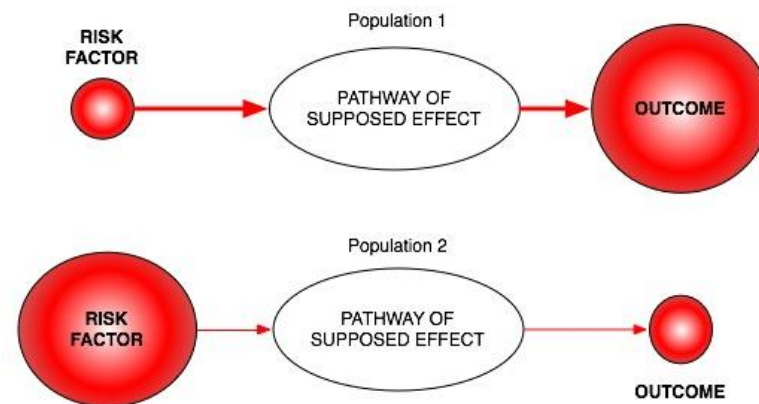
Confounding



Reverse Causation

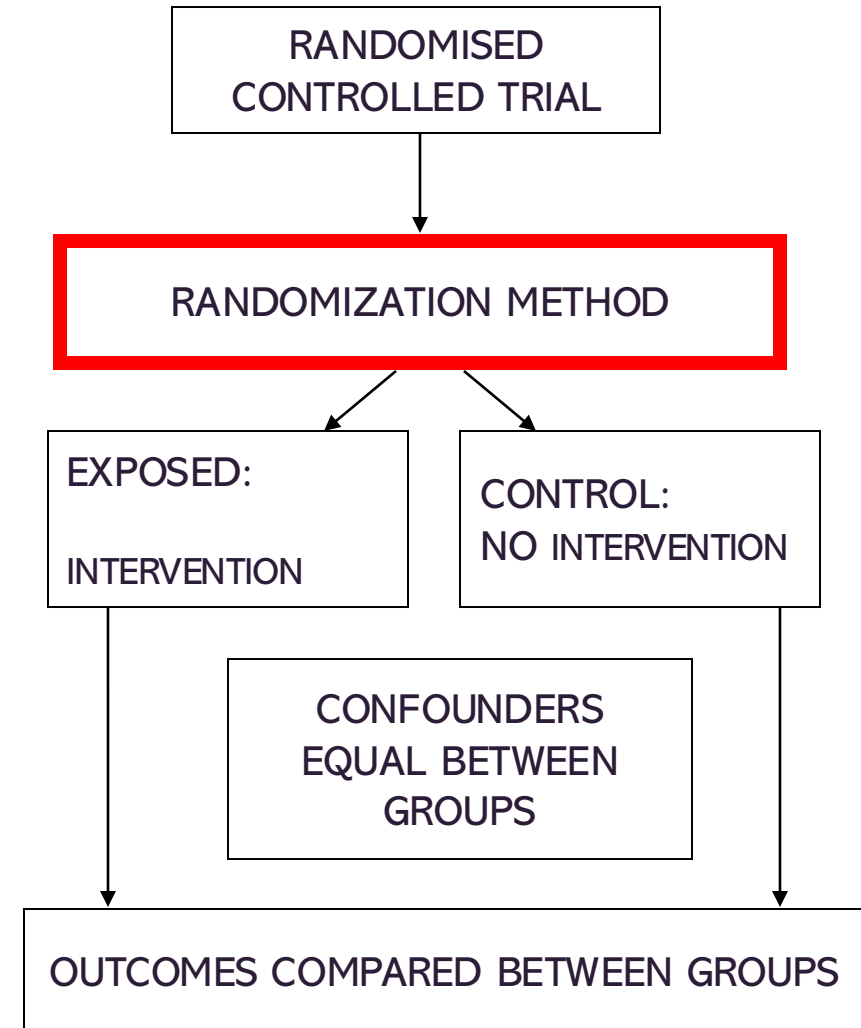


Bias



Randomised Control Trials (RCTs)

- The gold standard in inferring causality!



Mendelian randomization!

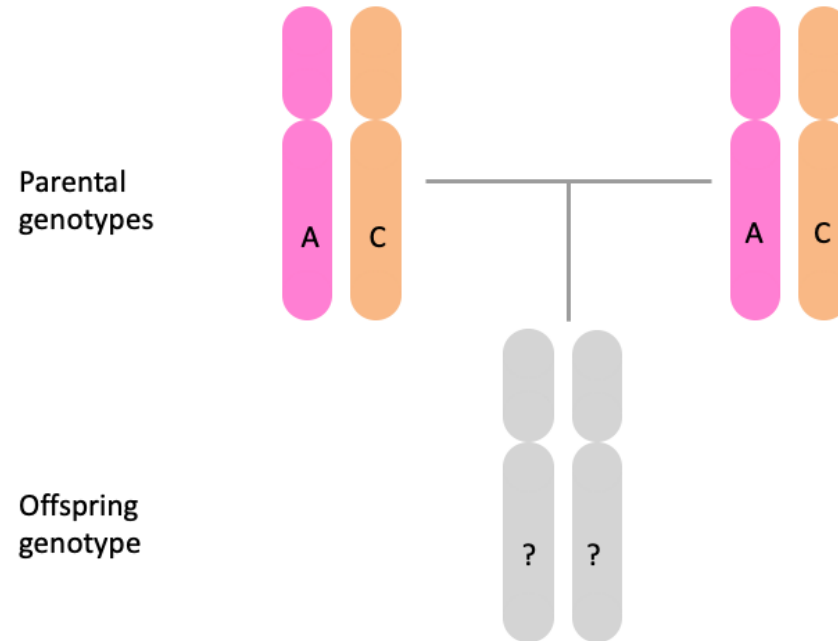
- A technique based on the idea that genetics can tell us about non-genetic factors and their effects on health and disease.
- MR uses genetic information as a proxy for non-genetic information.
- The modifiable exposure on the outcome will be the same whether the exposure is influenced by the environment or genetics.

Mendel's Laws of inheritance



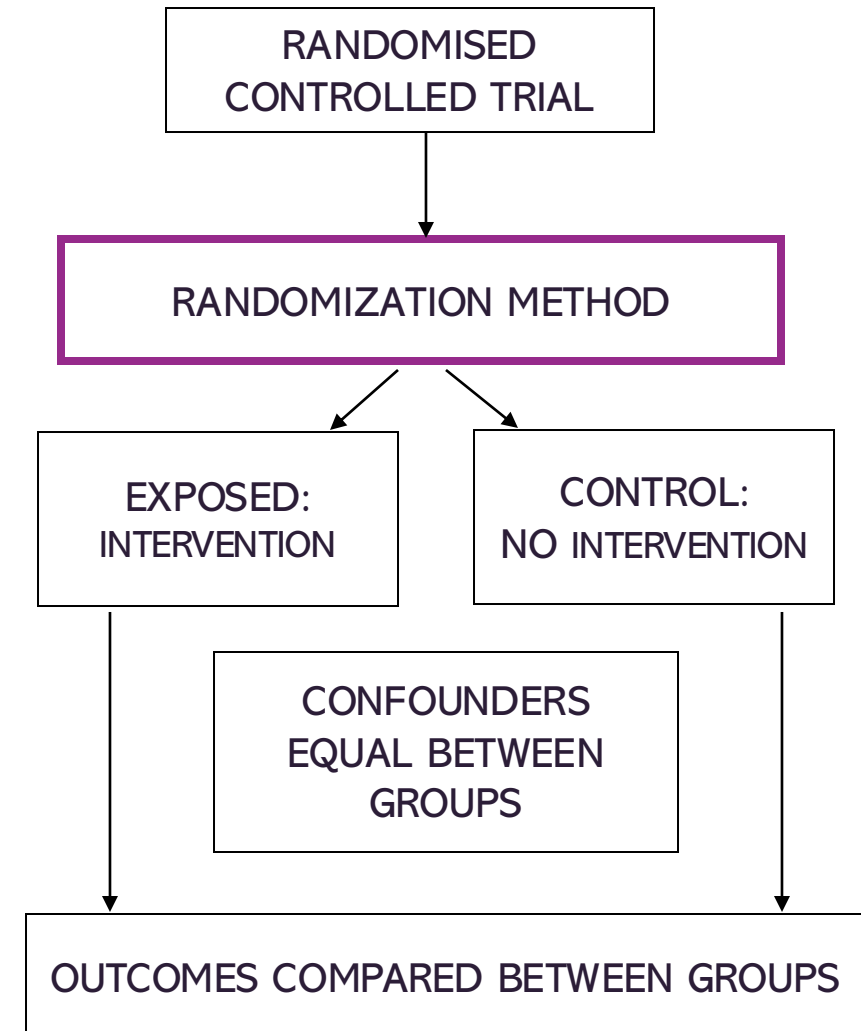
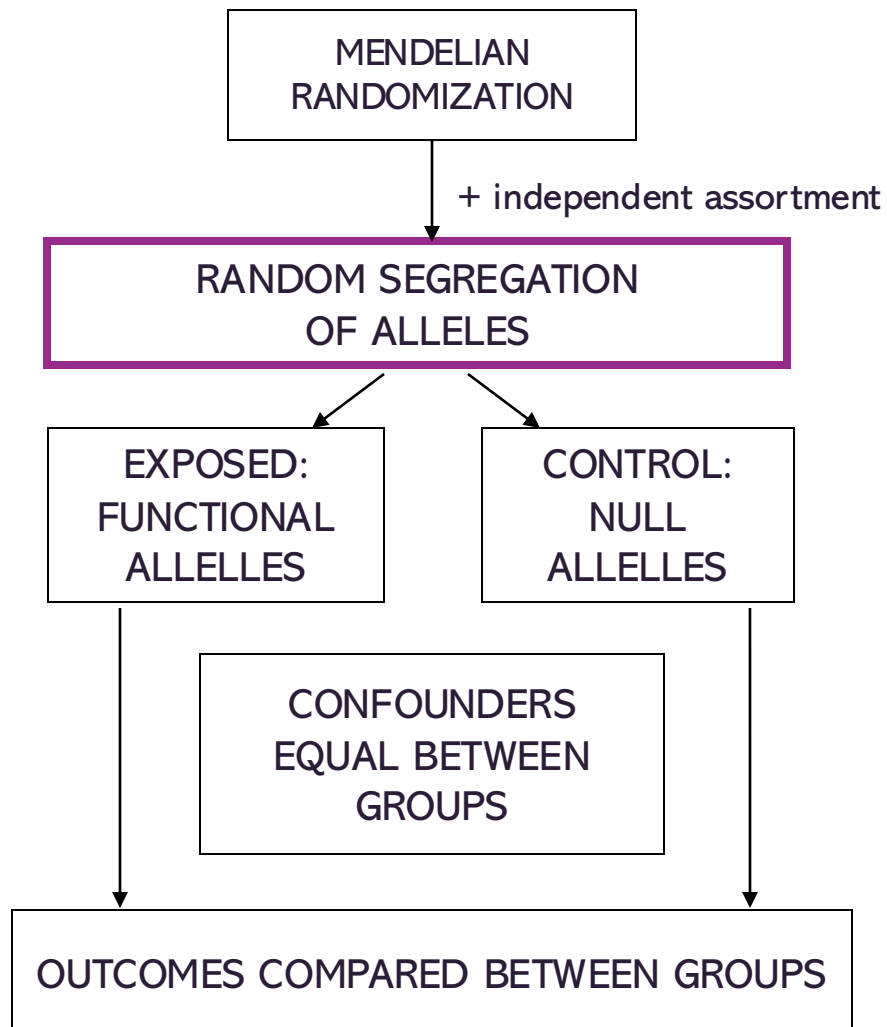
Gregor Mendel in 1862

1. **Segregation:** alleles separate at meiosis and a randomly selected allele is transmitted to offspring.

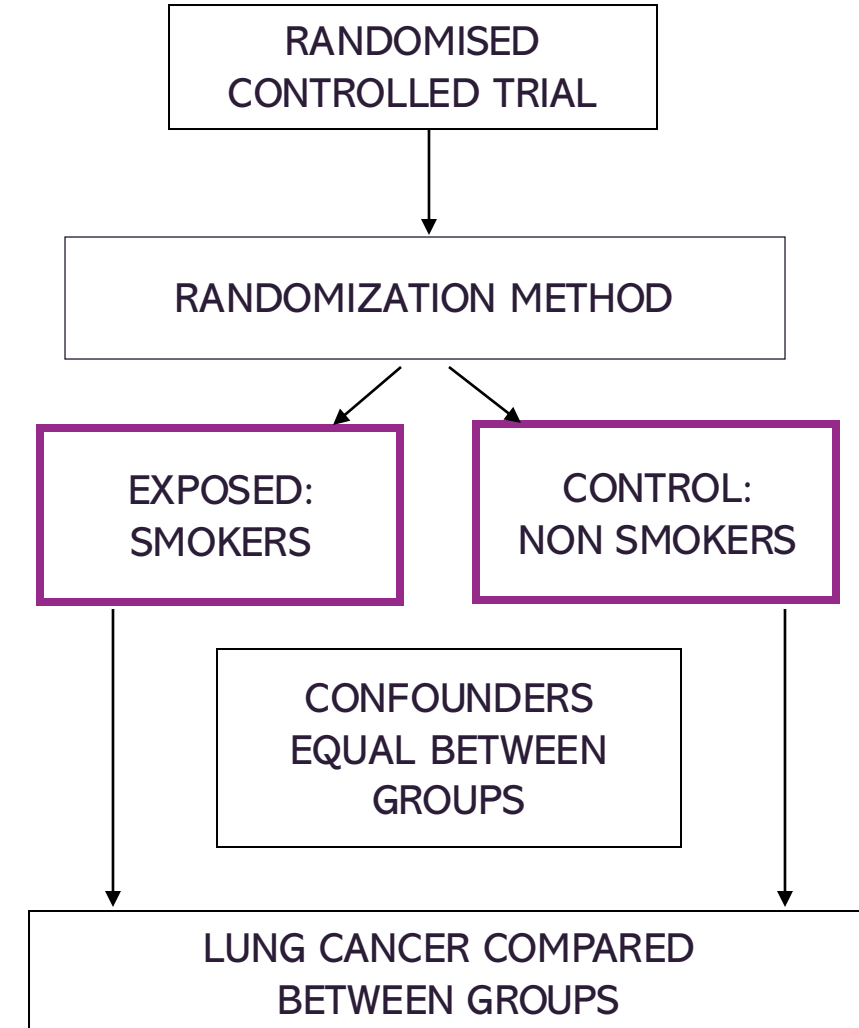
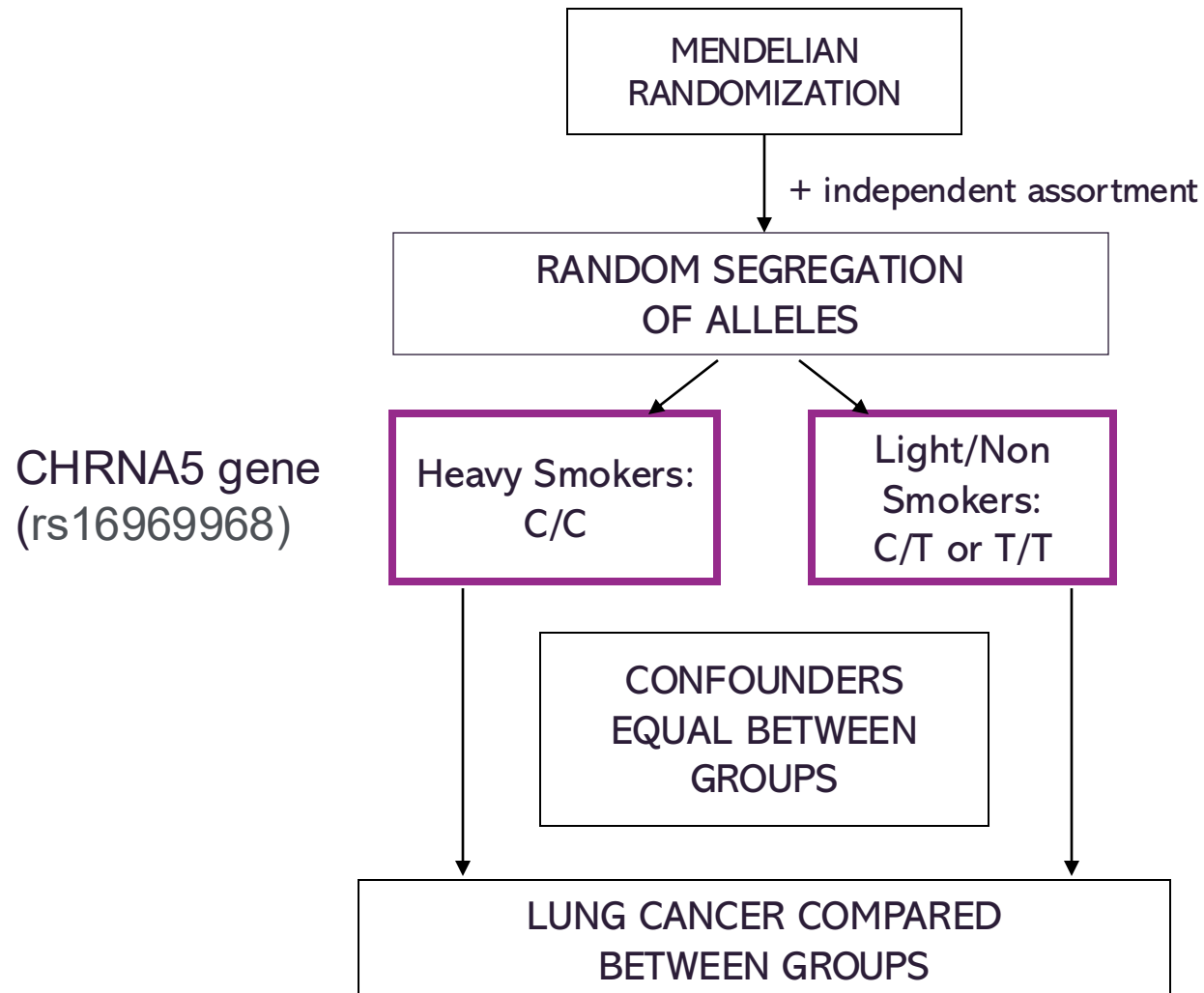


2. **Independent assortment:** alleles at different genetic loci (for different traits) are transmitted independently of one another.

Mendel's Laws of inheritance



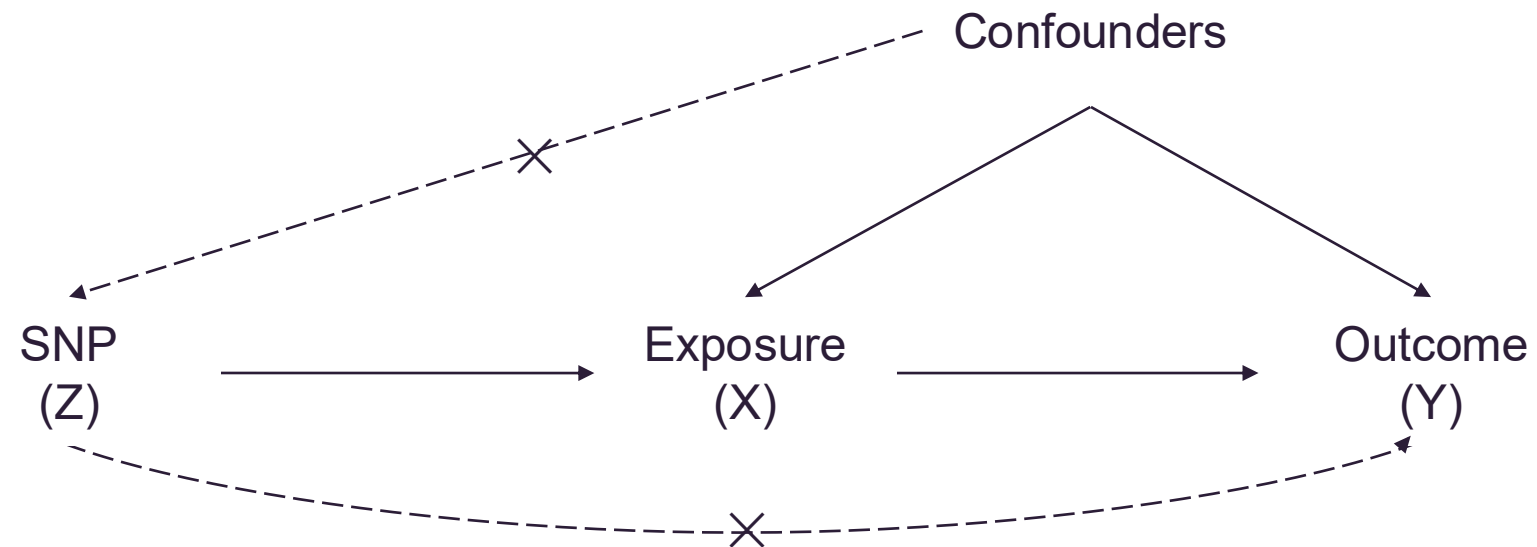
Mendel's Laws of inheritance



What is a DAG

- Directed Acyclic Graph.
- Systematic representation of causal relationships.
- Displays assumptions about the relationship between variables.
- Clarify study design.

What is a DAG



The DAG game

DAG Rules

- They have to be directed.
- They have to be acyclic.
- All common causes must be represented.
- Time flows from left to right.

DAG Rules

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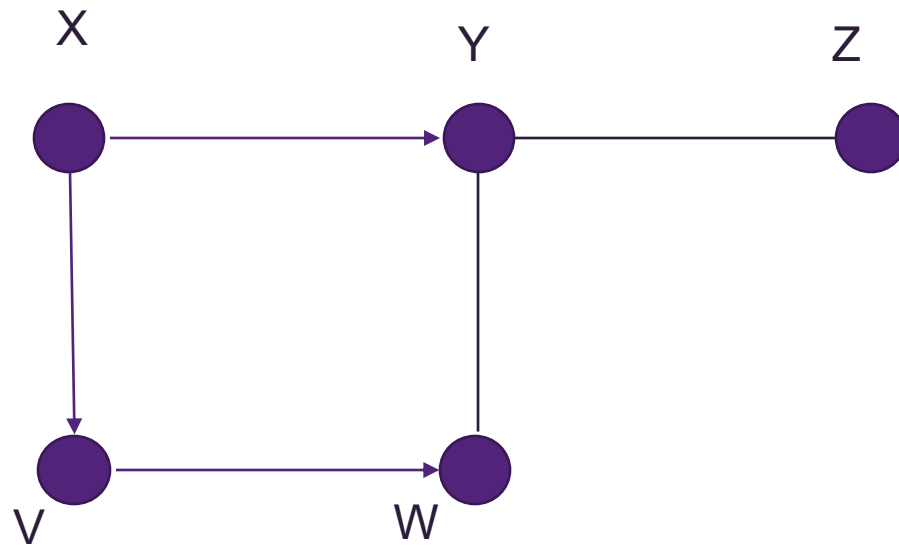
DAG Rules

- They have to be directed.
- They have to be acyclic.
- **Common causes of two variables must be represented.**
- Time flows from left to right.

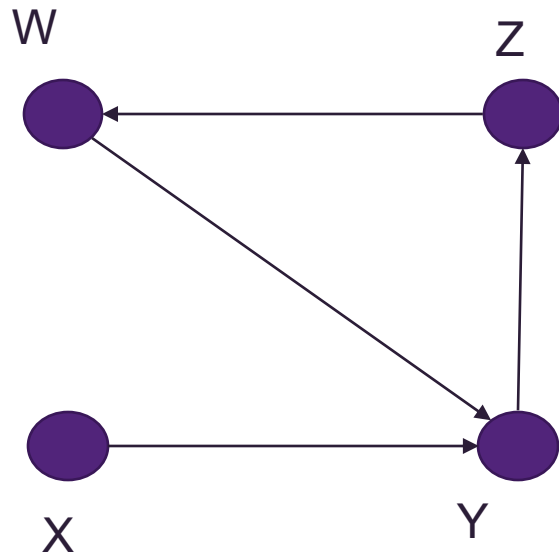
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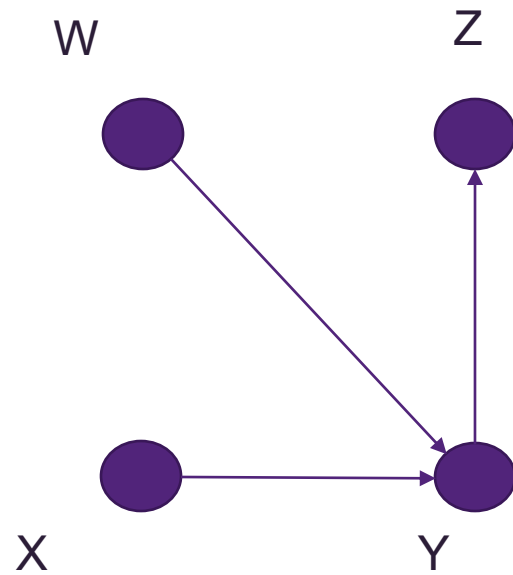
Is it a DAG?



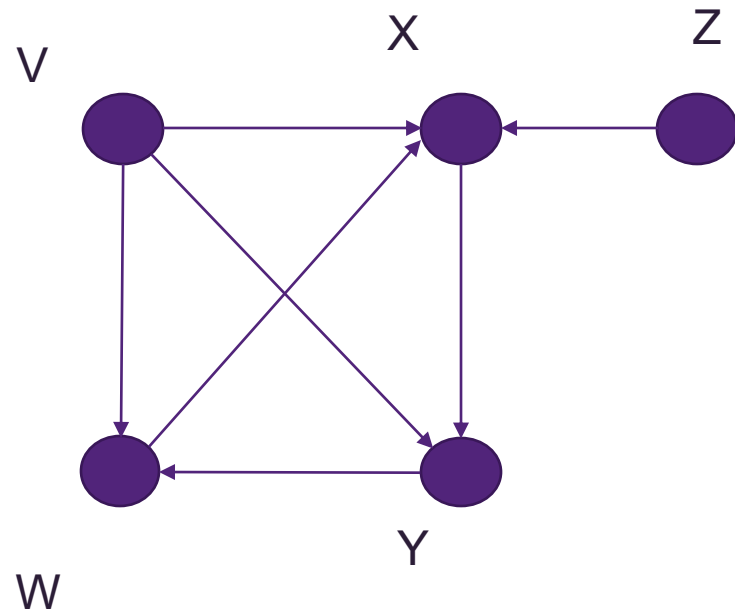
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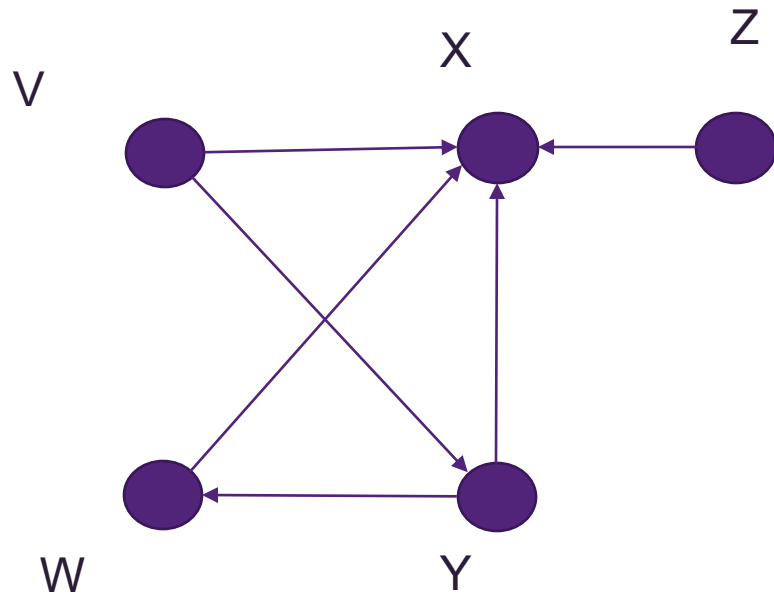
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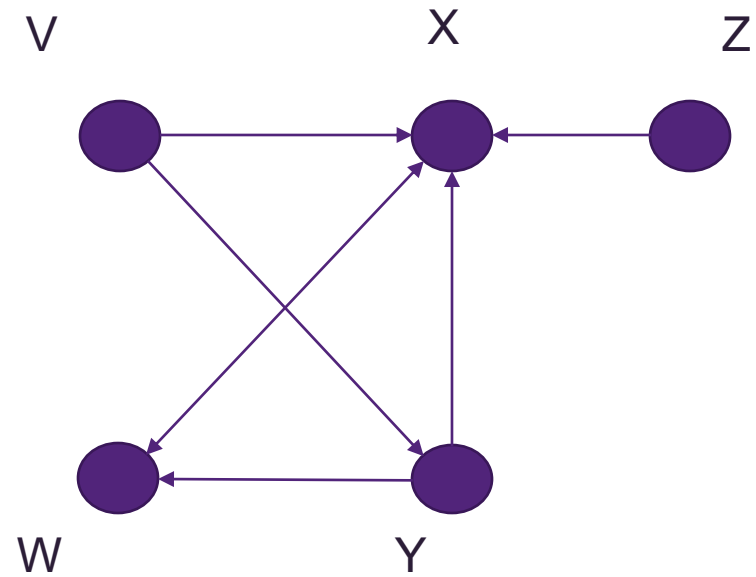
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IS IT A DAG?

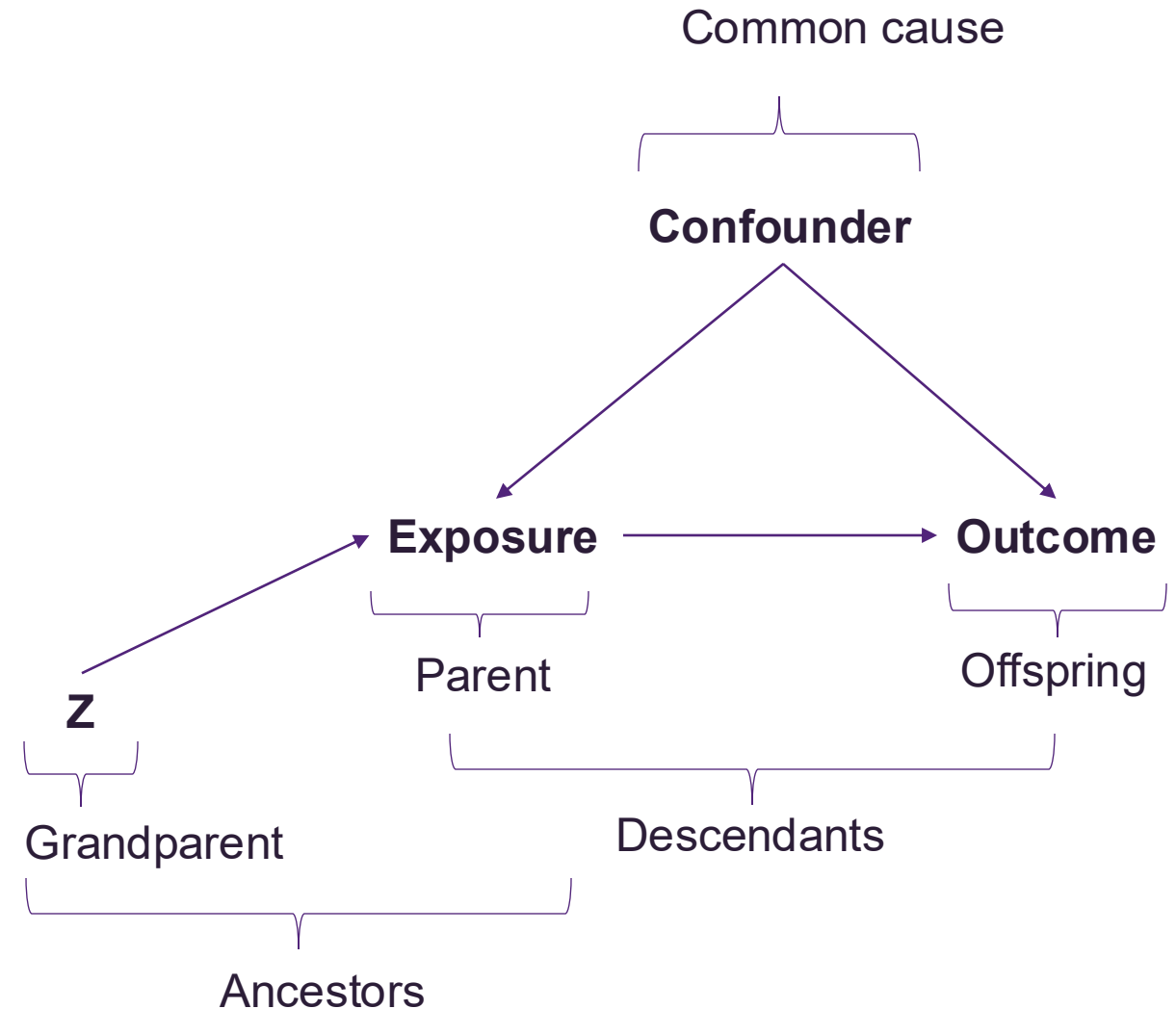


IS IT A DAG?



Glossary

- **Parent:** a direct cause of a particular variable.
- **Ancestor:** a direct cause or indirect cause of a particular variable.
- **Child:** The direct effect of a particular variable.
- **Descendant:** a direct effect or indirect effect of a particular variable.
- **Common cause:** A variable that is an ancestor of two other variables.



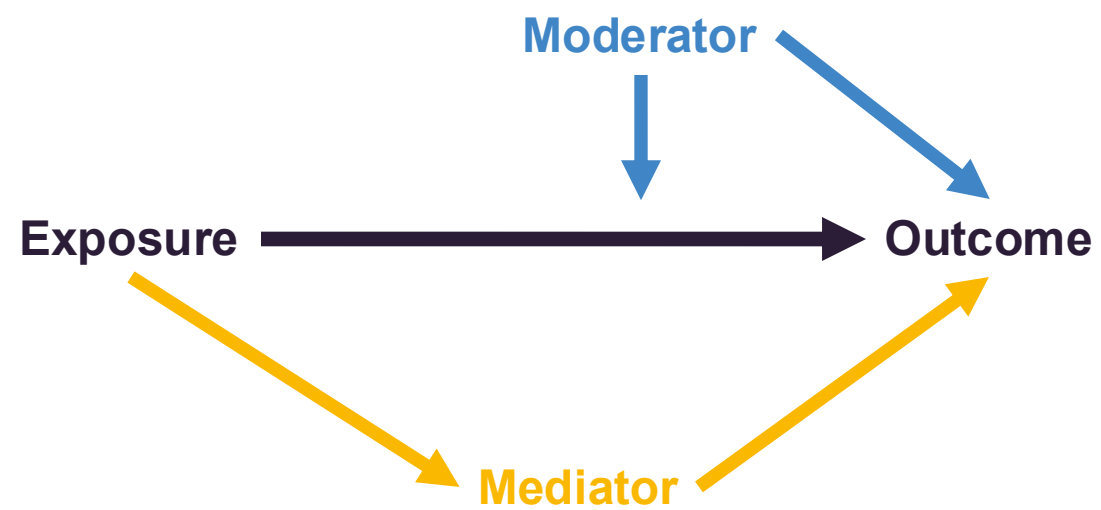
How to construct a DAG

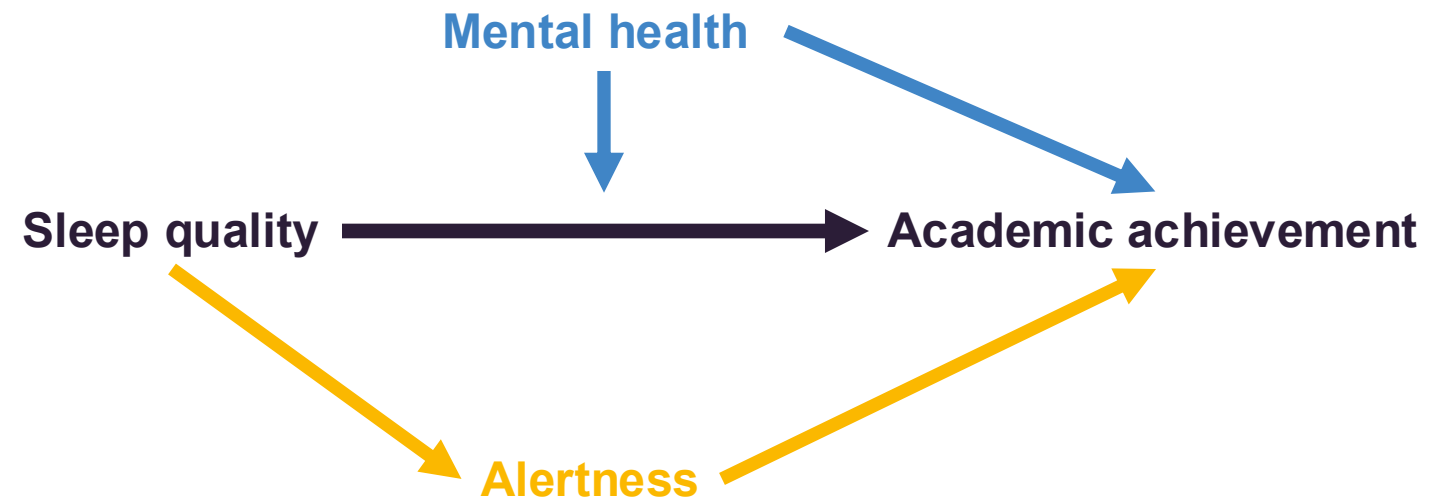
- Start with the exposure/treatment and the outcome/endpoint.

Exposure → Outcome

How to construct a DAG

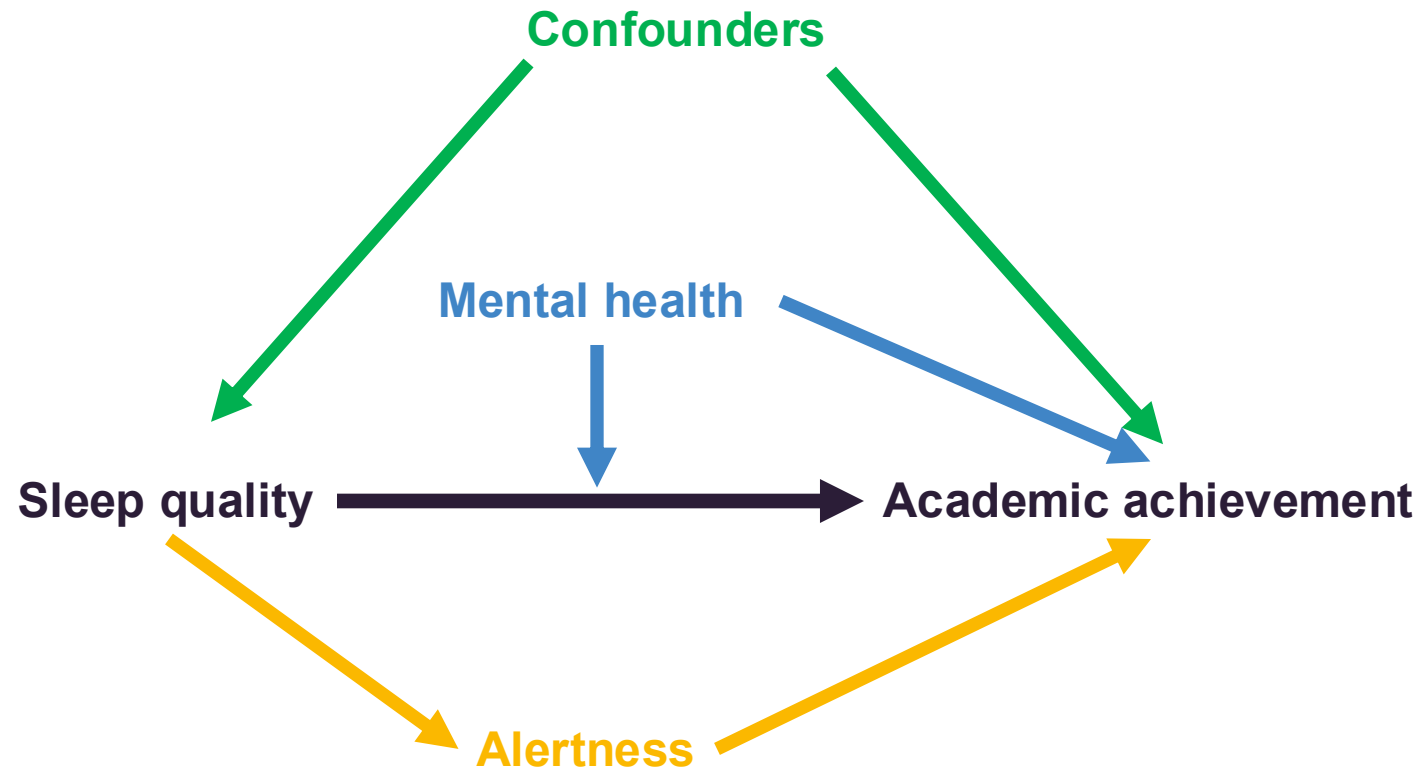
- Start with the exposure/treatment and the outcome/endpoint.
- Consider variables embedded in the question (e.g. mediators/moderators).

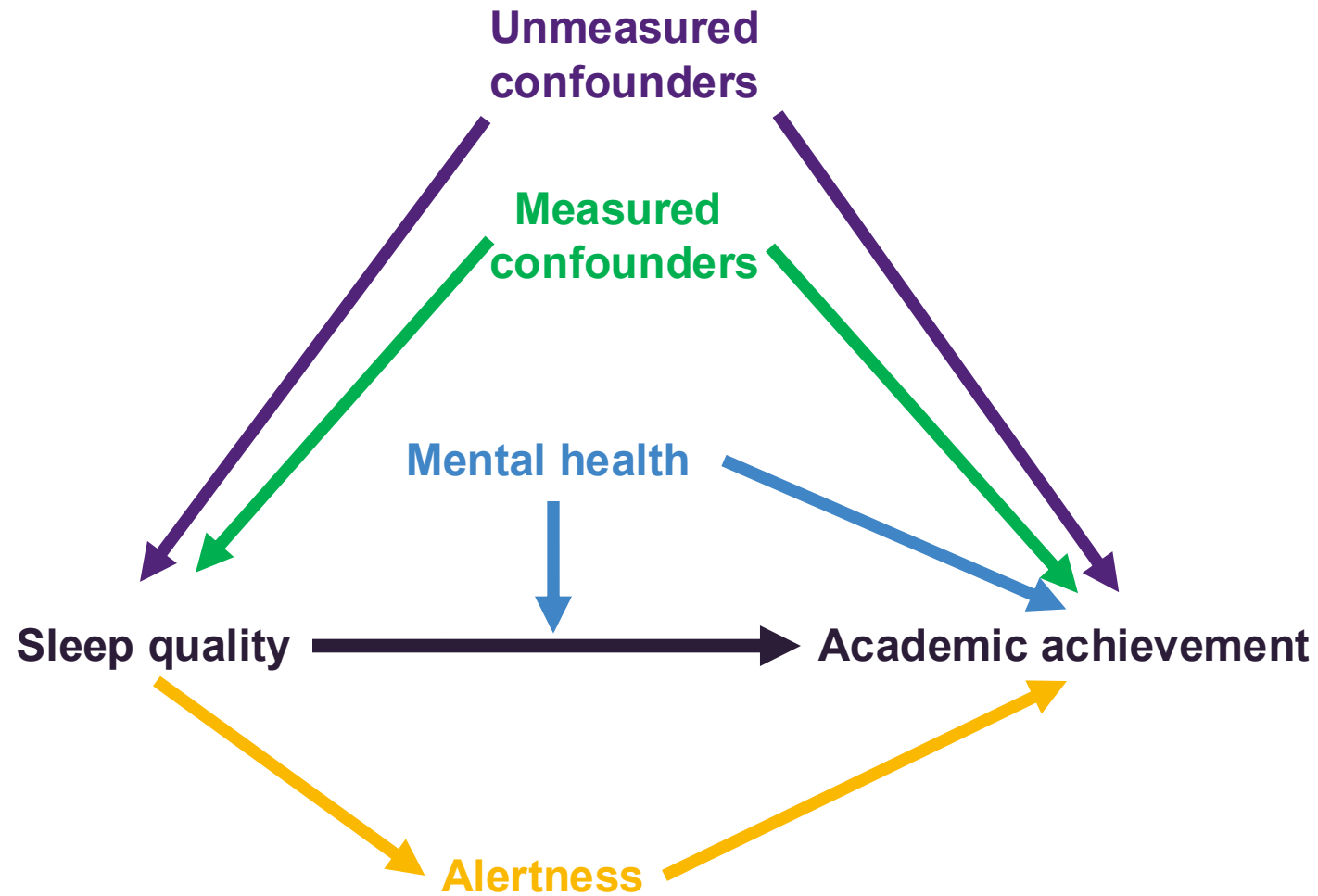




How to construct a DAG

- Start with the exposure/treatment and the outcome/endpoint.
- Consider variables embedded in the question (e.g. mediators/moderators).
- Consider confounding variables and add to the DAG.





How to construct a DAG

| Must be included | Not required |
|--|---|
| All common causes of any 2 variables (confounders) | Variables that cause Y but not A (moderators) |
| Unmeasured and unmeasurable common causes (use U notation) | |
| Selection variables (i.e. inclusion criteria) | |

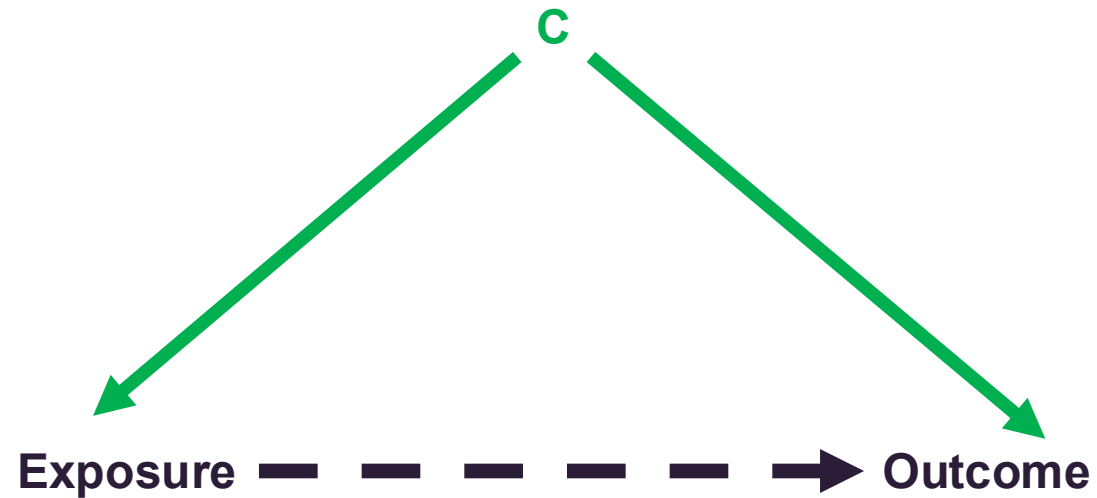
Remember:

- Assumptions must be made.
- There are often more than 1 appropriate DAG
- Alternative DAGs can make excellent sensitivity analyses.

Glossary

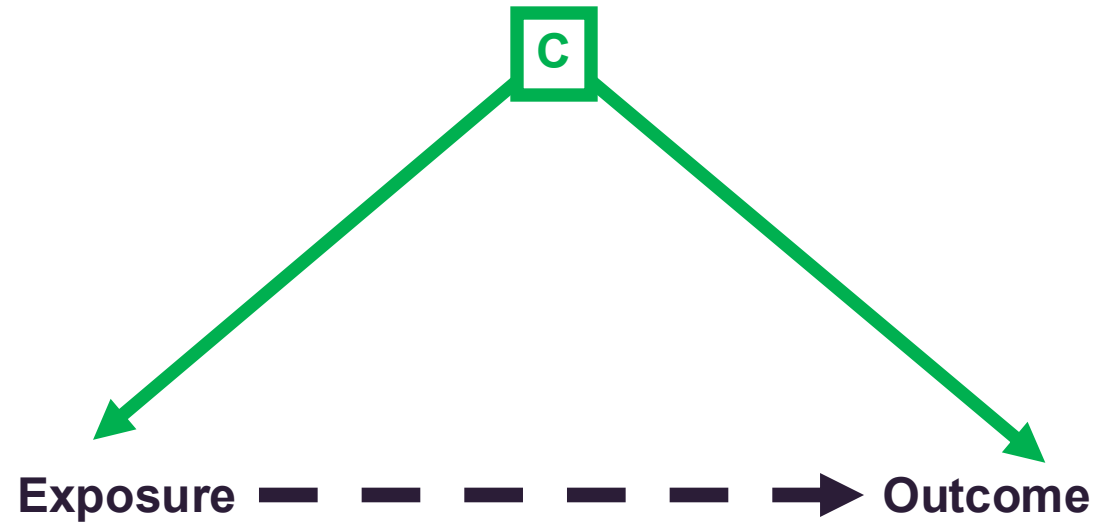
- **Back door path:** A connection between X and Y that does not follow the path of the arrows.
- **Collider:** A variable that is a descendant of two other variable. The term **collider** is used because the arrows “collide” at the descendant node.
- **Conditioning:** Conditioning on a variable means using either sample restriction, stratification, adjustment to examine the association of X and Y.

Back door path



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Back door path



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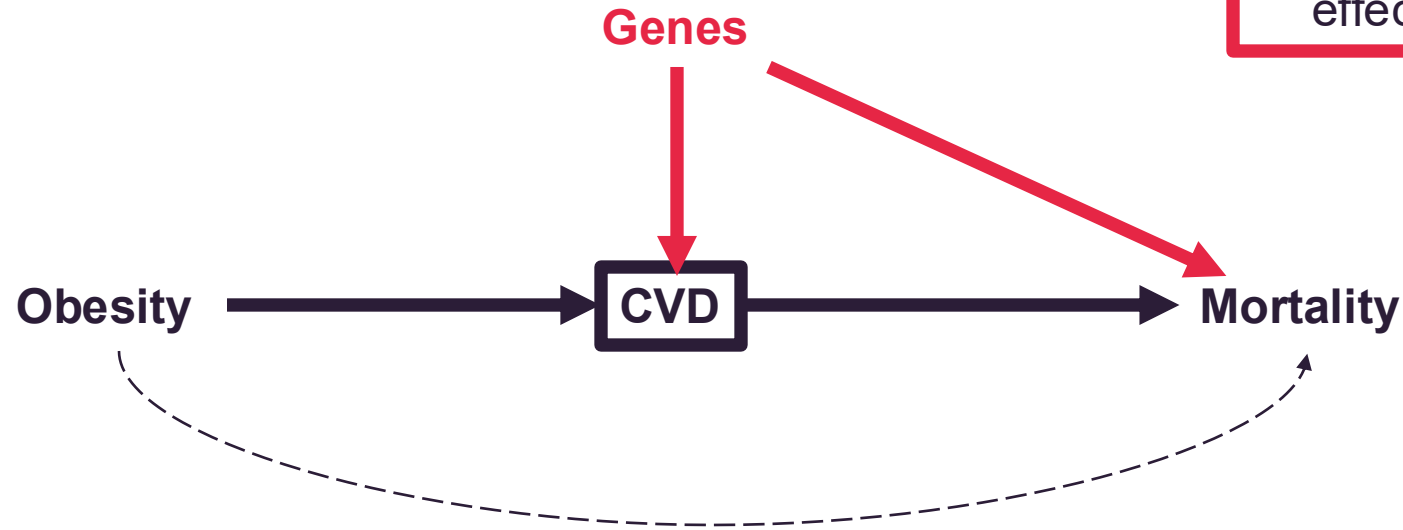
Collider

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- **Collider Bias:** A phenomenon involving conditioning on common effects.

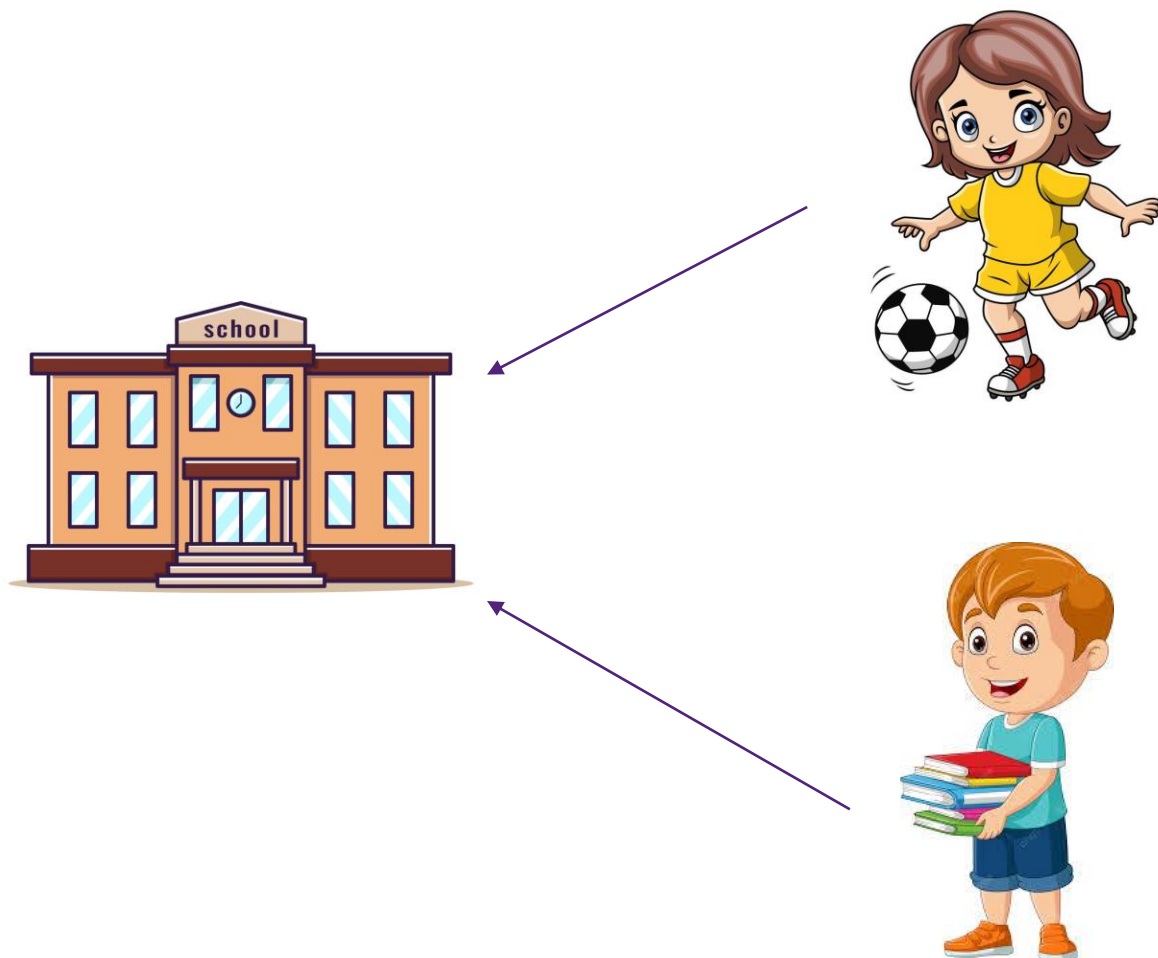


Collider

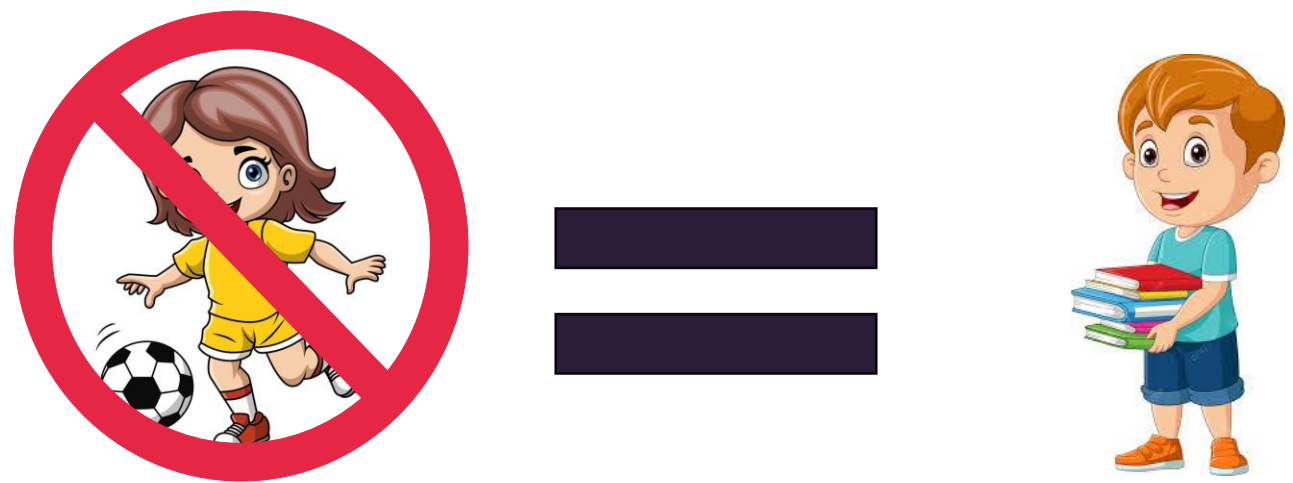
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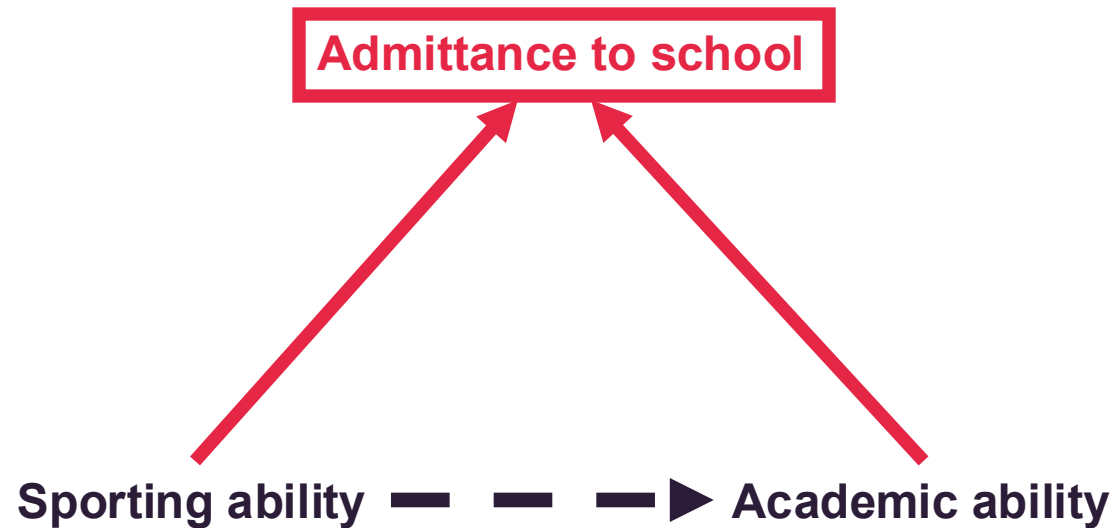
Collider



Collider



Collider



Sporting ability and admittance to the school are dependent

Academic ability and admittance to the school are dependent

Sporting ability and academic ability are independent

BUT

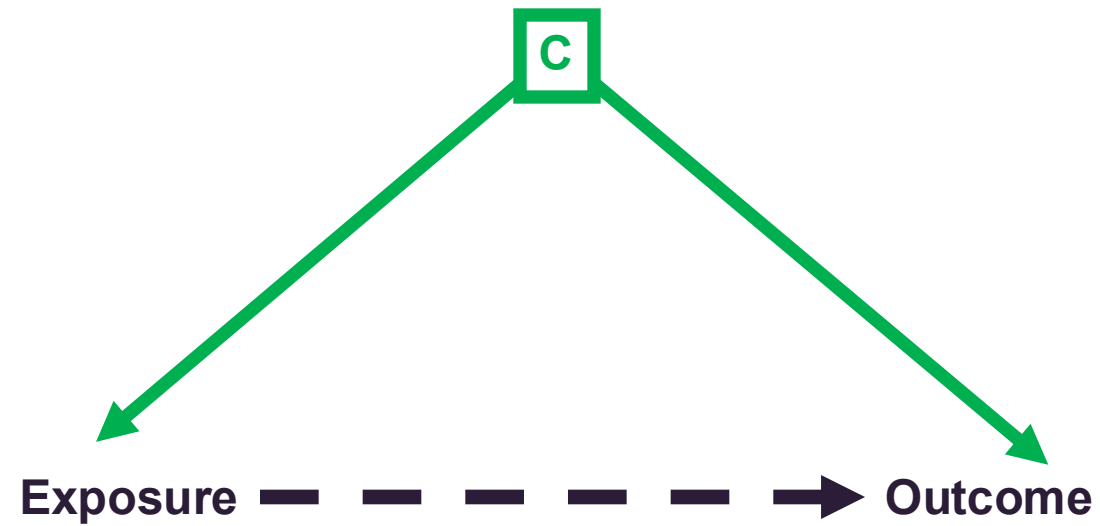
Sporting ability and academic ability are dependent.
Conditional on the school!

Conditioning

Draw a box around the conditioned variables.

1. Conditioning on a variable in an open backdoor path removes the non-causal association (controls for confounding).
2. Conditioning on a collider opens the path that the collider was blocking.
3. Conditioning on a variable in the causal pathway (mediator) removes part of the causal effect.

Conditioning

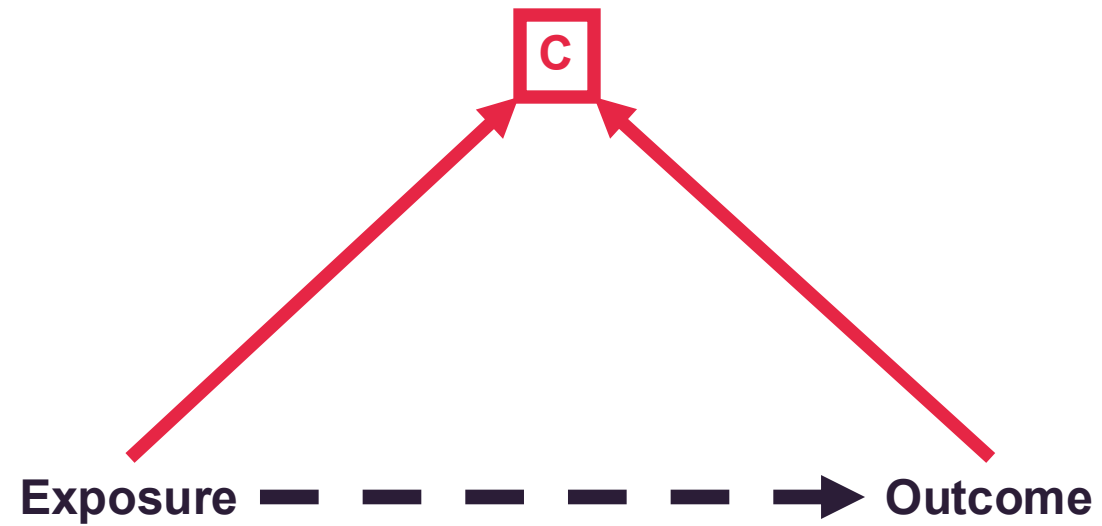


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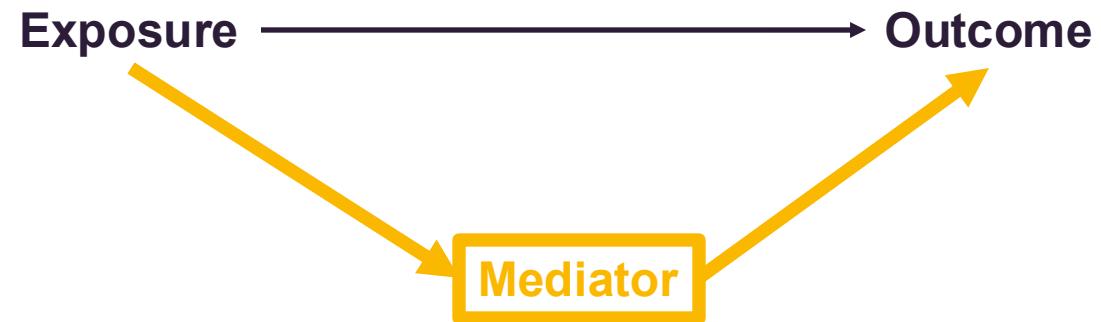


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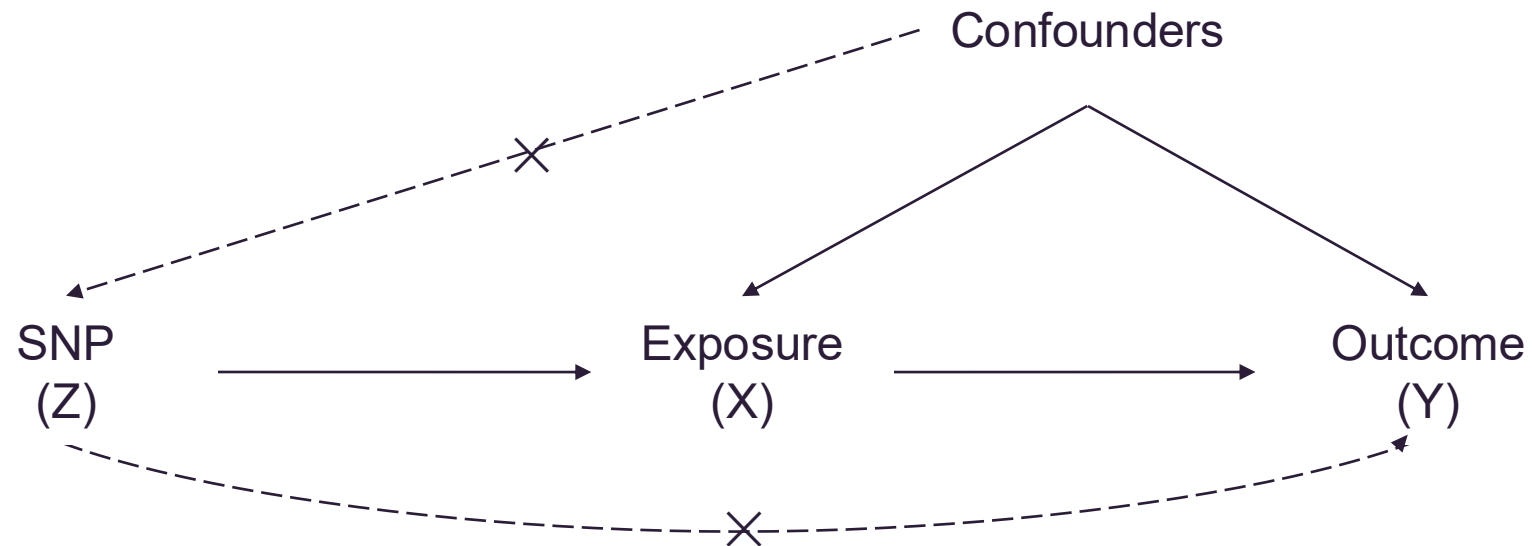
Conditioning



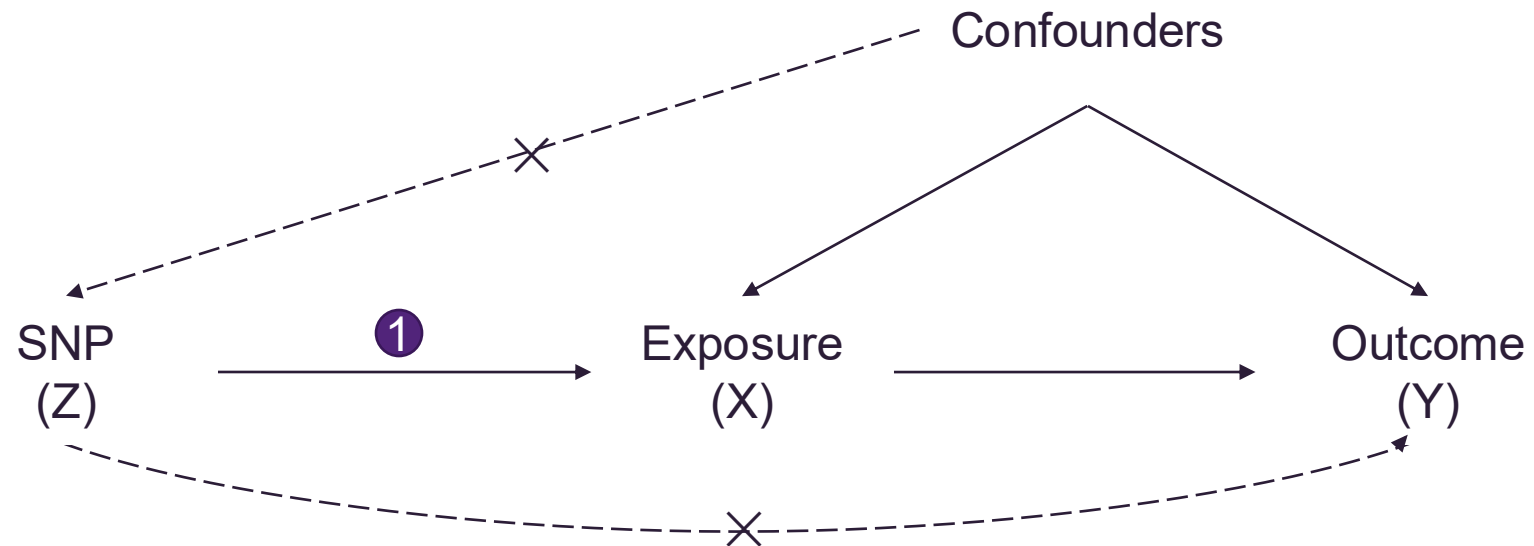
DAG elements

| Element | Description |
|---|--|
|  | Boxed elements indicate that the variable is conditioned on. |
|  | An arrow with a solid line indicates direct association between two variables. |
|  | An arrow with a dashed line indicates indirect association between two variables |
| C | Confounders. |
| U | Unmeasured confounders |

Assumptions underlying MR

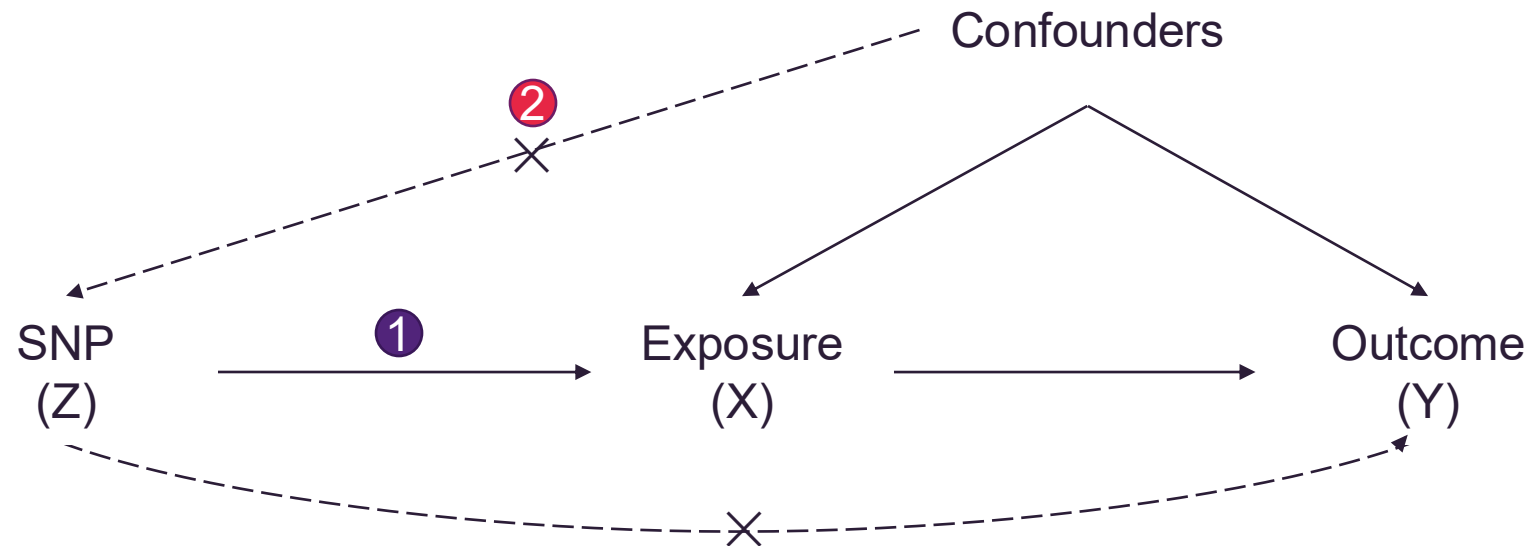


Assumptions underlying MR



(1) Relevance assumption: SNP is associated with the exposure

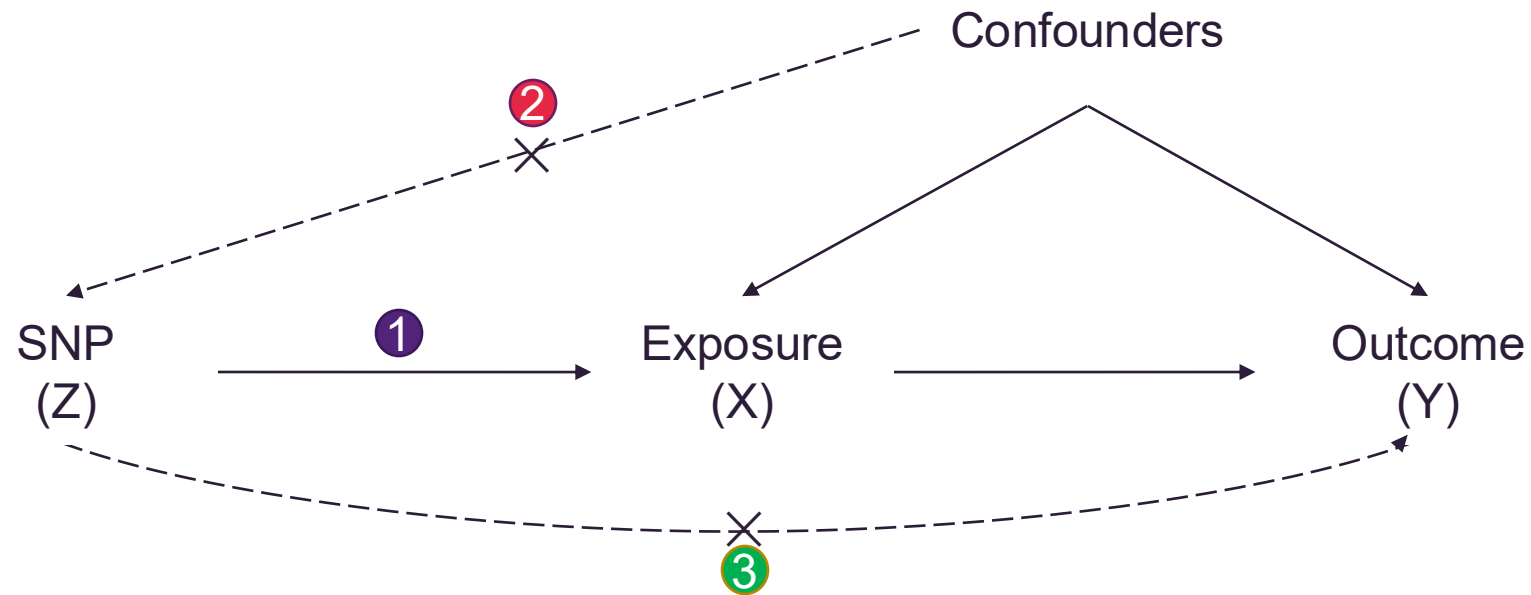
Assumptions underlying MR



(1) Relevance assumption: SNP is associated with the exposure

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Assumptions underlying MR

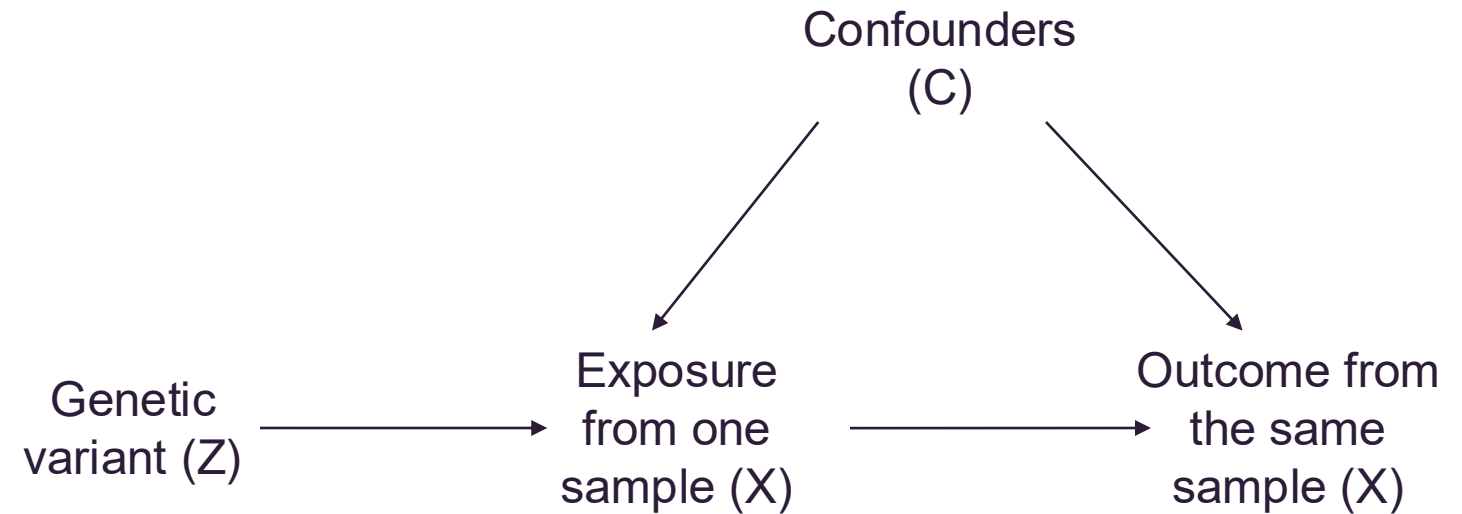


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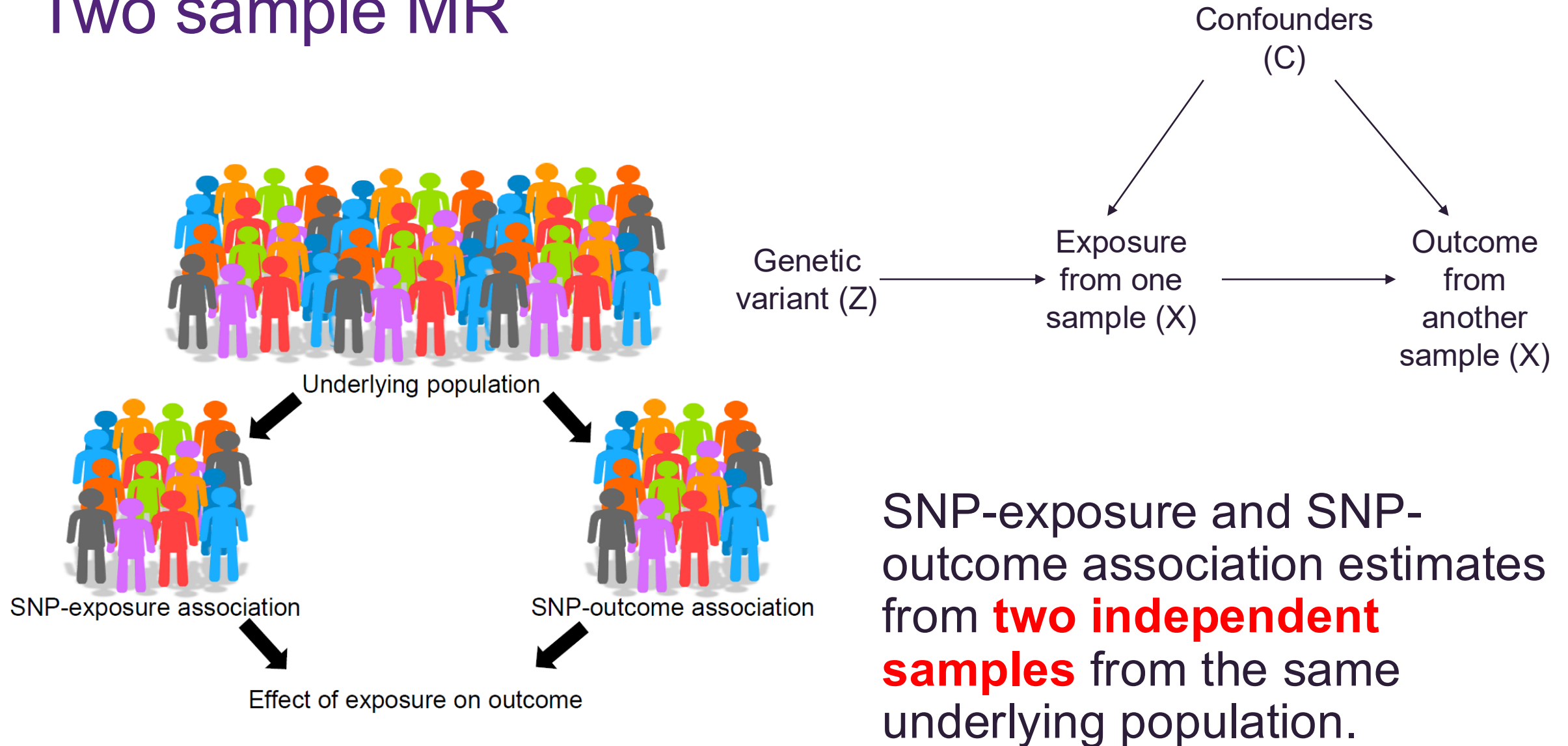
(3) Exclusion restriction: SNP ONLY associated outcome through the exposure

One-Sample MR



Genotypes, exposure and outcome are available on individuals from the same sample.

Two sample MR



Generate causal estimate

1. The association of the SNP and the outcome

} Test for existence of an effect

Generate causal estimate

1. The association of the SNP and the outcome
2. Two-stage least squares
3. The Wald estimator

} Test for existence of an effect

} Estimate the size of the effect

Calculating causal effect estimates

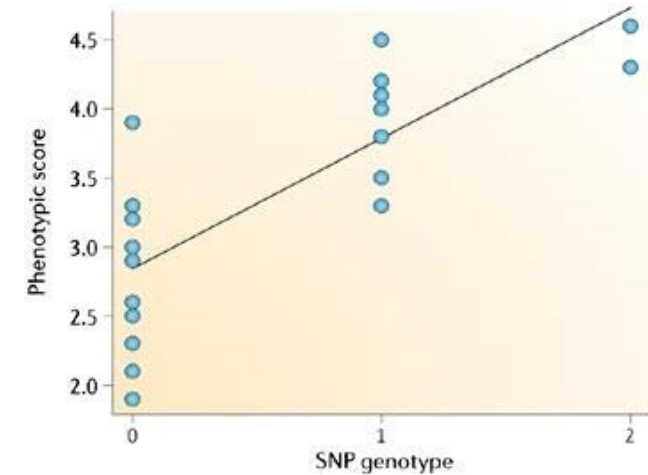
Two-Stage Least Squares

A single sample of individuals with data on the SNP, the exposure and the outcome. Also known as “One sample MR”.

Manual calculation:

1. Regress exposure on SNP to get predicted values.
2. Regress outcome on **predicted** exposure (from 1st stage regression).

The regression coefficient from the second stage is the estimate of the causal effect of the exposure on the outcome.



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Calculating causal effect estimates

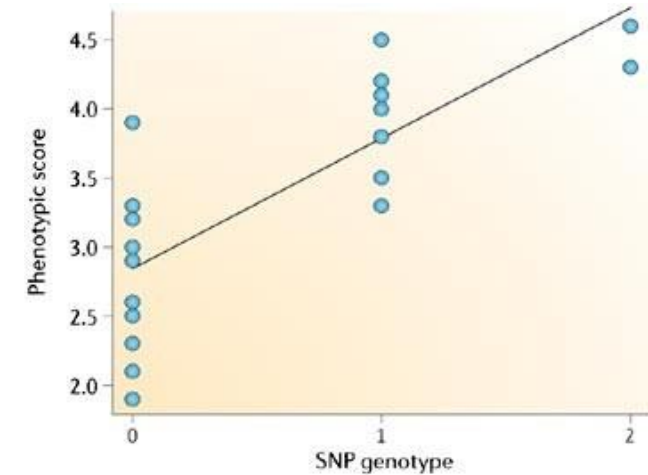
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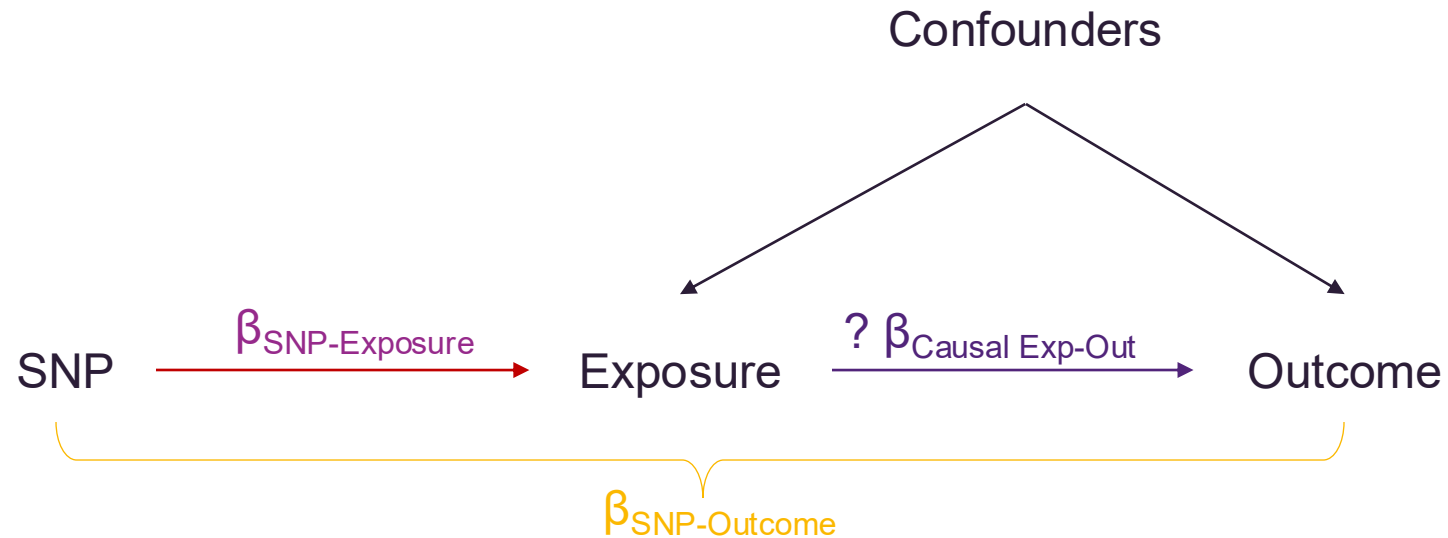


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This gives you: difference in outcome per unit change in (genetically-predicted) exposure

Calculating Causal Effect Estimates

Wald Estimator (Wald Ratio)



Where there is a linear relationship between SNP, exposure and outcome:

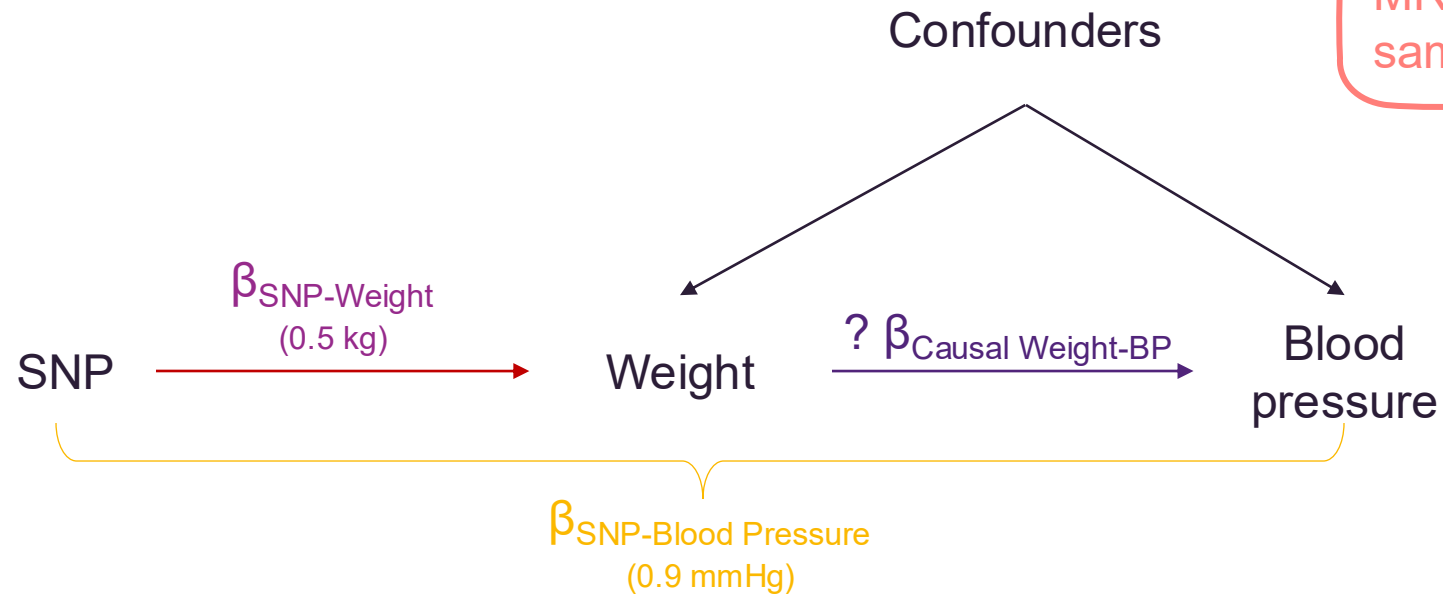
$$\beta_{\text{SNP-Outcome}} = \beta_{\text{Causal Exp-Out}} \times \beta_{\text{SNP-Exposure}}$$

$$\beta_{\text{Causal effect (Wald estimator)}} = \frac{\beta_{\text{SNP-Outcome}}}{\beta_{\text{SNP-Exposure}}}$$

Calculating Causal Effect Estimates

Wald Estimator (Wald Ratio)

Wald estimator can be used in one sample ("One sample MR") as well as different samples ("Two sample MR")



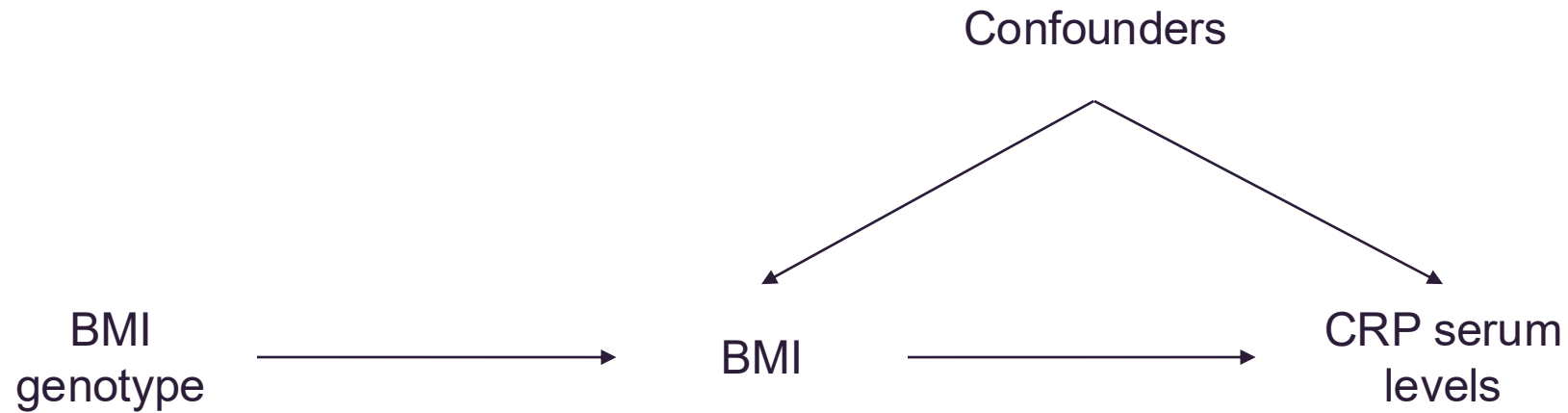
Where there is a linear relationship between SNP, exposure and outcome:

$$\beta_{\text{SNP-Outcome}} = \beta_{\text{Causal Exp-Out}} \times \beta_{\text{SNP-Exposure}}$$

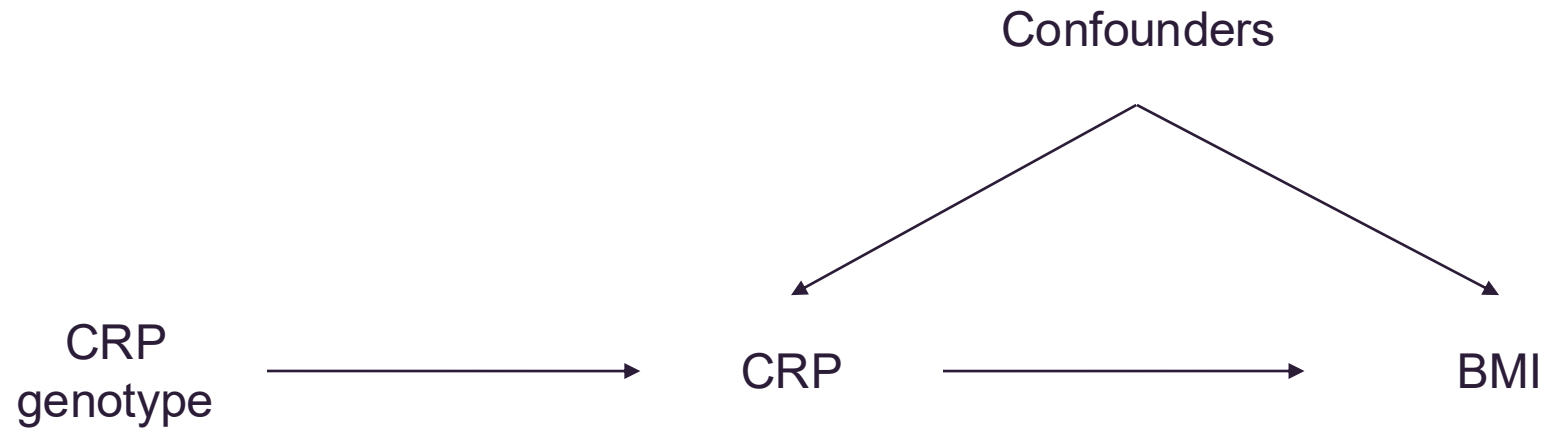
$$\beta_{\text{Causal effect}} \text{ (Wald estimator)} = \frac{\beta_{\text{SNP-Outcome}}}{\beta_{\text{SNP-Exposure}}}$$

$$\beta_{\text{Causal effect Weight-BP}} = \frac{0.9 \text{ mmHg/allele}}{0.5 \text{ kg/allele}} = 1.8 \text{ mmHg/kg}$$

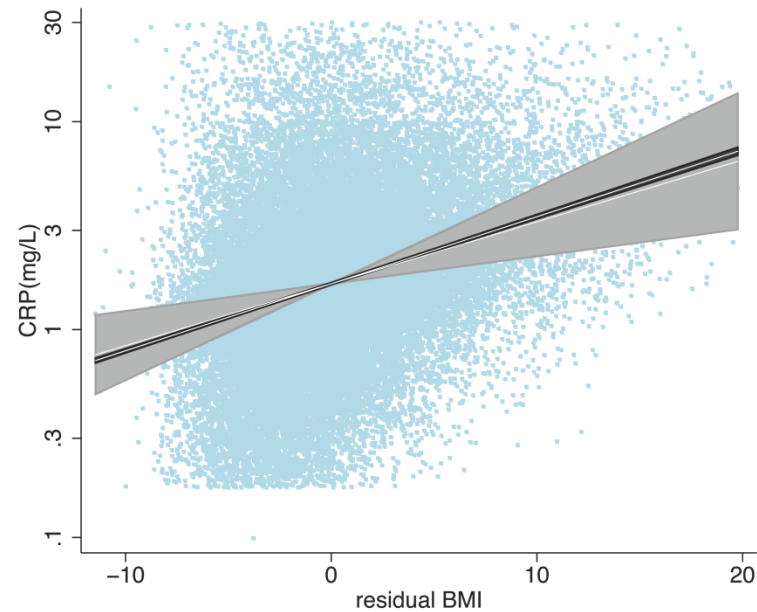
MR example: THE GOOD



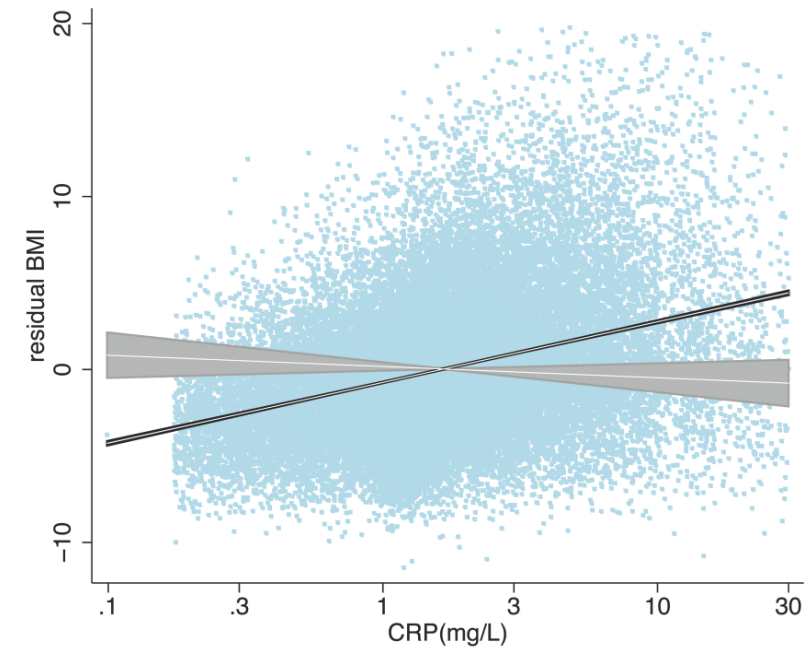
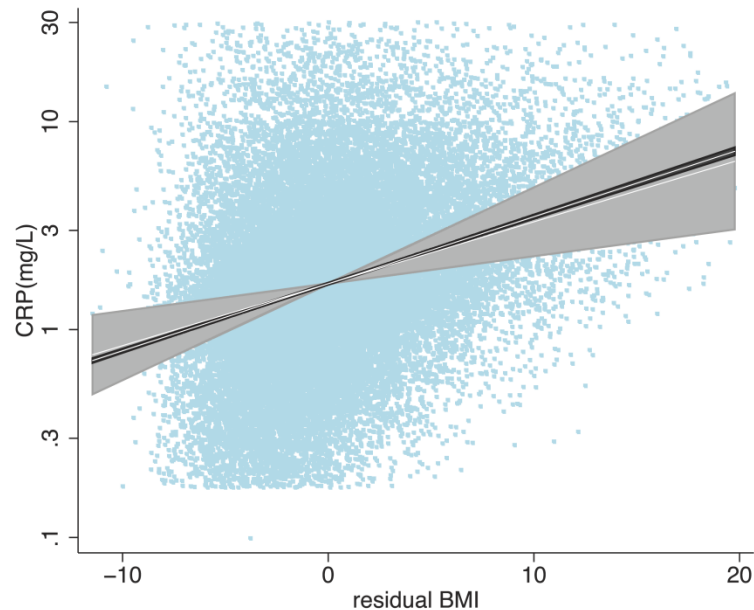
MR example: THE GOOD



| | Effect estimates | | | | |
|--------------------|---------------------------|----------------------------|----------|------------|-------------|
| Exposure → Outcome | Observational association | Instrumental variable (MR) | P_{IV} | P_{diff} | F_{first} |
| BMI → CRP | 1.075 (1.073, 1.077) | 1.06 (1.02, 1.11) | 0.002 | 0.6 | 50.2 |



| | Effect estimates | | | | |
|--------------------|---------------------------|----------------------------|----------|------------|-------------|
| Exposure → Outcome | Observational association | Instrumental variable (MR) | P_{IV} | P_{diff} | F_{first} |
| BMI → CRP | 1.075 (1.073, 1.077) | 1.06 (1.02, 1.11) | 0.002 | 0.6 | 50.2 |
| CRP → BMI | 1.58 (1.53, 1.63) | -0.30 (-0.78, 0.18) | 0.2 | <0.00001 | 78.3 |



MR Example: THE BAD

MR Example: THE BAD

[Nutrients](#). 2023 May; 15(9): 2091.

Published online 2023 Apr 26. doi: [10.3390/nu15092091](https://doi.org/10.3390/nu15092091)

PMCID: PMC10181479

PMID: [37432232](https://pubmed.ncbi.nlm.nih.gov/37432232/)

A Positive Causal Relationship between Noodle Intake and Metabolic Syndrome: A Two-Sample Mendelian Randomization Study

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A Positive Causal Relationship between Noodle Intake and Metabolic Syndrome: A Two-Sample Mendelian Randomization Study

Causal effects of COVID-19 on cancer risk: A Mendelian randomization study

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MR Example: THE BAD

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[Ann Transl Med](#). 2021 Feb; 9(3): 263.

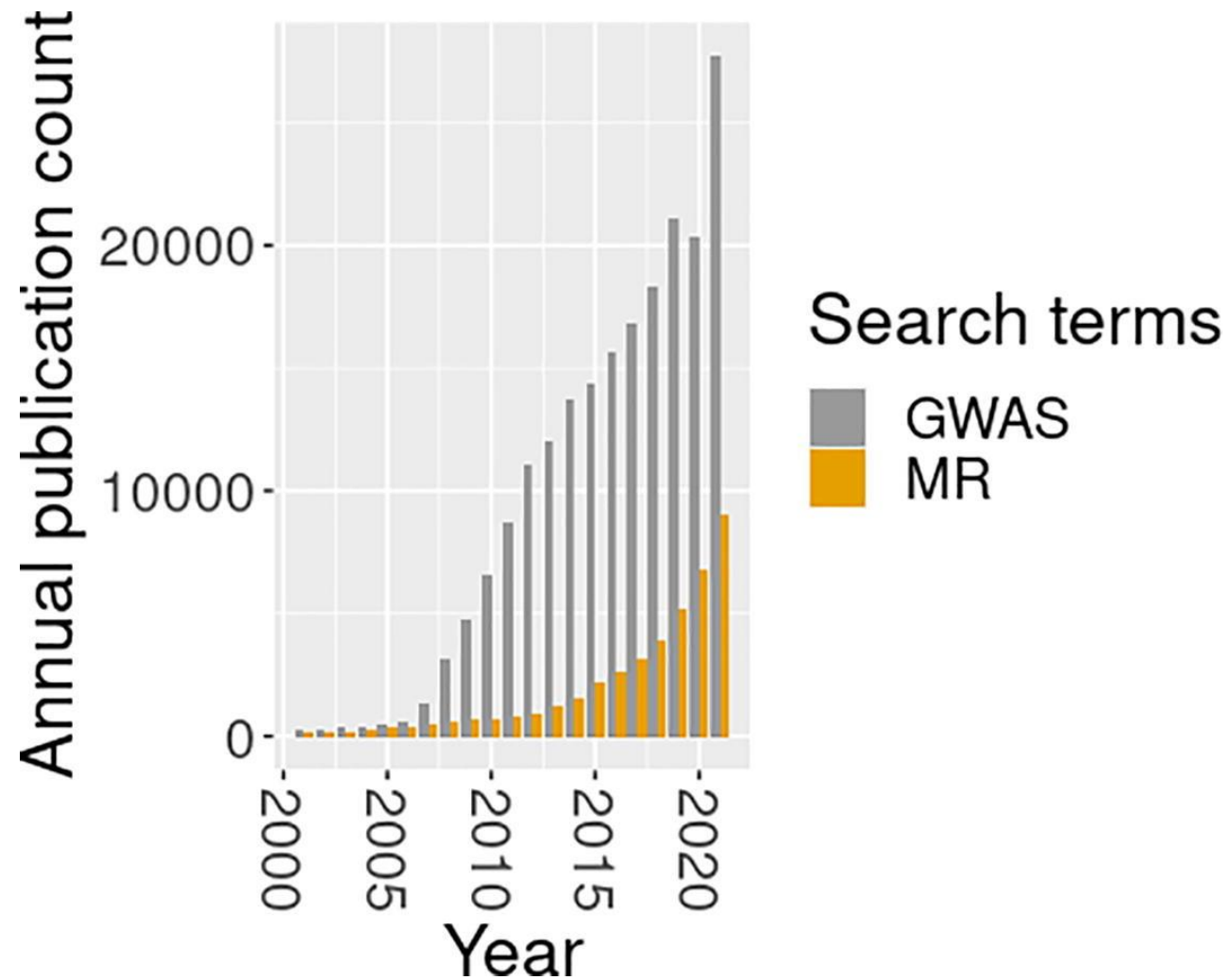
doi: [10.21037/atm-20-3063](https://doi.org/10.21037/atm-20-3063)

PMCID: PMC7940946

PMID: [33708890](https://pubmed.ncbi.nlm.nih.gov/33708890/)

Habitual consumption of alcohol with meals and lung cancer: a Mendelian randomization study

MR Example: THE BAD



Limitations of MR

Reasons for failing to observe a SNP-outcome association despite a real causal association existing

Power and weak instrument bias

Power:

- Genetic variants explain very small amounts of phenotypic variance in a given trait.
- VERY large sample sizes are generally required.

Weak instruments:

- Genetic variants that are weak proxies for the exposure.
- Results in biased causal estimates from MR.

Different impact of the bias from weak instruments:

- **One-Sample MR:** to the confounded estimate.
- **Two-Sample MR:** to the null.

Reasons for failing to observe a SNP-outcome association despite a real causal association existing

Power

http://cnsgenomics.com/shiny/mRnd/ mRnd: Power calculations f...

File Edit View Favorites Tools Help

mRnd: Power calculations for Mendelian Randomization

Continuous outcome Binary outcome Binary outcome derivations Citation About

Input

Calculate:

☒ Power
☐ Sample size

Provide:

Sample size

1000

α

0.05

Type-I error rate

β_{YZ}

0

Two-stage least squares

| | | |
|-------------|-------|--------------------------------|
| Power | 0.05 | |
| NCP | 0.00 | Non-Centrality-Parameter |
| F-statistic | 11.10 | The strength of the instrument |

Power or sample size calculations for two-stage least squares Mendelian Randomization studies using a genetic instrument Z (a SNP or allele score), a continuous exposure variable X (e.g. body mass index [BMI, $\frac{kg}{m^2}$]) and a continuous outcome variable Y (e.g. blood pressure [mmHg]).

YZ association

| | | |
|-------|------|--------------------------|
| Power | 0.05 | |
| NCP | 0.00 | Non-Centrality-Parameter |

Power or sample size calculations for the regression association of a genetic instrument Z (e.g. a BMI SNP), with a continuous outcome variable Y (blood pressure).

EN 2:26 PM 6/02/2017

Using Multiple Genetic Variants as Instruments

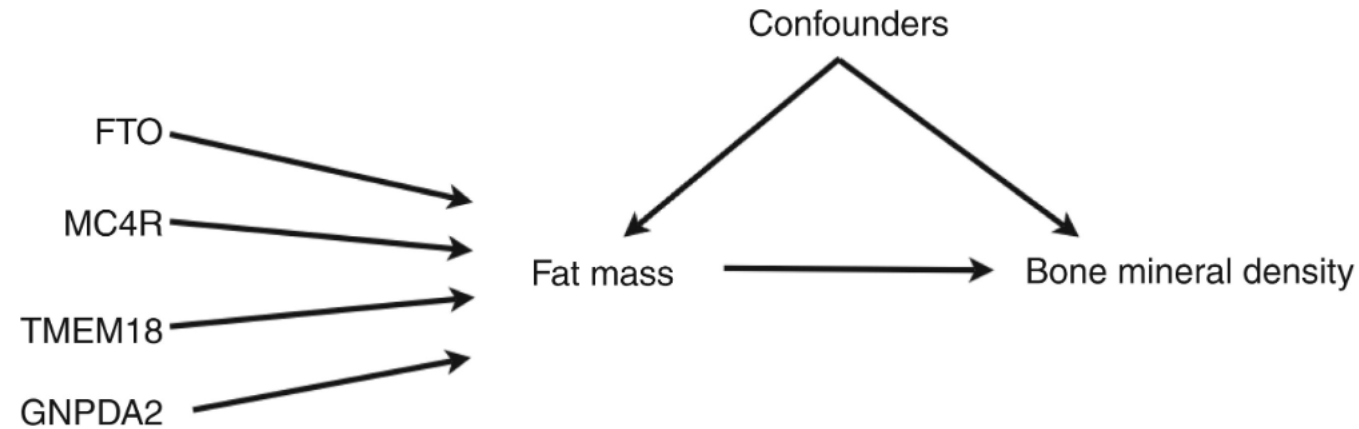


Figure 1. DAG for a Mendelian randomisation analysis using four genetic variants as instrumental variables for the effect of fat mass on bone mineral density.

Creating allelic scores using multiple genetic variants.

Testing multiple variants individually and then meta-analysing individual SNPs.

Reasons for detecting a causal SNP-outcome when it does not exist

Population Stratification:

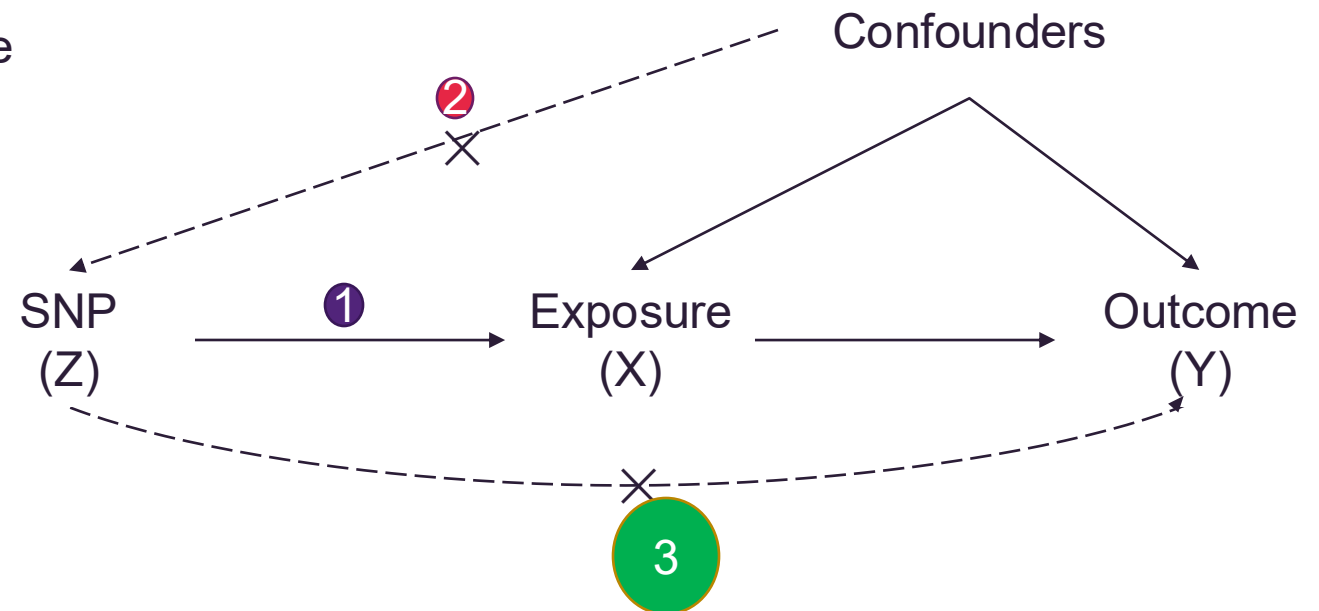
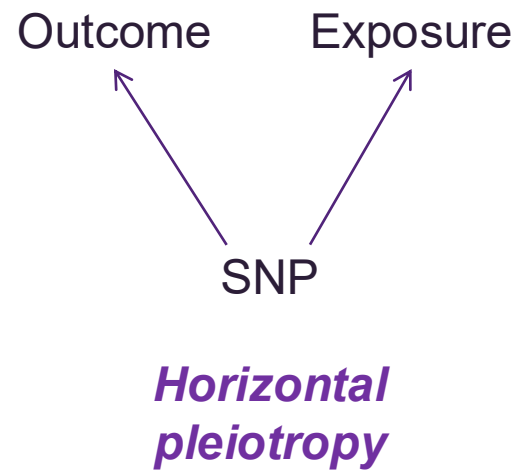
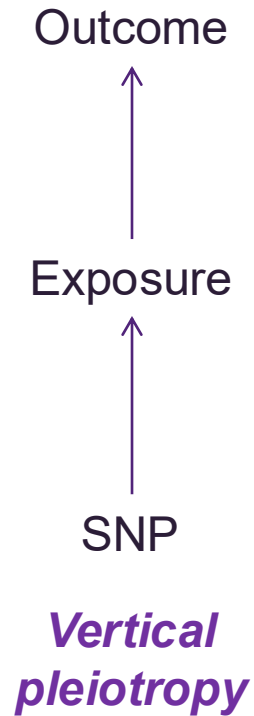
- Creates genetic confounding.
- Assumption 2 is violated.

Overlapping discovery GWAS and MR estimation samples.

Pleiotropy

- Multiple phenotypic effects.
- Assumption 3 is violated.

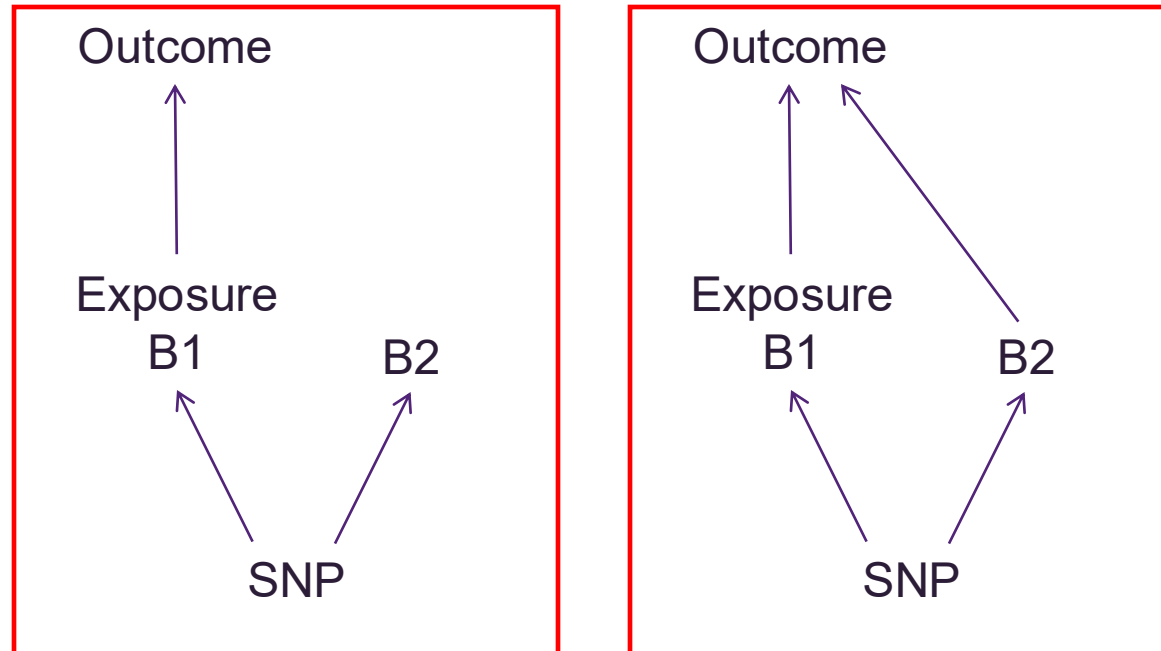
Pleiotropy: Genetic variant influences more than one trait




Horizontal Pleiotropy

Pleiotropy only violates MR's assumptions if it involves a pathway outside that of the exposure and is a pathway that affects your outcome.




Violation




MR Base



- Welcome to MR Base
- About
- Acknowledgements
- Changelog
- Data access agreement
- TwoSampleMR R package
- Perform MR analysis
 - Choose exposures
 - Choose outcomes
 - Run MR
- Quick SNP lookup





A platform for Mendelian randomisation using summary data from genome-wide association studies

Current status

Beta phase release

App version:
1.4.3 8a77eb (25 October 2020)

R version:
4.0.3

Host:
d81b2baaf993

R/TwoSampleMR version:
0.5.5

Database version:
0.3.0 (25 October 2020)

Before beginning analysis in the web application please do review the 'Data access agreement' in the sidebar.

25 October 2020 - Major updates - see Changelog

Information

This web-app represents relatively limited analytical scope compared to using the TwoSampleMR R package directly, which also enables analysis of your own outcome data:
<https://mrcieu.github.io/TwoSampleMR/>

See LD Hub for automated LD score regression:
<http://ldsc.broadinstitute.org/>

See EpiGraphDB for pre-calculated MR results and many other epidemiological datasets:
<https://www.epigraphdb.org/>

Data underlying this web-app are hosted by the OpenGWAS project:
<https://gwas.mrcieu.ac.uk>

The data is contributed by the international GWAS community - please see Acknowledgements and cite studies accordingly!

MR Dictionary

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The definitive list of terms for Mendelian randomization research

[Learn more about the project](#)Powered by Algolia

Recently added/updated:

[OneSampleMR](#)[Inverse variance weighted \(IVW\)](#)[fixed effects estimate](#)[debiased IVW](#)[Cis- and trans-variants](#)[MR for drug targets](#)[Browse All](#)

View all terms in the Dictionary in an A-Z list

[Definition](#)[Biases and limitations](#)[Weak instrument-robust one-sample methods](#)[Two-sample methods](#)[Genetic terms](#)[Related approaches](#)[One-sample methods](#)[Pleiotropy-robust one-sample methods](#)[Weak instrument-robust two-sample methods](#)

Conclusion

- MR uses genetic variants as proxies of modifiable exposures and can overcome some key limitations of observational studies.
- MR can reliably test for causal relationships, provided that three key assumptions are met.
- SNPs with known functional consequences increase the value of MR studies:
 - Less likely to violate the assumptions.
 - Increased biological understanding of the SNP -> exposure associations.
- Effect sizes are likely to be small, so sample sizes need to be very large.

Useful references

George Davey Smith, Gibran Hemani, Mendelian randomization: genetic anchors for causal inference in epidemiological studies, *Human Molecular Genetics*, Volume 23, Issue R1, 15 September 2014, Pages R89–R98, <https://doi.org/10.1093/hmg/ddu328>

Brion, Marie-Jo A et al. “Calculating statistical power in Mendelian randomization studies.” *International journal of epidemiology* vol. 42,5 (2013): 1497-501. doi:10.1093/ije/dyt179

Davey-Smith & Ebrahim (2003). "Mendelian randomization": can genetic epidemiology contribute to understanding environmental determinants of disease? *IJE*, 32. 1-22

Davies et al (2018). Reading Mendelian randomization studies: a guide. glossary, and checklist for clinicians. *BMJ*. Jul 12, 362:601

Evans & Davey-Smith (2015). Mendelian randomization: New applications in the coming age of hypothesis free causality. *Annu Rev Genomics Hum Genet*, 16, 327-50

Sanderson, E., Glymour, M.M., Holmes, M.V. *et al*. Mendelian randomization. *Nat Rev Methods Primers* **2**, 6 (2022). <https://doi.org/10.1038/s43586-021-00092-5>

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