



Leveraging Summary-data-based Mendelian Randomisation for Gene Target Discovery

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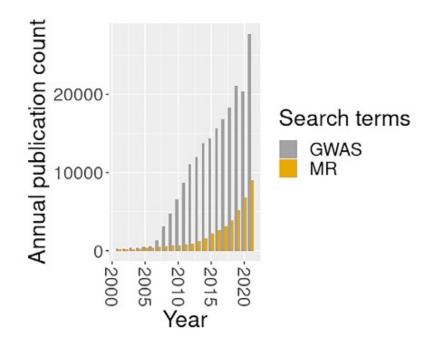
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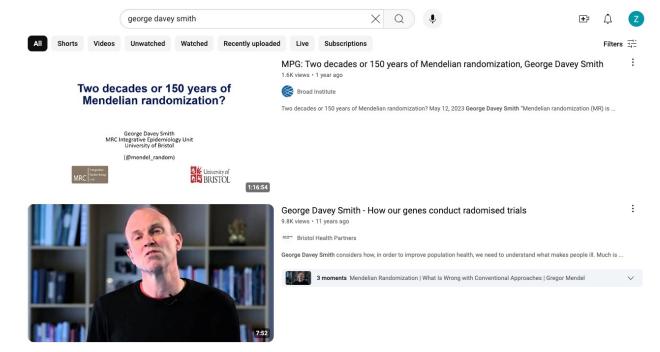
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Why Is Mendelian Randomisation?





Boehm et al. 2022

From YouTube



ZHIHONG ZHU
11. JULY 2025 SENIORFORSKER



What Is Mendelian Randomisation?

• Flexible

Fewer ethical restrictions

Accessible

GWAS summary data

LD reference data

Robust

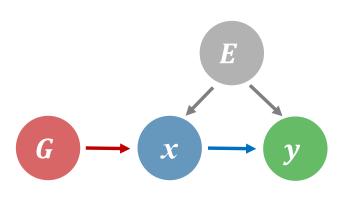
Less susceptible to environmental confounders and reverse causation







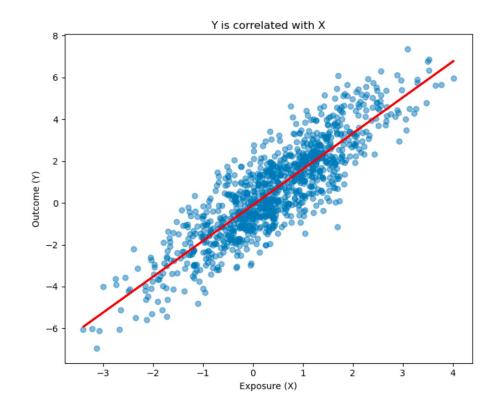
What Is Mendelian Randomisation?



GWAS data $(G \rightarrow Y)$

eQTL data $(G \rightarrow X)$

LD reference data

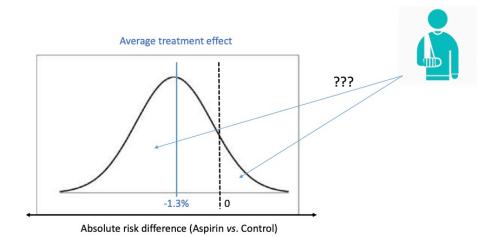


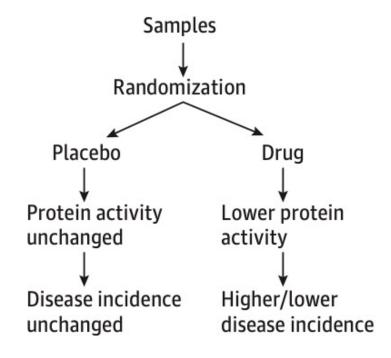




How Does Mendelian Randomisation Work?

Causal Inference

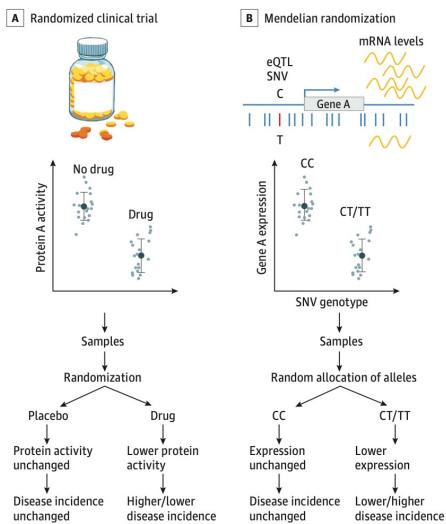








How Does Mendelian Randomisation Work?

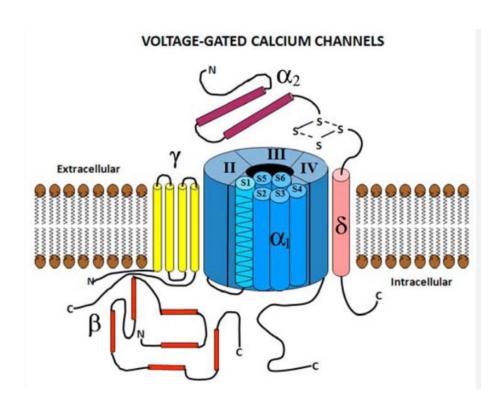






Voltage-Dependent Calcium Channel Complex

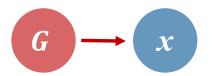
- Regulates calcium ion entry into cells
- Drug targets for hypertensive disease,
 cardiovascular diseases, psychiatric diseases,
 neurologic diseases, retinal diseases etc.
- Coding gene of CACNA2D4, part of the voltage-dependent calcium channel complex



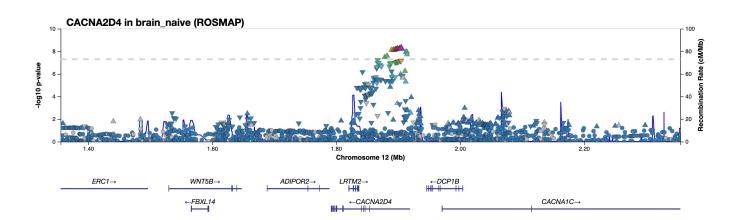




CACNA2D4, Predicting Gene Expression

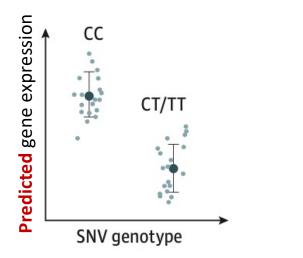


- cis-eQTL data
 - ☐ Association between SNP and exposure



- Assumption
 - ☐ Strong association between SNP and exposure
 - ☐ Linear relationship between SNP and exposure
- Genetically predicted exposure

$$\square \ \hat{x}_j = z_j \hat{\delta} + e_{x(j)}$$

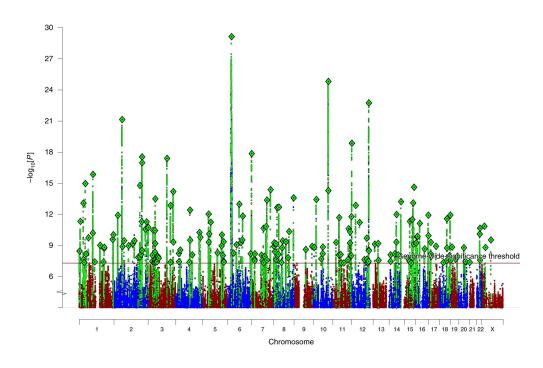


CACNA2D4, Predicting Disease Risk



- GWAS data
 - ☐ Association between SNP and outcome
- Assumption
 - ☐ Linear relationship between SNP and outcome
- Genetically predicted outcome

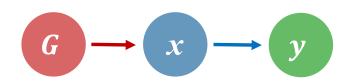
$$\square \ \hat{y}_j = z_j \hat{\gamma} + e_{y(j)}$$

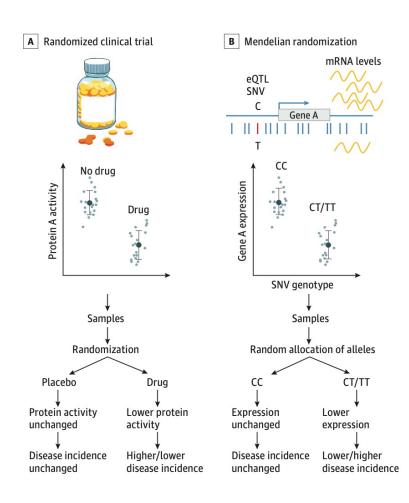


Lam et al 2019 Nature Genetics

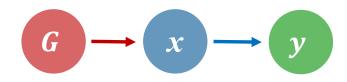
Summary-data-based MR

- SMR estimate
 - ☐ Assumption: Single causal variant, linear relationship between exposure and outcome
 - \Box Estimate: $\hat{\beta}_{SMR} = \hat{\gamma}/\hat{\delta}$
 - ☐ Interpretation: a *x* mg/L (1SD unit) higher exposure increase/decrease *y*% genetic risk of disease outcome
 - ☐ Equivalent to estimate from regression if individual-level data are available.





Proof of MR Estimate



- $E(\hat{\beta}_{SMR}) = \hat{\gamma}/\hat{\delta} = (\hat{\gamma} \times \hat{\delta})/(\hat{\delta} \times \hat{\delta})$
- SNP-exposure association: $\hat{\delta} = (z^T z)^{-1} z^T x$ SNP-outcome association: $\hat{\gamma} = (z^T z)^{-1} z^T y$
- $E(\hat{\beta}_{SMR}) = \hat{\gamma}/\hat{\delta} = (\hat{\gamma} \times \hat{\delta})/(\hat{\delta} \times \hat{\delta}) = \frac{x^T P_z y}{x^T P_z x} = \beta + \frac{x^T P_z e}{x^T P_z x}$, where $P_z = z(z^T z)^{-1} z^T$
- DNA variants are independent of environmental factors, $z^T e = 0$ $E(\hat{\beta}_{SMR}) = \beta$





CACNA2D4 - SMR Calculation

Gene	SNP	A1 / A2	Data	b	SE	<i>P</i> -value
CACNA2D4	rs1044825	G/T	eQTL (blood)	0.447	0.0186	4.1E-128
			GWAS (schizophrenia)	-0.0377	0.0087	1.3E-5

$$\hat{\beta} \approx \frac{\hat{\gamma}}{\hat{\delta}} = -\frac{0.0377}{0.447} = -0.084$$

$$\longrightarrow$$
 P-value = 2.0E-5

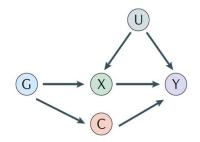
$$SE(\hat{\beta}) \approx \sqrt{\left(\frac{\gamma}{\delta}\right)^2 \left[\frac{var(\delta)}{\delta^2} + \frac{var(\gamma)}{\gamma^2}\right]} = \sqrt{\left(\frac{0.45}{-0.04}\right)^2 \left[\frac{0.02^2}{0.45^2} + \frac{0.01^2}{(-0.04)^2}\right]} = 0.020$$



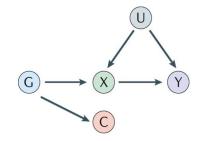


Bias Due to Pleiotropy

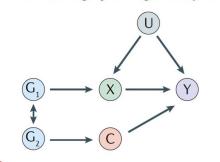
a Horizontal pleiotropy



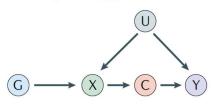
b Horizontal pleiotropy



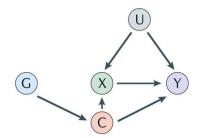
c Confounding by linkage disequilibrium



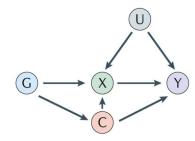
d Vertical pleiotropy



e Misspecification of the primary phenotype



f Correlated pleiotropy



Sanderson et al. Nature Reviews 2022





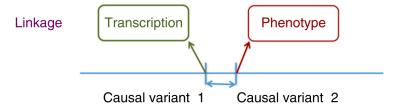
How to Examine the LD Confounding

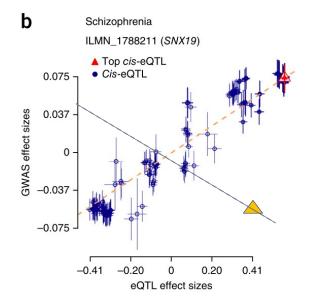
• HEIDI (<u>He</u>terogeneity <u>in D</u>ependent <u>Instruments</u>)

H0: No difference

H1: Significant difference at two

correlated SNPs

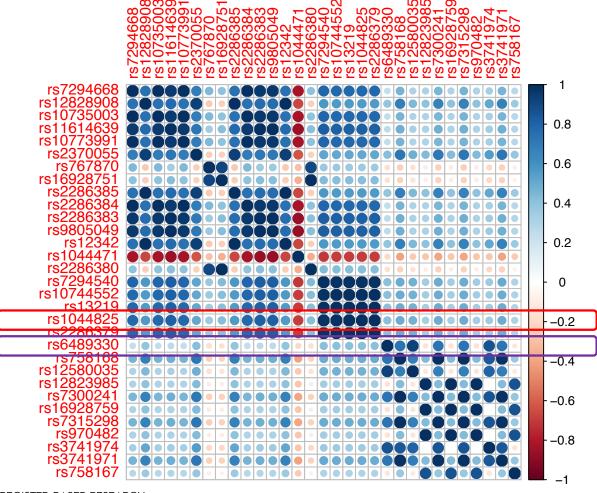








SMR/HEIDI – CACNA2D4



The top-associated SNP The SNP to test difference



NATIONAL CENTRE FOR REGISTER-BASED RESEARCH



SMR/HEIDI – CACNA2D4

SNP	A1 / A2	Data	b	SE	<i>P</i> -value
rs1044825	G/T	eQTL (blood)	0.447	0.0186	4.1E-128
		GWAS (schizophrenia)	-0.0377	0.0087	1.3E-5
rs6489330	A/G	eQTL (blood)	0.211	0.02384	9.5E-19
LD $r = 0.413$		GWAS (schizophrenia)	-0.0378	0.0108	4.7E-4

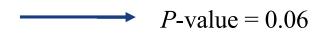
rs1044825,
$$\hat{\beta}_1 = -0.084$$
, SE $(\hat{\beta}_1) \approx 0.020$ rs6489330, $\hat{\beta}_2 = -0.179$, SE $(\hat{\beta}_2) \approx 0.055$

$$rs6489330, \hat{\beta}_2 = -0.179, SE(\hat{\beta}_2) \approx 0.055$$

Difference,
$$\hat{d} = \hat{\beta}_2 - \hat{\beta}_1 = -0.179 + 0.084 = -0.095$$

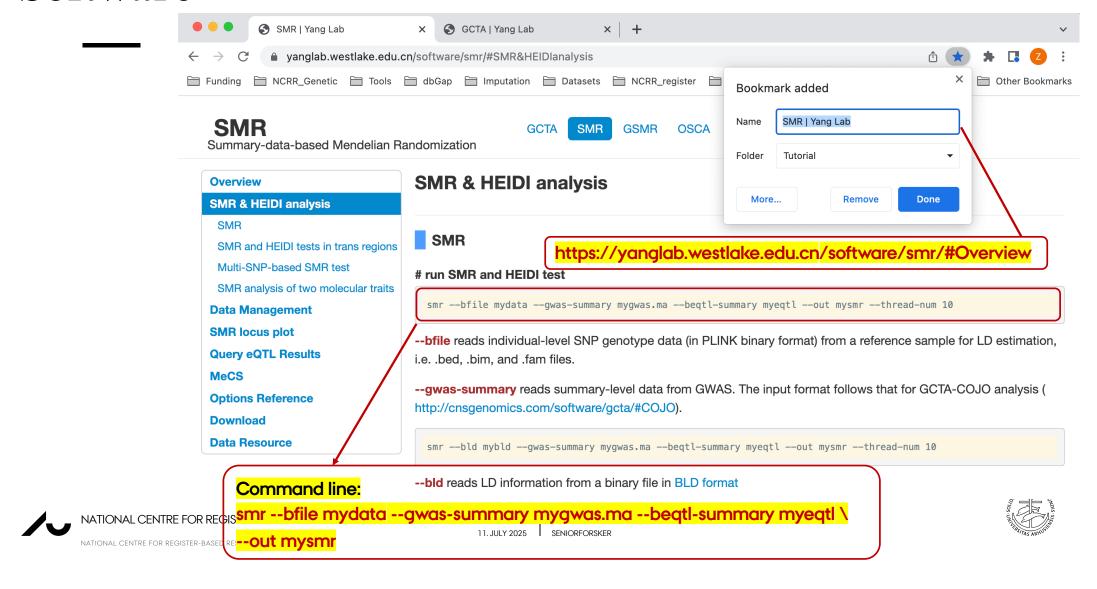
$$SE(\hat{d}) = \sqrt{var(\hat{\beta}_2 - \hat{\beta}_1)} = \sqrt{var(\hat{\beta}_2) + var(\hat{\beta}_1) - 2 \times cov(\hat{\beta}_1, \hat{\beta}_2)} = 0.050$$



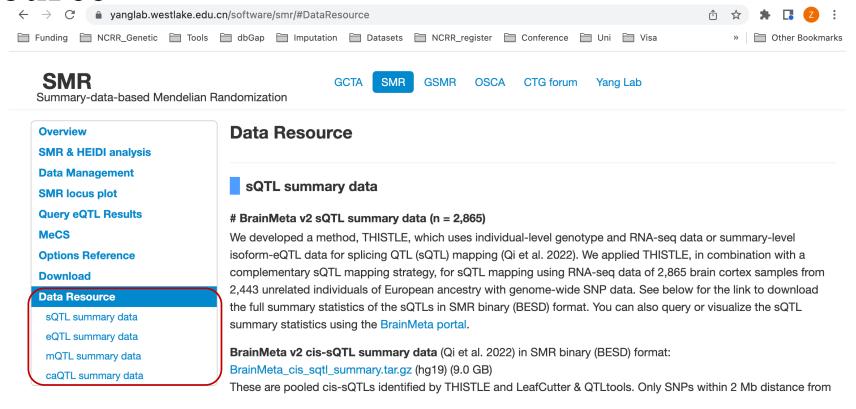




Software



Data Resource



sQTL – Summary statistics of splicing QTLs

eQTL – Summary statistics from associations of gene expression

mQTL – Summary statistics from associations of methylation





Finished? - No

- Interpretation is crucial
- Checklist

Experimental design

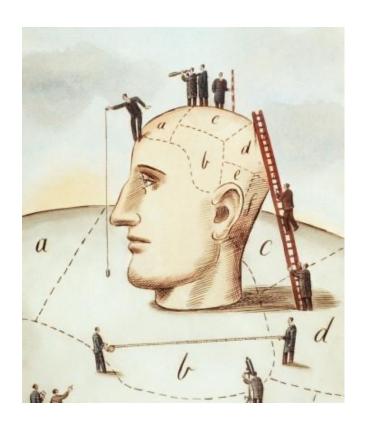
Cohorts used in GWAS studies

Biological context, such as age, sex, tissues, cell types etc.

Selection of SNP instruments

Sample sizes

. . .







Validating Assumptions

Table S13 Correlations between effect sizes of SNPs on brain *C4* gene expressions and neonatal circulating C4 protein concentration, related to the STAR Methods

Tissue	Brain C4A expression		Brain C4B expression	
113340	r _b (SE)	<i>P</i> -value	r _b (SE)	<i>P</i> -value
Brain - Amygdala	0.73 (0.02)	<1.0E-100	0.14 (0.11)	0.20
Brain - Anterior cingulate cortex BA24	0.79 (0.03)	<1.0E-100	-0.99 (0.22)	7.2E-06
Brain - Caudate basal ganglia	0.67 (0.01)	<1.0E-100	-1.01 (0.09)	7.9E-27
Brain - Cerebellar hemisphere	0.59 (0.01)	<1.0E-100	-0.78 (0.04)	5.3E-100
Brain - Cerebellum	0.55 (0.01)	<1.0E-100	-0.70 (0.02)	<1.0E-100
Brain - Cortex	0.64 (0.02)	<1.0E-100	-0.84 (0.04)	3.2E-85
Brain - Frontal cortex BA9	0.88 (0.02)	<1.0E-100	-0.88 (0.05)	5.8E-64
Brain - Hippocampus	0.70 (0.01)	<1.0E-100	0.77 (0.09)	2.0E-17
Brain - Hypothalamus	0.85 (0.02)	<1.0E-100	-0.44 (0.05)	2.1E-20
Brain - Nucleus accumbens basal ganglia	0.77 (0.02)	<1.0E-100	-0.91 (0.08)	5.6E-33
Brain - Putamen basal ganglia	0.72 (0.02)	<1.0E-100	-0.78 (0.04)	3.2E-71
Brain - Spinal cord cervical c-1	1.01 (0.04)	<1.0E-100	-0.96 (0.12)	1.0E-16
Brain - Substantia nigra	0.75 (0.03)	<1.0E-100	0.12 (0.02)	3.2E-11
Nerve - Tibial	0.58 (0.01)	<1.0E-100	0.36 (0.02)	5.1E-65
Pituitary	0.70 (0.01)	<1.0E-100	-0.01 (0.03)	0.63
Average	0.73		0.46	

Borbye-Lorenzen et al. 2023 Cell Genomics



Note: the Bonferroni-corrected threshold is 0.003 (= 0.05/15).



STROBE MR Checklist

STROBE-MR checklist of recommended items to address in reports of Mendelian randomization studies¹²

ltem No.	Section	Checklist item	Page No.	Relevant text from manuscript
1	TITLE and ABSTRACT	Indicate Mendelian randomization (MR) as the study's design in the title and/or the abstract if that is a main purpose of the study	1	Title page
	INTRODUCTION			
2	Background	Explain the scientific background and rationale for the reported study. What is the exposure? Is a potential causal relationship between exposure and outcome plausible? Justify why MR is a helpful method to address the study question	4-5	Introduction section
3	Objectives	State specific objectives clearly, including pre-specified causal hypotheses (if any). State that MR is a method that, under specific assumptions, intends to estimate causal effects	5	Final paragraph
	METHODS			
4	Study design and data sources	Present key elements of the study design early in the article. Consider including a table listing sources of data for all phases of the study. For each data source contributing to the analysis, describe the following:	6	Study design
	a)	Setting: Describe the study design and the underlying population, if possible. Describe the setting, locations, and relevant dates, including periods of recruitment, exposure, follow-up, and data collection, when available.	6-7	Data sources section
	b)	Participants: Give the eligibility criteria, and the sources and methods of selection of participants. Report the sample size, and whether any power or sample size calculations were carried out prior to the main analysis	6-7	Data sources section
	c)	Describe measurement, quality control and selection of genetic variants	6-7	Data sources section
	d)	For each exposure, outcome, and other relevant variables, describe methods of assessment and diagnostic criteria for diseases	7	Instrument selection section
	e)	Provide details of ethics committee approval and participant informed consent, if relevant	NA	NA





Links

- SMR: https://yanglab.westlake.edu.cn/software/smr/
- SMR portal: https://yanglab.westlake.edu.cn/smr-portal/
- STROBE-MR checklist

https://www.bmj.com/sites/default/files/attachments/bmj-article/pre-pub-history/strobe-mr-checklist-fillable_r2.pdf





